The Statistical Sleuth in R: Chapter 11

Kate Aloisio Ruobing Zhang Nicholas J. Horton*

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1 Introduction

This document is intended to help describe how to undertake analyses introduced as examples in the Second Edition of the *Statistical Sleuth* (2002) by Fred Ramsey and Dan Schafer. More information about the book can be found at http://www.proaxis.com/~panorama/home.htm. This file as well as the associated knitr reproducible analysis source file can be found at http://www.math.smith.edu/~nhorton/sleuth.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignette (http://cran.r-project.org/web/packages/mosaic/vignettes/MinimalR.pdf).

To use a package within R, it must be installed (one time), and loaded (each session). The package can be installed using the following command:

^{*}Department of Mathematics and Statistics, Smith College, nhorton@smith.edu

```
> install.packages("mosaic") # note the quotation marks
```

Once this is installed, it can be loaded by running the command:

```
> require(mosaic)
```

This needs to be done once per session.

In addition the data files for the *Sleuth* case studies can be accessed by installing the **Sleuth2** package.

```
> install.packages("Sleuth2")  # note the quotation marks
```

```
> require(Sleuth2)
```

We also set some options to improve legibility of graphs and output.

```
> trellis.par.set(theme = col.mosaic()) # get a better color scheme for lattice
> options(digits = 3, show.signif.stars = FALSE)
```

The specific goal of this document is to demonstrate how to calculate the quantities described in Chapter 11: Model Checking and Refinement using R.

2 Alcohol metabolism in men and women

How do men and women metabolise alcohol? This is the question addressed in case study 11.1 in the *Sleuth*.

2.1 Data coding, summary statistics and graphical display

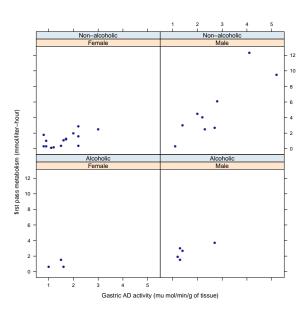
We begin by reading the data and summarizing the variables.

```
> summary(case1101)
   Subject
                 Metabol
                                Gastric
                                               Sex
Min. : 1.0
              Min. : 0.10
                                    :0.80
                                           Female:18
                             Min.
1st Qu.: 8.8
              1st Qu.: 0.60
                             1st Qu.:1.20
                                           Male :14
Median:16.5
              Median: 1.70 Median: 1.60
                   : 2.42
Mean
     :16.5
              Mean
                             Mean
                                  :1.86
              3rd Qu.: 2.93
3rd Qu.:24.2
                             3rd Qu.:2.20
              Max. :12.30
Max. :32.0
                             Max. :5.20
         Alcohol
Alcoholic : 8
Non-alcoholic:24
```

A total of 32 volunteers were included in this data. There were 18 females and 14 males. As recorded in Display 9.2 (page 237 of the *Sleuth*).

The following is a graphical display of the variables akin to Display 11.2 (page 306).

```
> xyplot(Metabol ~ Gastric | Sex + Alcohol, data = case1101, auto.key = TRUE,
+ xlab = "Gastric AD activity (mu mol/min/g of tissue)", ylab = "first pass metabolism (mm
```



2.2 Multiple regression

First we can fit a full model for estimating *metabolism* given a subjects *gastric AD activity*, whether they are *alcoholic* and *gender*. This first model is summarized on page 315 (Display 11.9).

```
> lm1 = lm(Metabol ~ Gastric + Sex + Alcohol + Gastric * Sex + Sex * Alcohol +
      Gastric * Alcohol + Gastric * Sex * Alcohol, data = case1101)
> summary(lm1)
Call:
lm(formula = Metabol ~ Gastric + Sex + Alcohol + Gastric * Sex +
    Sex * Alcohol + Gastric * Alcohol + Gastric * Sex * Alcohol,
    data = case1101)
Residuals:
  Min
           1Q Median
                         3Q
                               Max
-2.429 -0.619 -0.047 0.515 3.652
Coefficients:
                                      Estimate Std. Error t value Pr(>|t|)
(Intercept)
                                         0.106
                                                    3.839
                                                             0.03
                                                                      0.98
```

