

# Sequential Pattern Learning via Kernel Alignment

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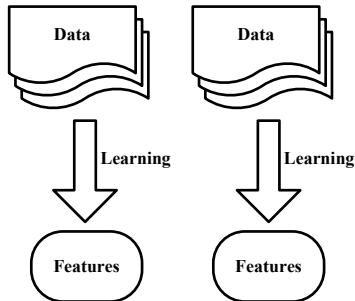
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- The calculation efficiency can be preserved for sequential learning. (✗, as a fresh attempt )

# Pattern Alignment

- General Learning Approaches



# Pattern Alignment

To make pattern alignment applicable

- Cross-domain learning
- Manifold matching

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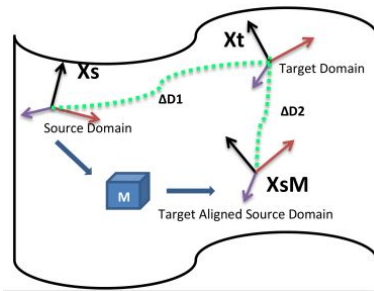
Suspicious, e.g.,

- Sequential Pattern Alignment



# Domain Adaptation

The figures from B. Gong's GFK and B. Fernando's SA papers

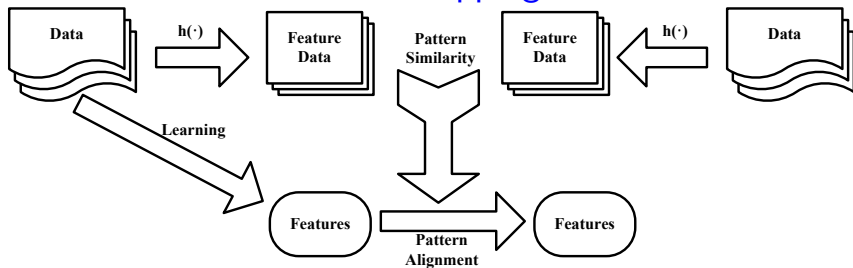


# Continuous Manifold Based Adaptation

- CMA: A continuous extension of GFK
- SA (Subspace Alignment): Can be conveniently extended
- The further considerations are necessary for advancements

# Pattern Alignment

Sequential alignment of incremental patterns with  
feature mapping



# Pattern Alignment

- Sequential alignment of incremental patterns with feature mapping
- It is, but not restricted to reference patterns derived from feature kernel spaces

# Basic Idea

- The source data is affected by target data sequentially.
- The subspace patterns of source and target data are aligned.
- Parallel mapping is involved to indirect alignments.

# Feature alignment

$$\begin{aligned}x_s &\sim h(x_s) \sim p(h(x_s)) \\x_t &\sim h(x_t) \sim q(h(x_t))\end{aligned}\tag{1}$$

$$\Psi = \int_{x_s} \int_{x_t} \psi(h(x_s), h(x_t)) dh(x_s) dh(x_t), \tag{2}$$

# Pattern alignment

$$\varphi(x_s, x_t) = \int_{x_s} \int_{x_t} f(x_s) \cdot g(x_t) dx_s dx_t \quad (3)$$

$$\Psi = \int_{x_s} \int_{x_t} \psi(h(x_s), h(x_t)) dh(x_s) dh(x_t) \quad (4)$$

# Pattern Alignment

Suppose that only source data are involved,

$$J = \arg \min_{\Gamma} \sum_{x_s} \|f(x_s) f(x_s) - h(x_s) \Gamma h(x_s)\|^2 + \lambda (\Gamma h(x_s)) \quad (5)$$

$$J = \arg \min_{\Gamma} \sum_{x_s} \|f(x_s) \cdot f(x_s) - k_s M k_s\|^2 + \lambda \text{tr}(M k_s), \quad (6)$$



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$$J = \arg \min_{\Pi} \sum_{x_s} \|f(x_s) - \Pi k_s\|^2 + \lambda \text{tr}(\Pi k_s) \quad (9)$$

# Pattern Alignment

$$\begin{aligned} J = \arg \min_f \sum_{x_s} \sum_{x_t} & \|f(x_s)g(x_t) - k_{st}Mk_s\|^2 \\ & + \lambda \text{tr}(Mk_s) \end{aligned} \quad (10)$$

# Pattern Alignment

$$J = \arg \min_f \sum_{x_s} \sum_{x_t} \|f(x_s) g(x_t) - k_{st} M k_s\|^2 + \lambda \text{tr}(M k_s) \quad (11)$$

Tips: iterative learning is possible by fixing one item while solving another

# Sequential Pattern Alignment

The last target data is denoted by  $X_t' \in R^{d \times a}$ , and the source data set  $X_s$  is modified with appended  $X_t'$ .

