

EDS 241: Assignment 1

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1 Introduction

This assignment uses data from CalEnviroScreen 4.0, a mapping and data tool produced by the California Office of Environmental Health Hazards Assessment (OEHHA). The data are compiled and constructed from a variety of sources and cover all 8,035 census tracts in California.

Specifically, I used the following variables:

- census tract ID,
- total population,
- California county name (the county where the census tract is located),
- Low Birth Weight (% of census tract births with weight < 2500g),
- PM25 (ambient concentrations of PM2.5 in the census tract, in $\mu\text{g}/\text{m}^3$),
- and Poverty (% of population in the census tract living below twice the federal poverty line).

2 Read in and clean data

Select variables of interest

```
data <- read_csv(here("data", "CES4.csv"))

data_clean <- data %>%
  clean_names()

data_clean <- data_clean %>%
  select(census_tract,
         california_county,
         total_population,
         low_birth_weight,
         pm2_5,
         poverty)
```

3 (a) What is the average concentration of PM2.5 across all census tracts in California?

```
mean_pm2.5 <- mean(data_clean$pm2_5) %>%
  round(digits = 2)
```

The mean concentration of PM2.5 across all census tracts in California is 10.15 $\mu\text{g}/\text{m}^3$.

4 (b) What county has the highest level of poverty in California?

Drop counties with NA values for poverty

```
data_pov <- data_clean %>%
  drop_na(poverty)

max_pov_county <- subset(data_pov, poverty == max(data_pov$poverty))
max_pov_county <- max_pov_county$california_county
```

Ventura is the county with the highest level of poverty in California.

5 (c) Make a histogram depicting the distribution of percent low birth weight and PM2.5

```
pm_lab <- expression(paste("PM2.5 (\mu\text{g}/\text{m}^3,"))"

p1 <- ggplot(data = data_clean) +
  geom_histogram(aes(x = low_birth_weight),
                 binwidth = 0.25) +
  theme_classic() +
  labs(y = "Frequency",
       x = "% of Low Birth Weights")

p2 <- ggplot(data = data_clean) +
  geom_histogram(aes(x = pm2_5),
                 binwidth = 0.5) +
  theme_classic() +
  labs(y = "Frequency",
       x = pm_lab)
```

Figure 1: Distributions of low birth weights and PM2.5 in California census tracts

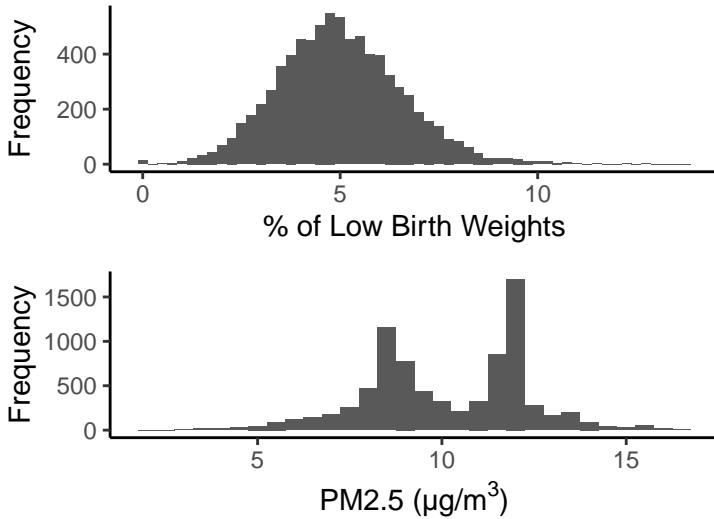


Figure 1 shows the distributions of % birth weights < 2500g and ambient concentrations of PM2.5 ($\mu\text{g}/\text{m}^3$) per census tract. Low birth weight data are approximately normally distributed while PM2.5 data is bimodal. Data is sourced from CalEnviroScreen 4.0.

6 (d) Estimate a OLS regression of LowBirthWeight on PM25. Report the estimated slope coefficient and its heteroskedasticity-robust standard error. Interpret the estimated slope coefficient. Is the effect of PM25 on LowBirthWeight statistically significant at the 5%?