Gastric	0.581	2.759	0.21	0.84				
SexMale	0.786	4.187	0.19	0.85				
AlcoholNon-alcoholic	-0.300	3.939	-0.08	0.94				
Gastric:SexMale	0.475	2.933	0.16	0.87				
SexMale:AlcoholNon-alcoholic	-2.252	4.394	-0.51	0.61				
Gastric:AlcoholNon-alcoholic	0.260	2.807	0.09	0.93				
<pre>Gastric:SexMale:AlcoholNon-alcoholic</pre>	1.199	2.998	0.40	0.69				
Residual standard error: 1.25 on 24 degrees of freedom Multiple R-squared: 0.828, Adjusted R-squared: 0.777 F-statistic: 16.5 on 7 and 24 DF, p-value: 9.35e-08								

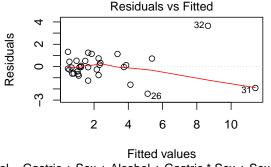
Next we can calculate a number of model diagnostics, including leverage, studentized resids and Cook's distance (pages 319–320).

> require(MASS)

```
> case1101$hat = hatvalues(lm1)
> case1101$studres = studres(lm1)
> case1101$cooks = cooks.distance(lm1)
> case1101[31, ]
   Subject Metabol Gastric Sex
                                      Alcohol
                                                hat studres cooks
                       5.2 Male Non-alcoholic 0.601
               9.5
                                                     -2.72
```

The following is a residual plot for the full model akin to Display 11.7 (page 313).

```
> plot(lm1, which = 1)
```



ol ~ Gastric + Sex + Alcohol + Gastric * Sex + Sex * Alc

From these diagnostics it appears that observations 31 and 32 may be influential points. Therefore, we next re-fit the full model excluding these two observations. The following results are found in Display 11.9 and discussed on page 315.

```
> case11012 = case1101[-c(31, 32), ]
> lm2 = lm(Metabol ~ Gastric + Sex + Alcohol + Gastric * Sex + Sex * Alcohol +
     Gastric * Alcohol + Gastric * Sex * Alcohol, data = case11012)
> summary(lm2)
Call:
lm(formula = Metabol ~ Gastric + Sex + Alcohol + Gastric * Sex +
    Sex * Alcohol + Gastric * Alcohol + Gastric * Sex * Alcohol,
    data = case11012)
Residuals:
                            3Q
   Min
            1Q Median
                                   Max
-1.8076 -0.5701 -0.0466 0.4976 1.4002
Coefficients:
                                    Estimate Std. Error t value Pr(>|t|)
                                                 2.881
                                                          0.04
(Intercept)
                                       0.106
                                                                    0.97
                                                 2.070
                                                           0.28
Gastric
                                       0.581
                                                                    0.78
SexMale
                                       0.786
                                                 3.141
                                                          0.25
                                                                  0.80
                                      -0.300
AlcoholNon-alcoholic
                                                  2.956 -0.10
                                                                    0.92
Gastric:SexMale
                                       0.475
                                                  2.201
                                                          0.22
                                                                    0.83
SexMale: AlcoholNon-alcoholic
                                      -1.272
                                                  3.467
                                                          -0.37
                                                                    0.72
Gastric:AlcoholNon-alcoholic
                                       0.260
                                                  2.106
                                                          0.12
                                                                    0.90
Gastric:SexMale:AlcoholNon-alcoholic
                                       0.606
                                                  2.316
                                                           0.26
                                                                    0.80
Residual standard error: 0.941 on 22 degrees of freedom
Multiple R-squared: 0.685, Adjusted R-squared: 0.585
F-statistic: 6.83 on 7 and 22 DF, p-value: 0.000226
```