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- $f(\cdot)$  is necessary to be modified corresponding to incremental data
- Feature alignment  $M$  also needs to be updated as well as kernels

# Sequential Pattern Alignment

- To update  $f(\cdot)$  with subspace alignment, it is straightforward to adopt **SVD update algorithm** to orthogonal decomposition of  $X_s$

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- To update  $f(\cdot)$  with subspace alignment, it is straightforward to adopt **SVD update algorithm** to orthogonal decomposition of  $X_s$
- Feature alignment  $M$  is updated with appended kernel matrices and the main calculation is on **inverse of kernels**
- The inverse of kernels can be approximated with SVD of kernel matrices  $K = V\Lambda^2V^T$

# Sequential Pattern Alignment

- The decomposition of updated kernel matrix is learned by following the incremental KPCA (H. Zhao et. al., 2006)

$$K = \begin{bmatrix} K_{ss} & K_{st} \\ K_{ts} & K_{tt} \end{bmatrix} = \begin{bmatrix} P_s & P_1 \\ P_2 & P_3 \end{bmatrix}^T \begin{bmatrix} P_s & P_1 \\ P_2 & P_3 \end{bmatrix}. \quad (13)$$

# Experiments

- Implemented in R language platform
- Ten common classes in three domains, namely Caltech, Amazon, DSLR, are referred, which contains 1123 (Caltech), 958 (Amazon), 157 (DSLR) images, respectively.
- SURF features of each data are extracted, and several state-of-the-art methods are involved to evaluate the performance.

# Experiments

**Table:** Classification accuracy (%) in object recognition with SURF features

Method	A -> C	C -> A	A -> D	D -> A	C -> D	D -> C	Mean
Baseline	15.94	15.66	3.18	6.68	15.92	12.38	11.63
LSCCA	26.63	28.5	30.57	18.89	28.03	15.05	24.61
GFK	35.55	36.29	31.97	32.5	36.97	29.58	33.81
unsupervised KEMA	22.8	26.3	20.38	22.96	31.85	26.54	25.14
SA	35.62	36.74	25.48	24.22	25.48	27.25	29.13
TCA	20.57	25.68	12.74	24.43	18.28	24.58	21.05
SPA	32.41	33.3	26.11	25.68	26.11	25.56	28.2

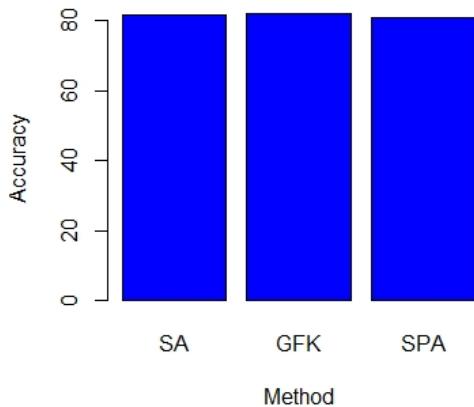
# Experiments

Sequential learning on benchmark traffic scene classification.

- 512 dimensional GIST features are learned from images.
- 500 labeled images are given, and then 2000 images come in a sequence with 100 images per duration.



# Experiments



# Experiments

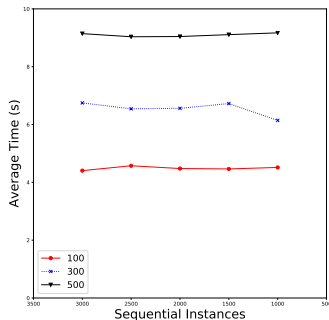
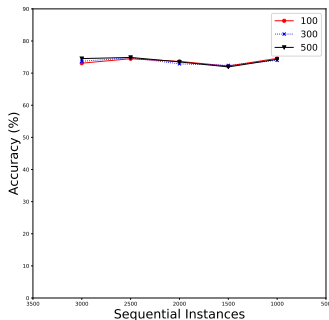
## Sequential learning on flower data set

- 512-dimensional VGG features are learned representatively
- 1000 instances are randomly selected to be source data, while target instances ranging from 1000 to 3000



# Experiments

Experimental results v.s. different sizes of sequential data





# Conclusion and Future Works

- A novel approach to sequential pattern alignment is proposed in this work, which considers the feature alignment as a reference for subspace alignment, while further more data is absorbed for sequential learning.
- The performance of proposed method is comparable, as a fresh attempt for further advancements.

# Conclusion and Future Works

This work can be continued with several open problems:

- Improvements of learning efficiency, and iterative learning could be adopted.
- Other attempts to replace the feature alignment can be done.
- Further extensions to multi-view pattern alignment is possible.

# Thank You