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#### Research paper

## Optical modeling, solver, and design of macroscopic single-enantiomer carbon nanotube film and reconfigurable chiral photonic device

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#### ABSTRACT

The interaction of circularly polarized light with chiral matter and functional devices enables novel phenomena and applications. Recently, macroscopic solid-state single-enantiomer carbon nanotube (CNT) films have become feasible and are emerging as a chiral photonic material platform thanks to their quantum-confinement-induced optical properties and facile scalable assembly. However, optical modeling, solver, and device design tools for such materials are non-existent. Here, we prepare macroscopic single-enantiomer (6,5) and (11,-5) randomly oriented CNT films and create an optical material model based on measured experimental optical spectra. We also implement a highly-parallel graphic-processing-unit accelerated transfer matrix solver for general bi-anisotropic materials and layered structures. Further, we demonstrate reconfigurable chiral photonic devices in a heterostructure with phase change materials through machine learning-enabled efficient gradient-based inverse design and optimization. Our developed full stack of a chiral photonic material and device hardware platform and a corresponding high-performance differential-programming-enabled solver opens the door for future chiral photonic devices and applications based on single-enantiomer CNT films.

#### 1. Introduction

Manipulating the interaction of circularly polarized light with chiral materials and their functional photonic devices is crucial for many applications, such as sensing [1,2], imaging [3,4], computing [5], and quantum technologies [6]. The advancement of developing such devices is nowadays hindered not only by the limited number of highperformance material platforms but also by efficient solvers and design tools. In current material platforms, small natural chiral molecules generally have weak chiroptical responses because of a large mismatch between molecule size and optical wavelength. Chiral organic supramolecular structures [7,8] and twisted structures of anisotropic materials [9] manufactured through cost-effective bottom-up selfassembly techniques can produce strong chiroptical responses, while individual constituents lack quantum-confinement-induced extraordinary properties and the design of structures is largely empirical. Artificial symmetry-breaking periodic structures can provide an engineerable platform with systematic electromagnetic design tools, such as finite difference time domain analysis, while their top-down manufacturing is sophisticated and challenging to scale up [10] and those design tools are generally computationally intensive and time-consuming [11].

Carbon nanotubes (CNTs) resurge as a promising chiral photonic material platform in the form of both natural and synthetic chirality thanks to the recent progress in large-scale chirality and enantiomer separation and bottom-up macroscopic ordered self-assembly techniques [12-21]. The optical properties of CNTs are determined by their one-dimensional (1D) atomic structures [22]. The quantum confinement in 1D nanoscale tubular geometry of CNTs leads to the formation of subbands and the interband transitions between subbands produce strong exciton-dominant optical spectral features. The transition energies can be tuned by the quantum engineering of CNT atomic structures, which are typically described by a pair of chirality indices (n, m), and by external stimuli such as electric fields and optical excitation. Except for special highly symmetric zigzag (n,0)and armchair (n, n) CNTs, all other CNTs are chiral and contain two enantiomers, denoted as (n, m) and (n + m, -m), with different chiral photonic responses. For example, as illustrated in Fig. 1, the interaction of (6,5) and (11,-5) CNTs of opposite handednesses with left circularly polarized (LCP) and right circularly polarized (RCP) light, such as circular dichroism (CD) that is the differential absorption of LCP and

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Fig. 1. Overview. Illustrations of the interaction of circularly polarized light with single-enantiomer CNT films and their excitonic chiral photonic responses. Schematics of CNTs were produced using VESTA [23].

RCP light, is distinctly different. Hence, their assembled macroscopic films become a solid-state material platform for building novel chiral photonic devices; see Fig. 1. However, to date, there is no demonstration of any optical modeling or solvers for such materials, hindering device design capability.

Here, we present an optical material model and a highly-parallel fast solver for macroscopic single-enantiomer (6,5) and (11,-5) randomly oriented CNT films, and demonstrate reconfigurable chiral photonic devices in a heterostructure with phase change materials (PCMs) through machine learning (ML)-enabled efficient gradient-based inverse design and optimization. Specifically, we prepared single-enantiomer (6,5) and (11,-5) suspensions through gel chromatography and macroscopic randomly oriented films through vacuum filtration, and experimentally measured CD and absorption spectra of suspension and solid-state samples. We created material models for (6,5) and (11,-5) films and implemented a graphic-processing-unit (GPU) accelerated transfer matrix solver for general bi-anisotropic materials and layered architectures based on a state-of-the-art ML framework. By simultaneously fitting experimental spectra, we extracted dielectric functions and chirality parameters for (6,5) and (11,-5) films. Furthermore, we leveraged the backpropagation algorithm in the ML framework to design a novel reconfigurable chiral photonic device based on a heterostructure consisting of single-enantiomer CNT films and PCM films. Our developed full stack of a chiral photonic material and device hardware platform and a corresponding GPU-accelerated and differential-programmingenabled solver opens the door for future chiral photonic devices and applications based on single-enantiomer CNT films.