2.3 Refining the Model

This section addresses the process of refining the model. We first tested the lack of fit for the removal of Alcohol as shown in Display 11.13 (page 322).

```
> lm3 = lm(Metabol ~ Gastric + Sex + Gastric * Sex, data = case11012)
> summary(lm3)

Call:
lm(formula = Metabol ~ Gastric + Sex + Gastric * Sex, data = case11012)

Residuals:
    Min    1Q Median    3Q    Max
```

```
-1.5962 -0.6025 -0.0408 0.4759 1.6473
Coefficients:
               Estimate Std. Error t value Pr(>|t|)
(Intercept)
                -0.197
                             0.586 -0.34
                                             0.739
                                     2.37
Gastric
                  0.837
                             0.353
                                             0.026
SexMale
                  0.267
                             0.993
                                     0.27
                                             0.790
Gastric:SexMale
                  0.728
                             0.539
                                     1.35
                                             0.188
Residual standard error: 0.882 on 26 degrees of freedom
Multiple R-squared: 0.673, Adjusted R-squared: 0.635
F-statistic: 17.8 on 3 and 26 DF, p-value: 1.71e-06
> anova(lm3, lm2) # page 322
Analysis of Variance Table
Model 1: Metabol ~ Gastric + Sex + Gastric * Sex
Model 2: Metabol ~ Gastric + Sex + Alcohol + Gastric * Sex + Sex * Alcohol +
   Gastric * Alcohol + Gastric * Sex * Alcohol
 Res.Df RSS Df Sum of Sq F Pr(>F)
     26 20.2
2 22 19.5 4
                     0.74 0.21 0.93
```

Next we assessed a model without an intercept which is scientifically plausible as summarized in Display 11.14 (page 323).

```
> lm4 = lm(Metabol ~ Gastric + Gastric:Sex - 1, data = case11012)
> summary(lm4)
Call:
lm(formula = Metabol ~ Gastric + Gastric:Sex - 1, data = case11012)
Residuals:
    Min
             1Q Median
                             3Q
                                    Max
-1.6171 -0.6075 -0.0262 0.4772 1.6230
Coefficients: (1 not defined because of singularities)
                  Estimate Std. Error t value Pr(>|t|)
Gastric
                     1.599
                                0.125
                                        12.80 3.2e-13
Gastric:SexFemale -0.873
                                0.174
                                        -5.02 2.6e-05
Gastric:SexMale
                        NA
                                   NA
                                           NA
Residual standard error: 0.852 on 28 degrees of freedom
```

```
Multiple R-squared: 0.877, Adjusted R-squared: 0.868
F-statistic: 99.9 on 2 and 28 DF, p-value: 1.8e-13

> anova(lm4, lm3)

Analysis of Variance Table

Model 1: Metabol ~ Gastric + Gastric:Sex - 1

Model 2: Metabol ~ Gastric + Sex + Gastric * Sex

Res.Df RSS Df Sum of Sq F Pr(>F)

1 28 20.3
2 26 20.2 2 0.094 0.06 0.94
```

Note that the "Summary of Statistical Findings" section (page 306) is based on this final model.

3 Blood brain barrier

Neuroscientists working to better understand the blood brain barrier have infused rats with cells to induce brain tumors. This is the topic addressed in case study 11.2 in the *Sleuth*.

3.1 Data coding and summary statistics

We begin by reading the data, performing transformations where needed and summarizing the variables.

