ACCOUNTING FOR ULTRASONIC SIGNAL ATTENUATION THROUGH MODEL PARAMETER INTERPOLATION

Myung-Hyun Yoon and Tenkasi V. Ramabadran Department of Electrical Engineering and Computer Engineering Center for Nondestructive Evaluation Iowa State University Ames, IA 50011

INTRODUCTION

In ultrasonic NDE of materials, deconvolution techniques are widely used to improve time/space resolution, minimize spectral coloring, and compensate for different experimental settings, e.g., transducer variations, pulser-receiver energy/damping settings, etc. The reference signal that is used for deconvolution is typically obtained as the front (or back) surface echo from a suitable sample under conditions identical to those used in acquiring the signal to be processed (deconvolved). When the signal to be processed is acquired from an attenuating medium, the effect of signal attenuation should be appropriately accounted for in the deconvolution technique. If the signal arises from a localized inhomogeneity as in the case of flaw scattered signals, this is easily accomplished by suitably modifying the reference signal; for instance, in the Wiener filter based deconvolution technique [1], the frequency dependent attenuation corresponding to the flaw location is determined and incorporated into the reference signal spectrum. When the inhomogeneities are distributed throughout the material as in the case of grain backscattered signals, the correction for attenuation should vary along the depth of the material. A suitable deconvolution technique for incorporating such correction is based on the Kalman filter [2, 3]. In this technique, the reference signal and the signal to be processed are modeled respectively as the impulse response of a system and the system output. The input to the system is the deconvolved signal that has to be estimated. The Kalman filter algorithm processes the data sequentially and its formulation allows the system parameters to change at each step. This property can be taken advantage of in providing varying amounts of correction for attenuation along the depth of the material.

In this paper, we investigate the use of a model parameter interpolation method to provide suitable correction for attenuation. System models (AR or ARMA) are first built for the front and back surface echos obtained from a suitable sample. The parameters of these models are then interpolated to obtain models corresponding to intermediate depths. The impulse responses of the interpolated models represent the reference signals corrected for attenuation. The effectiveness of this approach is evaluated using experimentally obtained signals from copper samples of different thicknesses (1/4'', 1/2'', 3/4'') and (1'').

MODELING THE REFERENCE SIGNAL

In the Kalman filter based deconvolution technique, the signal to be processed, e.g., grain backscattered signal, is modeled as follows:

$$z(k) = u(k) * r(k) + v(k) = y(k) + v(k),$$
 (1)

where k denotes the sample index, "*" denotes deconvolution, z(k) is the measured signal to be processed, v(k) is the measurement noise, r(k) is the reference signal, and u(k) is the deconvolved signal to be estimated. If we regard r(k) as the impulse response of a system and u(k) as the system input, the measured signal z(k) is just the system output y(k) corrupted by the additive noise v(k). Using state-space notation, (1) can be expressed as follows:

$$\mathbf{x}(k+1) = \mathbf{F}_k \mathbf{x}(k) + \mathbf{G}_k u(k)$$

$$z(k) = \mathbf{H}_k \mathbf{x}(k) + v(k),$$
(2)

$$z(k) = \mathbf{H}_k \mathbf{x}(k) + v(k), \tag{3}$$

where $\mathbf{x}(k)$ is the $(N \times 1)$ system state vector, \mathbf{F}_k is the $(N \times N)$ state transition matrix, G_k is the $(N \times 1)$ input matrix, and H_k is the $(1 \times N)$ measurement matrix. The matrices \mathbf{F}_k , \mathbf{G}_k , and \mathbf{H}_k which describe the system are chosen such that the system impulse response approximates the reference signal r(k).

Two of the popular system models are the ARMA (Auto-Regressive Moving Average) and the AR (Auto-Regressive) models. The difference equation relating the input and output of an N-th order ARMA model is given by

$$y(n) + \alpha_{1,k}y(n-1) + \alpha_{2,k}y(n-2) + \dots + \alpha_{N,k}y(n-N) = \beta_{1,k}u(n-1) + \beta_{2,k}u(n-2) + \dots + \beta_{N,k}u(n-N),$$
 (4)

where n is the sample index and $(\alpha_{i,k}, \beta_{i,k}: i = 1, 2, ..., N)$ represent the system parameters. These parameters are chosen to minimize the average squared error between r(n) and the system impulse response, i.e., y(n) when u(n) is the unit sample sequence. This is accomplished using a nonlinear least squares optimization technique, viz., Levenberg-Marquardt method [4]. In Z-transform notation, the system function of the ARMA model in (4) is represented by

$$H_k(Z) = \frac{\beta_{1,k} Z^{-1} + \beta_{2,k} Z^{-2} + \dots + \beta_{N,k} Z^{-N}}{1 + \alpha_{1,k} Z^{-1} + \alpha_{2,k} Z^{-2} + \dots + \alpha_{N,k} Z^{-N}}.$$
 (5)

The system matrices corresponding to the ARMA model in (4) are realized in the controllable canonical form as follows:

$$\mathbf{F}_{k} = \begin{pmatrix} 0 & 1 & \cdots & 0 \\ 0 & 0 & \cdots & 0 \\ \vdots & \vdots & & \vdots \\ -\alpha_{N,k} & -\alpha_{N-1,k} & \cdots & -\alpha_{1,k} \end{pmatrix}, \quad \mathbf{G}_{k} = \begin{pmatrix} 0 \\ 0 \\ \vdots \\ 1 \end{pmatrix}, \\ \mathbf{H}_{k} = \begin{pmatrix} \beta_{N,K} & \beta_{N-1,k} & \cdots & \beta_{1,k} \end{pmatrix}.$$
 (6)

In the case of an AR system model, (4), (5) and (6) are modified so that $\beta_{1,k} = 1$ and $\beta_{i,k} = 0 \text{ for } i = 2, 3, \dots, N.$

PARAMETER INTERPOLATION

Suppose $(\alpha_{i,0}, \beta_{i,0}: i=1,2,\ldots,N)$ and $(\alpha_{i,L}, \beta_{i,L}: i=1,2,\ldots,N)$ represent the parameters of the systems obtained respectively using the front and back surface echos from a suitable sample as reference signals. The system model parameters at