#### 2. Experimental section

#### 2.1. Preparation of single-enantiomer CNT suspensions

We purchased CoMoCAT CNT powders and mixed them with a combination of surfactants. The mixture was tip-sonicated to disperse CNTs to form a homogenized aqueous suspension. The suspension was then purified through ultracentrifugation to remove undispersed impurities, such as catalysts and large bundles. The supernatant was collected for enantiomer separation, which was performed through an automatic temperature-controlled chromatography system for largescale separation following the procedures described in Ref. [14,15,24]. By controlling the composition and concentration of surfactant elution solutions, CNTs of different diameters and handednesses were collected at various times during the process; see more details in Supporting Information Note 1. Fig. 2a displays a photograph of a prepared single-enantiomer suspension. During the separation process, we characterized the quality of suspensions by measuring their absorption spectra using an ultraviolet-visible-near infrared (UV-Vis-NIR) spectrometer (Shimadzu UV-3600 UV-Vis-NIR Spectrophotometer) in a wavelength range from 200 to 1200 nm. Fig. S1 displays a normalized

absorption spectrum of a separated (11,–5) suspension (red line). The spectrum was normalized with respect to the  $E_{11}$  peak. By repeating the enantiomer separation process multiple times, we collected enough CNT suspensions for preparing macroscopic films.

#### 2.2. Preparation of single-enantiomer CNT films

We produced macroscopic (e.g.,  $5 \times 5 \text{ mm}^2$ ) single-enantiomer (6,5) and (11,-5) CNT films using vacuum filtration. Briefly, we exchanged the mixed surfactant system in separated single-enantiomer suspensions to a single sodium deoxycholate (DOC) surfactant system before pouring it into the filtration system. The DOC concentration was kept higher than its critical micelle concentration and a fast filtration was performed to produce randomly oriented films instead of highly aligned ones [18]. When all suspensions finished filtration, the deposited films were kept on the filtration system for a complete dry. The obtained films on the filter membrane can be transferred onto arbitrary substrates following a wet transfer process [18]; see more details in Supporting Information Note 2. For optical characterization, we transferred films onto silica substrates, which have broadband optical transparency from ultraviolet to near-infrared wavelength ranges. Fig. 2b shows a photo of a produced film. Due to the self-limiting nature of the vacuum filtration process [25,26], the film thickness was uniform and can be controlled by adjusting the suspension concentration and volume. The film lateral size will be potentially scalable to be wafer-scale using large-scale filtration systems.

#### 2.3. Film thickness measurement and morphological characterization

We measured the thicknesses of obtained films through atomic force microscopy (Bruker Multimode 8 AFM). Fig. S2a displays a representative AFM image of one CNT film. The film thickness was measured by creating a section profile that crossed a crack in the film, leading to a relatively smooth edge. In contrast, multiple bumps formed around the physical edge of the film because the film was cut into certain shapes manually. Fig. S2b shows the height profile of the film with a thickness of  $\sim 60$  nm. Further, we characterized the surface morphology of obtained films using scanning electron microscopy (FEI Teneo SEM). Fig. S3 shows SEM images of one prepared single-enantiomer CNT film at two different positions. Some areas showed randomly oriented structures (Position 1) while other areas displayed the formation of local, microscopic, oriented structures (Position 2).

#### 2.4. Characterization of optical linear anisotropy

We verified the optical linear anisotropy of obtained films by measuring linear-polarization-dependent optical attenuation. We used a laser at a wavelength of 635 nm (Thorlabs, CPS635R) incident on obtained films. The circular beam size was  $\sim 2$  mm in diameter to probe

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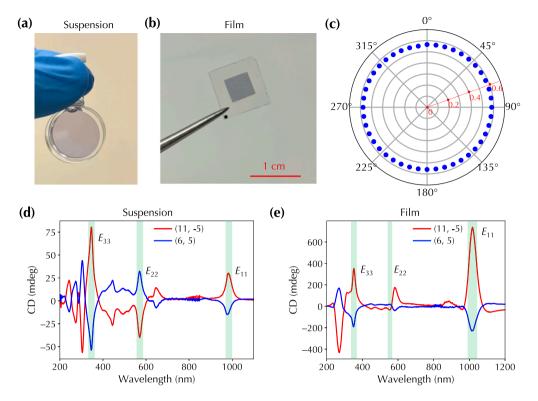


Fig. 2. Experimental results. Photos of (a) separated single-enantiomer suspensions and (b) macroscopic films. (c) Polar plot of polarization-dependent transmission of one obtained film. CD spectra of single-enantiomer (6,5) and (11,-5) (d) suspensions and (e) macroscopic films. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the degree of alignment in a large area. The linear polarization state of the laser was rotated through a half-waveplate (Thorlabs, WPH10ME-633). The transmitted optical power was measured by a photodiode (Thorlabs, PM16-130). The transmitted optical power of both CNT samples and a bare reference substrate was measured and the ratio was calculated as transmittance. Fig. 2c shows a polar plot of measured transmittance at various polarization angles and there was no clear angle dependence, confirming that obtained films were macroscopically randomly oriented.

#### 2.5. CD spectra measurement and enantiomeric purity

We measured the CD and absorption spectra of separated singleenantiomer suspensions and macroscopic films using a Jasco CD J-1500 spectrometer under normal incidence. The circular probe beam size was ~2 mm in diameter. The absorption spectra measured from the CD spectrometer are expressed as  $(A_L + A_R)/2$ , where  $A_L$  and  $A_R$  are the absorption spectra when the incident light is LCP and RCP, respectively. These spectra are equivalent to the absorption spectra measured from commercial UV-Vis-NIR spectrometers because the incident light in UV-Vis-NIR spectrometers is unpolarized and can be treated as a combination of equal amount of LCP and RCP light. Fig. S1 shows two normalized absorption spectra of two similarly separated (11,-5) suspensions measured using UV-Vis-NIR and CD spectrometers, respectively. Both spectra were normalized with respect to their  $E_{11}$  peaks and were nearly identical. The g factor was calculated as the ratio between CD and average absorption, which was measured from the CD spectrometer and expressed as  $(A_L + A_R)/2$ . Fig. 2d shows the measured CD spectra of single-enantiomer (6,5) and (11,-5) suspensions in a wavelength range from 200 to 1200 nm. The excitonic interband transitions with the same band indices for valance and conduction bands, such as  $E_{11}$ ,  $E_{22}$ , and  $E_{33}$ , correspond to the CD spectral features in green shaded rectangles of Fig. 2d with alternating signs [13-15,27].