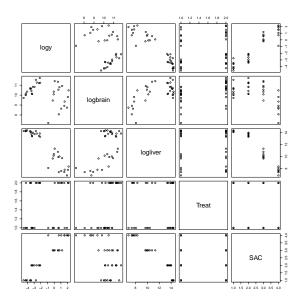
```
> case1102$Y = with(case1102, Brain/Liver)
> case1102$logliver = with(case1102, log(Liver))
> case1102$logbrain = with(case1102, log(Brain))
> case1102$SAC = as.factor(case1102$Time)
> case1102$logy = with(case1102, log(Brain/Liver))
> case1102$logtime = with(case1102, log(Time))
> case1102$Treat = relevel(case1102$Treat, ref = "NS")
> summary(case1102)
                                       Time
                                                 Treat
    Brain
                     Liver
                                                             Days
 Min. : 1334
                 Min. :
                             928
                                  Min. : 0.5
                                                 NS:17
                                                         Min. : 9
 1st Qu.: 19281 1st Qu.: 16210
                                  1st Qu.: 1.1
                                                 BD:17
                                                         1st Qu.:10
Median: 32572 Median: 643965
                                  Median: 3.0
                                                         Median:10
Mean : 39965
               Mean : 668776
                                  Mean
                                        :23.5
                                                         Mean :10
 3rd Qu.: 50654
                 3rd Qu.:1318557
                                  3rd Qu.:24.0
                                                         3rd Qu.:10
Max. :123730 Max.
                                  Max. :72.0
                       :1790863
                                                         Max.
                                                                :11
 Sex
           Weight
                          Loss
                                        Tumor
                                                        Y
 F:26 Min. :184
                            :-4.90 Min. : 25
                                                  Min.
                                                         :0.01
                     Min.
 M: 8
      1st Qu.:225
                     1st Qu.: 1.20
                                    1st Qu.:136
                                                  1st Qu.:0.03
       Median :240
                    Median: 3.95
                                  Median:166 Median:0.12
```

```
: 3.64
       Mean
              :242
                     Mean
                                     Mean
                                             :183
                                                    Mean
                                                           :1.50
       3rd Qu.:259
                     3rd Qu.: 5.97
                                      3rd Qu.:223
                                                    3rd Qu.:1.95
              :298
                            :12.80
                                             :484
                                                           :8.55
       Max.
                     Max.
                                     Max.
                                                    Max.
   logliver
                   logbrain
                                 SAC
                                              logy
                                                            logtime
Min.
       : 6.83
                Min.
                       : 7.20
                                 0.5:9
                                                :-4.58
                                                         Min.
                                                                :-0.69
                                         Min.
1st Qu.: 9.69
                1st Qu.: 9.86
                                3 :9
                                         1st Qu.:-3.39
                                                         1st Qu.:-0.25
                Median :10.39
                                         Median :-2.13
Median :13.37
                                24:8
                                                         Median: 1.10
Mean
       :11.61
                Mean
                       :10.23
                                72:8
                                         Mean
                                                :-1.39
                                                         Mean
                                                                : 1.86
3rd Qu.:14.09
                3rd Qu.:10.83
                                         3rd Qu.: 0.67
                                                         3rd Qu.: 3.18
Max. :14.40
                Max. :11.73
                                         Max. : 2.15
                                                         Max. : 4.28
```

A total of 34 rats were included in this experiment. Each rat was given either the barrier solution (n = 17) or a normal saline solution (n = 17). Then variables of interest were calculated and are displayed in Display 9.2 (page 237 of the *Sleuth*).

We can graphically relationships between the variables using a pairs plot.

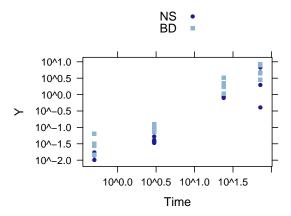
```
> smallds = case1102[, c("logy", "logbrain", "logliver", "Treat", "SAC")]
> pairs(smallds)
```



3.2 Graphical presentation

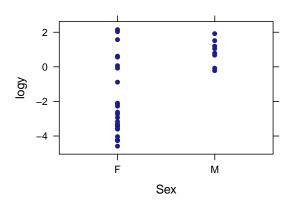
The following displays a scatterplot of log ratio (Y) as a function of log time, akin to Display 11.5 on page 309.

```
> xyplot(Y ~ Time, group = Treat, scales = list(y = list(log = TRUE), x = list(log = TRUE)),
+ auto.key = TRUE, data = case1102)
```

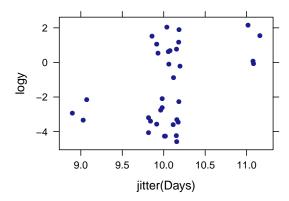


The following graphs are akin to the second and third plots in Display 11.16 on page 326.

