



ACADGILD

Session 11: Random variable and Normal Distribution

Assignment 1

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Assignment

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1. Introduction

In this assignment, you will learn to solve problems on Normal distribution, Functions of Random Variables

2. Objective

The objective of this course is to solve problems related to Normal distribution, Functions of Random Variables

3. Prerequisites

Not applicable.

4. Associated Data Files

Not applicable.

5. Problem Statement

1. The time required for servicing transmissions is normally distributed with $\mu = 45$ minutes and $\sigma = 8$ minutes. The service manager plans to have work begin on the transmission of a customer's car 10 minutes after the car is dropped off and the customer is told that the car will be ready within 1 hour from drop-off. What is the probability that the service manager cannot meet his commitment?
 - A. 0.3875
 - B. 0.2676
 - C. 0.5
 - D. 0.6987
2. The current age (in years) of 400 clerical employees at an insurance claims processing center is normally distributed with mean $\mu = 38$ and Standard deviation $\sigma = 6$. For each statement below, please specify True/False. If false, briefly explain why.
 - A. More employees at the processing center are older than 44 than between 38 and 44.
 - B. A training program for employees under the age of 30 at the center would be expected to attract about 36 employees.
3. If $X_1 \sim N(\mu, \sigma^2)$ and $X_2 \sim N(\mu, \sigma^2)$ are *iid* normal random variables, then what is the difference between $2X_1$ and $X_1 + X_2$? Discuss both their distributions and parameters.
4. Let $X \sim N(100, 20^2)$. Find two values, a and b , symmetric about the mean, such that the probability of the random variable taking a value between them is 0.99.
 - A. 90.5, 105.9
 - B. 80.2, 119.8
 - C. 22, 78

- D. 48.5, 151.5
 - E. 90.1, 109.9
5. Consider a company that has two different divisions. The annual profits from the two divisions are independent and have distributions $\text{Profit}_1 \sim N(5, 3^2)$ and $\text{Profit}_2 \sim N(7, 4^2)$ respectively. Both the profits are in \$ Million. Answer the following questions about the total profit of the company in Rupees. Assume that \$1 = Rs. 45
- A. Specify a Rupee range (centered on the mean) such that it contains 95% probability for the annual profit of the company.
 - B. Specify the 5th percentile of profit (in Rupees) for the company
 - C. Which of the two divisions has a larger probability of making a loss in a given year?

6. Expected Output

7. Approximate Time to Complete Task