Other peaks are mainly from cross-polarized excitons [14]. Fig. S4a and S4b show the corresponding absorption and g factor spectra. Based on the ratio of CD and absorption peaks at the  $E_{22}$  location, denoted as  $CD_{norm}$ , we estimated enantiomeric purities (EPs) for (6,5) and (11,–5) suspensions following two linear regression fitting curves, EP(6,5) (%) =  $50 + \alpha CD_{norm}$  and EP(11,-5) (%) =  $50 - \alpha CD_{norm}$ , where  $\alpha = 0.421 \, \text{mdeg}^{-1}$  [14]. Hence, the calculated EPs for (6,5) and (11,–5) suspensions were nearly the same  $\sim 87\%$ .

Further, we measured the CD and absorption spectra of macroscopic single-enantiomer (6,5) and (11,-5) randomly oriented films. In contrast to suspension measurements, the CD measurements of solid-state samples require special treatment to eliminate instrumentation artifacts. We adopted a "four-configuration" approach, where CD spectra were captured under four different sample configurations as shown in Fig. S5a, and thus the averaged CD spectra removed artifacts and provided the genuine CD response from samples [20]; see Supporting Information Note 3, Fig. S5b, and Fig. S5c for more details. Fig. 2e, Fig. S6a, Fig. S6b display the measured CD, absorption, and g factor spectra of single-enantiomer (6,5) and (11,-5) random films in a wavelength range from 200 to 1200 nm, respectively. The assignment of excitonic transitions in the film CD spectra (green shaded rectangles in Fig. 2e) also followed the rule of alternating signs. Compared to suspension CD and absorption spectra, as expected, the excitonic peaks in films become broadened due to CNT bundling. Interestingly, the relative heights of  $E_{11}$ ,  $E_{22}$ , and  $E_{33}$  peaks in films are substantially different from those in suspensions, and  $E_{11}$  becomes the strongest in films. Moreover, the peak heights of the same excitonic transitions for two enantiomers are asymmetric, even though the thicknesses of two enantiomer films are nearly the same as evidenced in absorption spectra shown in Fig. S6a and the purities of suspensions are almost identical. Moreover, the degree of the peak height asymmetry is different for different excitonic transitions. For example, the  $E_{11}$  transition shows a three-time difference while the  $E_{33}$  transition shows a two-time

difference.

We attributed these distinctions in CD spectra between suspensions and films to the formation of local, microscopic twisted stack architecture; see the illustration in Fig. S7. Although obtained films were nearly isotropic in a mm<sup>2</sup>-size area characterized using the optical approach, local orientations could form on a microscopic scale (nm<sup>2</sup> to μm<sup>2</sup> size) as evidenced in scanning electron microscopy images shown in Fig. S3, and could form anywhere in the film thickness direction during the vacuum filtration process. Orientation directions could be randomly selected across the thickness, possibly forming the twisted stack architecture. The structure-induced chirality in this architecture can also produce CD responses because of the helical arrangement of 1D CNT excitonic dipoles [20] and the signs of CD response depend on the twist direction. Hence, the observed CD responses of singleenantiomer CNT films have combined contributions from the intrinsic chirality of enantiomers and the structure-induced chirality of microscopic twisted stacks, leading to asymmetric peak heights of the same excitonic transitions in (6,5) and (11,-5) films. If the twisted direction is the same as one enantiomer handedness, these two contributions enhance each other to have a boosted CD signal. In contrast, the twist direction of the same twisted stack is opposite to the handedness of the other enantiomer, these two contributions counteract to have a reduced CD signal. Furthermore, the CD contribution from the twisted stack is mainly dependent on the dielectric function while the CD contribution from enantiomers is mainly from the chirality parameter, as described below. Hence, for the same twisted stack and enantiomer, if the relative strength between the chirality parameter and dielectric function is different, the degree of asymmetry can also be different. Since the film absorption is related to the dielectric function, the g factor can be a good indicator of the relative strength between these two quantities. For example, the g factor in the  $E_{33}$  region is larger than that in the  $E_{11}$ region, suggesting a larger contribution from the enantiomer intrinsic chirality and a smaller contribution from the twisted stack structureinduced chirality in the  $E_{33}$  region than those in the  $E_{11}$  region. Hence, the degree of asymmetry of peak heights in the  $E_{33}$  region appears less than that in the  $E_{11}$  region. It is challenging to eliminate the formation of twist structures during film preparation, but we can combine the contributions of CD signals from chiral atomic structures and twisted stacks and treat them as a phenomenological and effective material parameter for designing optoelectronic devices.