> xyplot(logy ~ Sex, data = case1102)



> xyplot(logy ~ jitter(Days), data = case1102)



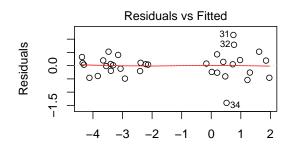
3.3 Multiple regression

We first fit a model that reflects the initial investigation. This is the proposed model from page 311.

```
> lm1 = lm(logy ~ SAC + Treat + SAC * Treat + Days + Sex + Weight + Loss + Tumor,
     data = case1102)
> summary(lm1)
Call:
lm(formula = logy ~ SAC + Treat + SAC * Treat + Days + Sex +
   Weight + Loss + Tumor, data = case1102)
Residuals:
   Min
                           3Q
            1Q Median
                                 Max
-1.4056 -0.2559 0.0458 0.1957 1.1583
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -3.836741 3.391046 -1.13
                                           0.271
SAC3
             1.015463 0.399578
                                 2.54
                                           0.019
SAC24
             4.337135 0.477836
                                 9.08 1.0e-08
SAC72
            5.010605
                      0.454953
                                 11.01 3.5e-10
                                 2.10
TreatBD
            0.795999 0.378970
                                        0.048
            -0.036987 0.295645
Days
                                  -0.13
                                           0.902
            0.001295 0.373368
                                 0.00
SexM
                                        0.997
Weight
            -0.000558 0.005330
                                 -0.10
                                        0.918
            -0.059544 0.030422
                                 -1.96 0.064
Loss
Tumor
            0.001551 0.001226
                                 1.26
                                           0.220
SAC3:TreatBD 0.179831 0.551964
                                   0.33
                                           0.748
SAC24:TreatBD -0.386047 0.585450 -0.66
                                           0.517
SAC72:TreatBD 0.379104
                        0.569242
                                   0.67
                                           0.513
Residual standard error: 0.564 on 21 degrees of freedom
Multiple R-squared: 0.96, Adjusted R-squared: 0.937
F-statistic: 41.9 on 12 and 21 DF, p-value: 6.45e-12
```

We can then display a residual plot to assess the fit of the above model. This is provided in Display 11.6 (page 312).

```
> plot(lm1, which = 1)
```



Fitted values
- SAC + Treat + SAC * Treat + Days + Sex + Weight + I

3.4 Refining the model

Lastly, we fit a refined model. These results can be found in Display 11.17 (page 327).

```
> lm2 = lm(logy ~ SAC + Treat, data = case1102)
> summary(lm2)
Call:
lm(formula = logy ~ SAC + Treat, data = case1102)
Residuals:
    Min
             1Q Median
                             3Q
                                    Max
-1.7402 -0.1755 -0.0178 0.2477 1.0551
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
              -4.302
                          0.205 -21.01 < 2e-16
(Intercept)
SAC3
               1.134
                          0.252
                                   4.50 0.00010
SAC24
               4.257
                          0.259
                                  16.43 3.1e-16
SAC72
               5.154
                          0.259
                                  19.89
                                        < 2e-16
TreatBD
               0.797
                          0.183
                                   4.35 0.00016
Residual standard error: 0.533 on 29 degrees of freedom
Multiple R-squared: 0.951, Adjusted R-squared: 0.944
F-statistic: 140 on 4 and 29 DF, p-value: <2e-16
> anova(lm2, lm1)
Analysis of Variance Table
Model 1: logy ~ SAC + Treat
```

```
Model 2: logy ~ SAC + Treat + SAC * Treat + Days + Sex + Weight + Loss + Tumor

Res.Df RSS Df Sum of Sq F Pr(>F)

1 29 8.23
2 21 6.68 8 1.55 0.61 0.76
```