To analyze the relationship between Low Birth Weight and PM2.5, we estimate the following regression:

$$Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + u_i \quad (1)$$

where Y_i is Low Birth Weight for vehicle model i , X_{1i} is PM2.5 concentrations, X_{2i} is Poverty, and u_i the regression error term. We will consider a regression including only PM2.5, and a regression including PM2.5 and Poverty.

```
mdl <- lm_robust(low_birth_weight ~ pm2_5, data=data_clean) %>%
  broom::tidy()
```

The estimated slope coefficient for PM2.5 (β_1) = 0.1179305, meaning that a $1 \mu\text{g}/\text{m}^3$ change in PM2.5 on average increases the low birth rate by 0.1179305. At the 5% significance level, the effect of PM2.5 on low birth rate is statistically significant because the p-value < 0.05. The standard error for PM2.5 (β_1) = 0.0885829, 0.0084024.

7 (e) Suppose a new air quality policy is expected to reduce PM2.5 concentration by $2 \mu\text{g}/\text{m}^3$. Predict the new average value of LowBirthWeight and derive its 95% confidence interval. Interpret the 95% confidence interval.

```
int = mdl$estimate[1]
b1 = mdl$estimate[2]
x = -2
y = mdl$estimate[1] + mdl$estimate[2] * x
```

Given the equation: $\text{PM2.5} = 3.8009877 + 0.1179305 * \text{LowBirthWeight}$, if PM2.5 is reduced by 2, then we predict the Low Birth Rate to be approximately 3.5651266%.

The 95% confidence interval is bounded by 0.1344015 and , meaning we are 95% confident that the true parameter β_1 lies within this interval.

8 (f) Add the variable Poverty as an explanatory variable to the regression in (d). Interpret the estimated coefficient on Poverty. What happens to the estimated coefficient on PM25, compared to the regression in (d). Explain.

```
mdl12 <- lm_robust(low_birth_weight ~ pm2_5 + poverty, data=data_clean) %>%
  broom::tidy()
```

The estimated slope coefficient for Poverty (β_2) = 0.0274353, meaning that a 1% change in Poverty on average increases Low Birth Rate by 0.0274353. Compared to the prior model, the slope coefficient of PM2.5 (β_1) has decreased from 0.1179305 to 0.0591077 because Poverty helps explain some of the change in Low Birth Weight. In other words, the prior model suffered from omitted variables bias and caused us to overestimate the impact of PM2.5 alone on Low Birth Weight.

Table 1 shows the estimated coefficients from estimating equation (1).

Table 1: PM2.5 and Poverty associate with Low Birth Rate in California census tracts

Statistic	N	Mean	St. Dev.	Min	Pctl(25)	Pctl(75)	Max
PM2.5	2	1.959	2.604	0.118	1.039	2.880	3.801
Poverty	2	0.048	0.057	0.008	0.028	0.069	0.089
statistic	2	28.472	20.417	14.035	21.254	35.690	42.909
p.value	2	0.000	0.000	0	0	0	0
conf.low	2	1.864	2.493	0.101	0.983	2.746	3.627
conf.high	2	2.055	2.715	0.134	1.094	3.015	3.975
df	2	7,806.000	0.000	7,806	7,806	7,806	7,806

Table 2: PM2.5 and Poverty associate with Low Birth Rate in California census tracts

Statistic	N	Mean	St. Dev.	Min	Pctl(25)	Pctl(75)	Max
PM2.5	3	1.210	2.021	0.027	0.043	1.801	3.544
Poverty	3	0.031	0.046	0.001	0.005	0.047	0.085
statistic	3	25.441	17.428	7.127	17.251	34.598	41.823
p.value	3	0.000	0.000	0	0	0	0
conf.low	3	1.149	1.930	0.025	0.034	1.710	3.378
conf.high	3	1.272	2.112	0.029	0.052	1.893	3.710
df	3	7,802.000	0.000	7,802	7,802	7,802	7,802

9 (g) From the regression in (f), test the null hypothesis that the effect of PM2.5 is equal to the effect of Poverty

$H_0: \text{PM2.5} = \text{Poverty}$

$H_A: \text{PM2.5} \neq \text{Poverty}$

```
# mdl3 <- linearHypothesis(model = mdl2,
#                           hypothesis.matrix = c("pm2_5 - poverty = 0"),
#                           white.adjust = "hc2")
#
# p <- mdl3$`Pr(>F)`[2]
```