#### 3. Results and discussion

#### 3.1. Transfer matrix and fitting material parameters

On the macroscopic level, randomly oriented single-enantiomer CNT films can be treated as a reciprocal, chiral, bi-anisotropic medium with constitutive relations written as  $\vec{D} = \overline{\bar{\epsilon}} \vec{E} + \overline{\bar{\xi}} \vec{H}$  and  $\vec{B} = \overline{\bar{\zeta}} \vec{E} + \overline{\bar{\mu}} \vec{H}$ , where  $\vec{D}$  is displacement field,  $\vec{E}$  is electric field,  $\vec{H}$  is magnetic field,  $\vec{B}$  is magnetic flux density,  $\epsilon$  is electric permittivity or dielectric function tensor,  $\overline{\mu}$  is magnetic permeability tensor, and  $\overline{\bar{\xi}}$  and  $\overline{\bar{\zeta}}$  are two magnetoelectric tensors describing the coupling between electric and magnetic components in constitutive relations [28]. Further,  $\overline{\bar{\xi}}$  and  $\overline{\bar{\zeta}}$  can be expressed as  $\sqrt{\epsilon_0\mu_0}(\overline{\chi}-j\overline{\bar{\kappa}})$  and  $\sqrt{\epsilon_0\mu_0}(\overline{\chi}+j\overline{\bar{\kappa}})$ , respectively, where  $\overline{\bar{\chi}}$  and  $\overline{\bar{\kappa}}$  are two unitless magnetoelectric tensors. Since our produced single-enantiomer CNT films are reciprocal and chiral,  $\overline{\bar{\chi}}$  is thus diminishing and  $\overline{\bar{\kappa}}$  is specifically called the chirality parameter.

In this work, we focused on the  $E_{11}$  transitions in (6,5) and (11,–5) films because their CD responses are distant from cross-polarized transitions and have little spectral interference from these transitions. We expressed the relative electric permittivity tensor for a CNT film,  $\overline{\bar{\epsilon}}_{\rm CNT}$ , as

$$\overline{\overline{\varepsilon}}_{\text{CNT}} = \begin{bmatrix} \varepsilon_{\text{in}} & 0 & 0 \\ 0 & \varepsilon_{\text{in}} & 0 \\ 0 & 0 & \varepsilon_{\text{out}} \end{bmatrix},$$

where  $\varepsilon_{\rm in}$  and  $\varepsilon_{\rm out}$  are in-plane and out-of-plane dielectric functions.  $\varepsilon_{\rm in}$  is a function of angular frequency  $\omega$  and described using a Lorentz oscillator model as

$$\varepsilon_{\rm in}(\omega) = \varepsilon_{\infty} + \frac{\omega_{\rm p}^2}{\omega_{\rm 0}^2 - \omega^2 - j\omega\Gamma},$$

where  $\epsilon_{\infty}$  is a constant,  $\omega_{\rm p}$  is plasma frequency,  $\omega_{\rm 0}$  is the resonance frequency for  $E_{11}$  transition, and  $\Gamma$  is the corresponding decay rate.  $\epsilon_{\rm out}$  is a constant as  $\sim 3.4$  determined in Ref. [29] since cross-polarization transitions are negligible around the  $E_{11}$  transition. In addition, since materials are non-magnetic,  $\overline{\mu}$  was assumed to be a scalar constant  $\mu_0$ , which is the vacuum magnetic permeability.

Moreover, we assumed  $\overline{\kappa}$  tensor as an isotropic scalar function  $\kappa(\omega)$ . We would like to note that the CD contribution from chiral atomic arrangements in (6,5) and (11,–5) enantiomers should be isotropic while the CD contribution from twisted stacks could possibly be anisotropic between in-plane and out-of-plane components. However, under our current capacity with only normal incidence CD experiments, a close examination of the out-of-plane chirality parameter is not feasible. A carefully crafted custom CD spectrometer with the removal of artifacts and extrinsic effects in solid-state samples will be needed, which is beyond the scope of our current work.

We described  $\kappa(\omega)$  using a Condon model [30]. Since  $E_{11}$  transitions lie far away from other transitions, the Condon model has one dominant resonance and  $\kappa(\omega)$  becomes

$$\kappa(\omega) = \frac{\omega R}{\omega_1^2 - \omega^2 + j\omega \Gamma_1},$$

where R is the rotational strength of transitions,  $\omega_1$  is the resonance frequency for  $E_{11}$  transition, and  $\Gamma_1$  is the corresponding decay rate. Note that  $\omega_1$  is close to but not necessarily identical to  $\omega_0$  in dielectric function expression because there is an observable slight difference of the peaks in experimental CD and absorption spectra as shown before.

We then developed a transfer matrix solver for general bianisotropic materials and their layered architectures [31] to fit CD and absorption spectra to extract  $\varepsilon_{\rm in}(\omega)$  and  $\kappa(\omega)$  as illustrated in the inset panel of Fig. 3a and Fig. S8. In the medium of the incident light, the electric field vector  $\vec{E}(\vec{r})$  and magnetic field vector  $\vec{H}(\vec{r})$  propagating along z axis can be expressed as

$$\vec{E}(\vec{r}) = \vec{e}(z)e^{jq(x\cos\psi + y\sin\psi)},$$
  
$$\vec{H}(\vec{r}) = \vec{h}(z)e^{jq(x\cos\psi + y\sin\psi)}.$$

where  $q=k_0n_1\sin\theta_i$  is complex-valued wavenumber,  $\psi$  is azimuthal angle,  $\theta_i$  is incident angle,  $n_1$  is refractive index of incident light medium,  $\vec{e}(z)$  is the unit vector as  $e_x(z)\hat{x}+e_y(z)\hat{y}+e_z(z)\hat{z}$ , and  $\vec{h}(z)$  is the unit vector as  $h_x(z)\hat{x}+h_y(z)\hat{y}+h_z(z)\hat{z}$ . For z-components, we have  $e_z(z)=v_{zx}^{ee}e_x(z)+v_{zy}^{ee}e_y(z)+v_{zy}^{ee}h_x(z)+v_{zy}^{eh}h_y(z)$  and  $h_z(z)=v_{xx}^{he}e_x(z)+v_{zy}^{he}e_y(z)+v_{zx}^{hh}h_x(z)+v_{zy}^{hh}h_y(z)$  because of the coupled electric and magnetic fields in constitutive relations.

By solving the Maxwell's equations and matching boundary conditions, we have

thous, we have 
$$v_{zx}^{ee} = -\frac{\mu_{zz}\varepsilon_{zx} - \xi_{zz}[\zeta_{zx} + (q/\omega)\sin\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}}, v_{zy}^{ee} = -\frac{\mu_{zz}\varepsilon_{zy} - \xi_{zz}[\zeta_{zy} - (q/\omega)\cos\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}},$$

$$v_{zx}^{eh} = \frac{\xi_{zz}\mu_{zx} - \mu_{zz}[\xi_{zx} - (q/\omega)\sin\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}}, v_{zy}^{eh} = \frac{\xi_{zz}\mu_{zy} - \mu_{zz}[\xi_{zy} + (q/\omega)\cos\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}},$$

$$v_{zx}^{he} = \frac{\zeta_{zz}\varepsilon_{zx} - \varepsilon_{zz}[\zeta_{zx} + (q/\omega)\sin\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}}, v_{zy}^{he} = \frac{\zeta_{zz}\varepsilon_{zy} - \varepsilon_{zz}[\zeta_{zy} - (q/\omega)\cos\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}},$$

$$v_{zx}^{hh} = -\frac{\varepsilon_{zz}\mu_{zx} - \zeta_{zz}[\xi_{zx} - (q/\omega)\sin\psi]}{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}}, v_{zy}^{hh} = -\frac{\varepsilon_{zz}\mu_{zz} - \xi_{zz}\zeta_{zz}}{\varepsilon_{zz} - \xi_{zz}\zeta_{zz}},$$

where  $\varepsilon_{ij}, \mu_{ij}, \xi_{ij}, \zeta_{ij}, i, j \in \{x, y, z\}$  are tensor components of  $\overline{\varepsilon}, \overline{\mu}, \overline{\xi}, \overline{\varepsilon}$  and  $\overline{\zeta}$ , respectively, for materials in each layer. Furthermore, there are  $\mathbf{P_m}$  and  $\mathbf{M_m}$  matrices for mth layer with a thickness  $d_{\mathbf{m}}$ , which are expressed as

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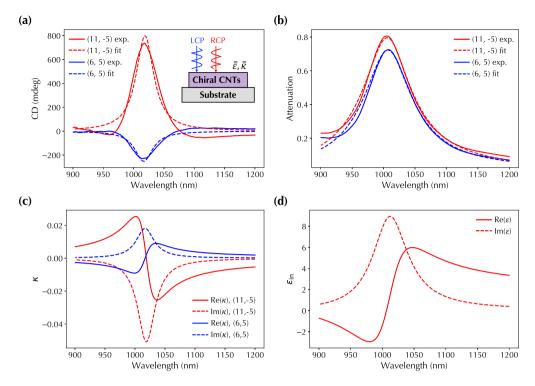


Fig. 3. Transfer matrix fitting. Experimental and fitting (a) CD spectra and (b) absorption spectra of (6,5) and (11,-5) single-enantiomer films. Extracted complex-valued (c) chirality parameters and (d) dielectric functions.

$$\begin{split} \mathbf{P_m} &= \omega \begin{bmatrix} \zeta_{yx} & \zeta_{yy} & \mu_{yx} & \mu_{yy} \\ -\zeta_{xx} & -\zeta_{xy} & -\mu_{xx} & -\mu_{xy} \\ -\varepsilon_{yx} & -\varepsilon_{yy} & -\xi_{yx} & -\zeta_{yy} \\ \varepsilon_{xx} & \varepsilon_{xy} & \zeta_{xx} & \zeta_{xy} \end{bmatrix} + \\ \begin{bmatrix} \zeta_{yz} + \frac{q}{\omega} \cos\psi & 0 & 0 & 0 \\ 0 & -\zeta_{xz} + \frac{q}{\omega} \sin\psi & 0 & 0 \\ 0 & 0 & -\varepsilon_{yz} & 0 \\ 0 & 0 & 0 & \varepsilon_{xz} \end{bmatrix} \cdot \mathbf{J} \cdot \begin{bmatrix} v_{ee}^{ee} & 0 & 0 & 0 \\ 0 & v_{zx}^{ee} & 0 & 0 \\ 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & -\zeta_{yz} + \frac{q}{\omega} \cos\psi & 0 \\ 0 & 0 & 0 & v_{zx}^{eh} & 0 \end{bmatrix} \cdot \mathbf{J} \cdot \begin{bmatrix} v_{ee}^{ee} & 0 & 0 & 0 \\ 0 & v_{zx}^{ee} & 0 & 0 \\ 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} & 0 \\ 0 & 0 & 0 & 0 & 0 & v_{zx}^{eh} &$$

$$\mathbf{M_m} = e^{j\mathbf{P_m}d_{\mathrm{m}}}.$$

There are  $K_{inc}$  and  $K_{tr}$  matrices for the incident and transmission layers with the incident angle  $\theta_{i}$  and output angle  $\theta_{tr}$ , which are expressed as

$$\mathbf{K_{inc}} = \begin{bmatrix} -\sin\psi & -\cos\psi\cos\theta_i & -\sin\psi & \cos\psi\cos\theta_i \\ \cos\psi & -\sin\psi\cos\theta_i & \cos\psi & \sin\psi\cos\theta_i \\ -\left(\frac{n_1}{\eta_0}\right)\cos\psi\cos\theta_i & \left(\frac{n_1}{\eta_0}\right)\sin\psi & \left(\frac{n_1}{\eta_0}\right)\cos\psi\cos\theta_i & \left(\frac{n_1}{\eta_0}\right)\sin\psi \\ -\left(\frac{n_1}{\eta_0}\right)\sin\psi\cos\theta_i & -\left(\frac{n_1}{\eta_0}\right)\cos\psi & \left(\frac{n_1}{\eta_0}\right)\sin\psi\cos\theta_i & -\left(\frac{n_1}{\eta_0}\right)\cos\psi \end{bmatrix}$$

and

$$\mathbf{K_{tr}} = \begin{bmatrix} -\sin\psi & -\cos\psi\cos\theta_{tr} & -\sin\psi & \cos\psi\cos\theta_{tr} \\ \cos\psi & -\sin\psi\cos\theta_{tr} & \cos\psi & \sin\psi\cos\theta_{tr} \\ -\left(\frac{n_2}{\eta_0}\right)\cos\psi\cos\theta_{tr} & \left(\frac{n_2}{\eta_0}\right)\sin\psi & \left(\frac{n_2}{\eta_0}\right)\cos\psi\cos\theta_{tr} & \left(\frac{n_2}{\eta_0}\right)\sin\psi \\ -\left(\frac{n_2}{\eta_0}\right)\sin\psi\cos\theta_{tr} & -\left(\frac{n_2}{\eta_0}\right)\cos\psi & \left(\frac{n_2}{\eta_0}\right)\sin\psi\cos\theta_{tr} & -\left(\frac{n_2}{\eta_0}\right)\cos\psi \end{bmatrix}.$$

Hence, the overall transfer matrix  $\mathbf{Q} = \mathbf{K}_{tr}^{-1} \left(\prod_{m=1}^{N} \mathbf{M}_{m}\right) \mathbf{K}_{inc}$ , where *N* is the total number of layers. The input and output vectors are related

$$\begin{bmatrix} t_s \\ t_p \\ 0 \\ 0 \\ 0 \end{bmatrix} = \mathbf{Q} \cdot \begin{bmatrix} a_s \\ a_p \\ r_s \\ r_p \end{bmatrix} = \begin{bmatrix} Q_{00} & Q_{01} & Q_{02} & Q_{03} \\ Q_{10} & Q_{11} & Q_{12} & Q_{13} \\ Q_{20} & Q_{21} & Q_{22} & Q_{23} \\ Q_{30} & Q_{31} & Q_{32} & Q_{33} \\ \end{bmatrix} \cdot \begin{bmatrix} a_s \\ a_p \\ r_s \\ r_p \end{bmatrix}.$$

Since we have
$$\begin{bmatrix} r_{s} \\ r_{p} \end{bmatrix} = \begin{bmatrix} r_{ss} & r_{sp} \\ r_{ps} & r_{pp} \end{bmatrix} \cdot \begin{bmatrix} a_{s} \\ a_{p} \end{bmatrix},$$

$$\begin{bmatrix} t_{\rm s} \\ t_{\rm p} \end{bmatrix} = \begin{bmatrix} t_{\rm ss} & t_{\rm sp} \\ t_{\rm ps} & t_{\rm pp} \end{bmatrix} \cdot \begin{bmatrix} a_{\rm s} \\ a_{\rm p} \end{bmatrix}$$

we can represent all reflection and transmission coefficients under different combinations of polarization states based on elements of matrix Q. Specifically, we have reflection and transmission coefficients under linear polarizations as

$$\begin{split} r_{\rm ss} &= \frac{\dot{Q}_{30}Q_{23} - Q_{33}Q_{20}}{Q_{22}Q_{23} - Q_{23}Q_{32}}, \quad r_{\rm sp} &= \frac{Q_{31}Q_{23} - Q_{33}Q_{21}}{Q_{22}Q_{23} - Q_{23}Q_{32}}, \\ r_{\rm ps} &= \frac{Q_{32}Q_{20} - Q_{30}Q_{22}}{Q_{22}Q_{23} - Q_{23}Q_{32}}, \quad r_{\rm pp} &= \frac{Q_{32}Q_{21} - Q_{31}Q_{22}}{Q_{22}Q_{23} - Q_{23}Q_{32}}, \\ t_{\rm ss} &= Q_{00} + Q_{02}r_{\rm ss} + Q_{03}r_{\rm ps}, \quad t_{\rm sp} &= Q_{01} + Q_{02}r_{\rm sp} + Q_{03}r_{\rm pp}, \\ t_{\rm ps} &= Q_{10} + Q_{12}r_{\rm ss} + Q_{13}r_{\rm ps}, \quad t_{\rm pp} &= Q_{11} + Q_{12}r_{\rm sp} + Q_{13}r_{\rm pp}, \end{split}$$

and coefficients under circular polarizations as

$$\begin{split} r_{\rm LL} &= -\frac{r_{\rm ss} + r_{\rm pp} + j(r_{\rm sp} - r_{\rm ps})}{2}, \quad r_{\rm LR} = \frac{r_{\rm ss} - r_{\rm pp} - j(r_{\rm sp} + r_{\rm ps})}{2}, \\ r_{\rm RL} &= \frac{r_{\rm ss} - r_{\rm pp} + j(r_{\rm sp} + r_{\rm ps})}{2}, \quad r_{\rm RR} = -\frac{r_{\rm ss} + r_{\rm pp} - j(r_{\rm sp} - r_{\rm ps})}{2}, \\ t_{\rm LL} &= \frac{t_{\rm ss} + t_{\rm pp} + j(t_{\rm sp} - t_{\rm ps})}{2}, \quad t_{\rm LR} = -\frac{t_{\rm ss} - t_{\rm pp} - j(t_{\rm sp} + t_{\rm ps})}{2}, \\ t_{\rm RL} &= -\frac{t_{\rm ss} - t_{\rm pp} + j(t_{\rm sp} + t_{\rm ps})}{2}, \quad t_{\rm RR} = \frac{t_{\rm ss} + t_{\rm pp} - j(t_{\rm sp} - t_{\rm ps})}{2}. \end{split}$$

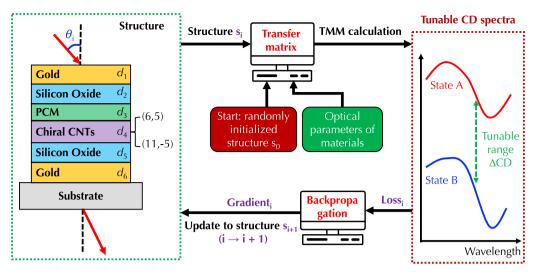


Fig. 4. Optimization flowchart. Illustration of employing GPU-accelerated calculations and backpropagation-enabled optimizations for designing reconfigurable chiral photonic

Hence, we can obtain circular reflectance and transmittance for any polarization combination with  $R=|r|^2$  and  $T=\frac{n_2\mathrm{Re}[\cos\theta_{\mathrm{tr}}]}{n_1\cos\theta_{\mathrm{tr}}}|t|^2$ . Attenuation is defined as  $A=-\log_{10}T$ , CD is defined as  $A_{\mathrm{L}}-A_{\mathrm{R}}$ , and average absorption is  $(A_{\mathrm{L}}+A_{\mathrm{R}})/2$ . Here,  $A_{\mathrm{L}}=-\log_{10}(T_{\mathrm{LL}}+T_{\mathrm{RL}})$  is the attenuation for a LCP incident light and  $A_{\mathrm{R}}=-\log_{10}(T_{\mathrm{RR}}+T_{\mathrm{LR}})$  is the attenuation for a RCP incident light.

We employed the developed transfer matrix to simultaneously fit the CD and absorption spectra of obtained single-enantiomer (6,5) and (11,–5) films and extract material parameters, including  $\omega_{\infty}, \omega_{\rm p}, \omega_{\rm 0}, \omega_{\rm 1}, \Gamma, \Gamma_{\rm 1}$ , and R in  $\varepsilon_{\rm in}$  and  $\kappa$ . We assumed that  $\varepsilon_{\rm in}$  was the same for (6,5) and (11,–5) CNTs while  $\kappa$  was different. Figs. 3a and 3b display the experimental and fitting CD and absorption spectra for both films, showing a good agreement. Figs. 3c and 3d display the extracted complex-valued  $\kappa$  and  $\varepsilon_{\rm in}$ . Note that  $\kappa$  of the (11,–5) film is larger than that of the (6,5) film because the CD signals of the (11,–5) film is larger and  $\kappa$  was treated as an effective parameter to include contributions from both intrinsic and structure-induced chiralities. The developed transfer matrix solver and material models were uploaded to a public open-source repository. I

### 3.2. ML-accelerated calculation and design of reconfigurable chiral photonic devices

Since all mathematical operations in transfer matrix calculations are based on tensor algebra, we leveraged the state-of-the-art ML framework, PyTorch, to implement the transfer matrix solver so that the calculations can be substantially accelerated on GPU hardware. Further, we were able to employ the gradient-based backpropagation algorithm in PyTorch to design chiral photonic devices. Fig. 4 illustrates the flowchart of designing a heterostack architecture consisting of single-enantiomer (6,5) or (11,-5) CNT randomly oriented films and phase change material (PCM) films for reconfigurable chiral photonic devices [21]. Upon the excitation of electrical or optical pulses, PCMs can be fast and reversely reconfigured between crystalline and amorphous phases, leading to a substantial change of dielectric functions [32-35]. Furthermore, after the reconfigurability of PCMs, the optical properties of PCMs are preserved even after removing the excitation stimulus. In addition, PCMs are scalable and compatible with other materials for constructing complex architectures [36]. Such strong non-volatile reconfigurability of scalable PCM films make Our design target is to find the best combination of layer thicknesses  $\{d_1,d_2,\dots,d_6\}$  under a given incidence angle  $\theta_i$  to produce the largest tunable range of CD, denoted as  $\Delta$ CD. The design started with a randomly initialized structure  $s_0$  and known optical constants of materials. Specifically, we utilized the fitted material parameters of single-enantiomer (6,5) and (11,–5) CNT randomly oriented films and dielectric functions of GST, silicon oxide, and gold films from our prior work. [21,46] and public database<sup>2</sup> We performed the forward calculation of CD spectra under crystalline and amorphous GST phases and defined  $-\Delta$ CD as the loss function. Hence, the minimization of the loss in the backpropagation algorithm is equivalent to maximizing  $\Delta$ CD. Based on the calculated gradient, the structural parameters were updated to  $s_1$  and these cycles were repeated multiple times to achieve optimal design.

Figs. 5a and 5b show 3D plots of optimal △CD after optimization under various  $\theta_i$  and CNT thickness  $d_{\text{CNT}}$  for (11,-5) and (6,5) films, respectively. The values of optimal ∆CD in structures with (11,-5) films are larger than those in structures with (6,5) films because of the larger  $\kappa$  of (11,-5) films; see Fig. 3c. It is clear that large oblique incident angles and thick films produce strong reconfigurability because oblique incidence breaks mirror symmetry and generates strong CD response and thick films naturally have strong chiral light-matter interaction. Notably, there is no reconfigurability of CD response at normal incidence. It seems to contradict the intuition that multiple reflections between gold reflectors can enhance chiral light-matter interaction and changing the dielectric environment between reflectors can lead to CD change. It is noted that reflectors are still planar and symmetric and the incident circularly polarized light changes the handedness, such as from LCP to RCP light or from RCP to LCP light, upon the reflection. Hence, the handedness of circularly polarized light cannot be preserved during multiple reflections so there is no enhancement or reconfigurability.

them ideal for reconfigurable photonic devices in both free space [37–40] and integrated circuits [41–45]. The top and bottom gold layers and sandwiched silicon oxide layers are intended to provide multiple reflections to enhance the chiral light-matter interaction. From a practical perspective, silicon oxide layers can also protect PCMs from being exposed to the surrounding environment for a long device lifespan. We chose germanium-antimony-tellurium (GST) PCM for the demonstration because of its mature manufacturing and broad applications.

 $<sup>^1</sup>$  Open-source  $\,$  repository. https://github.com/GaoUtahLab/chiral\_cnt\_model.

<sup>&</sup>lt;sup>2</sup> Refractive Index Database. https://refractiveindex.info/.

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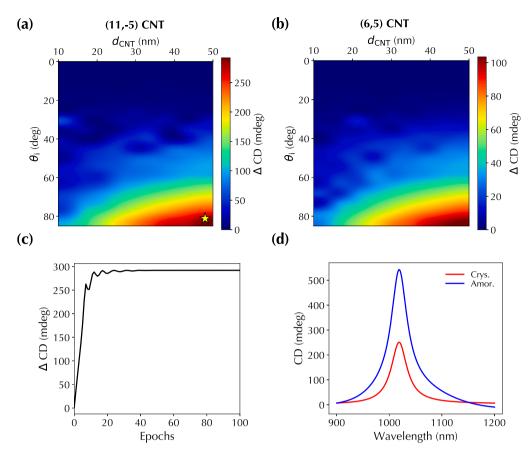


Fig. 5. Optimization results. 3D plots of optimal ΔCD after optimization under various  $\theta_i$  and CNT thickness  $d_{\text{CNT}}$  for single-enantiomer (a) (11,–5) and (b) (6,5) films, respectively. (c) The optimization curve for the architecture showing the largest tunable at  $\theta_i = 85^\circ$  and  $d_{\text{CNT}} = 50\,$  nm. (d) CD spectra under crystalline and amorphous GST phases for a 50-nm thick (11,–5) film at  $\theta_i = 85^\circ$  corresponding to the yellow star in (a).

Fig. 5c shows the evolution of  $\Delta$ CD with iteration epochs, confirming a successful optimization driven by the backpropagation algorithm. Fig. 5d demonstrates the largest tunable range of CD spectra under crystalline and amorphous GST phases for a 50-nm thick (11,–5) film at  $\theta_i=85^\circ$  (yellow star in Fig. 5a), and Fig. S9a and S9b show the reconfigurability of corresponding absorption and g factor spectra, respectively. The tunable range gradually decreases with decreasing  $\theta_i$  as shown in Fig. S10a - S10d.

#### 4. Conclusions

In summary, we created an optical material model, developed a high-performance general transfer matrix solver, extracted material parameters, and efficiently designed and optimized a reconfigurable chiral photonic heterostructure with PCMs for macroscopic, randomly oriented, single-enantiomer (6,5) and (11,–5) CNT films. The demonstrated integrated hardware and software platform opens new opportunities for exploring both fundamental chiral phenomena and novel applications based on macroscopic solid-state CNT films.

#### CRediT authorship contribution statement

Jichao Fan: Writing – review & editing, Writing – original draft, Visualization, Validation, Methodology, Investigation, Formal analysis, Data curation. Benjamin Hillam: Writing – review & editing, Methodology, Investigation, Data curation. Cheng Guo: Writing – review & editing, Software, Methodology, Data curation. Hiroyuki Fujinami: Methodology, Data curation. Koki Shiba: Methodology, Data curation. Haoyu Xie: Methodology. Ruiyang Chen: Methodology. Kazuhiro

Yanagi: Writing – review & editing, Supervision, Methodology, Funding acquisition. Weilu Gao: Writing – review & editing, Writing – original draft, Visualization, Validation, Supervision, Software, Resources, Project administration, Methodology, Investigation, Funding acquisition, Formal analysis, Data curation, Conceptualization.

#### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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#### Appendix A. Supplementary data

Supplementary material related to this article can be found online at https://doi.org/10.1016/j.carbon.2025.120016.

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