



下一项



测验,6个问题

How many satisfying assignments does the following formula have? $(x_1 ee \overline{x}_2 ee \overline{x}_3)(x_1 ee x_2)(\overline{x}_1 ee \overline{x}_2)$

1/1分

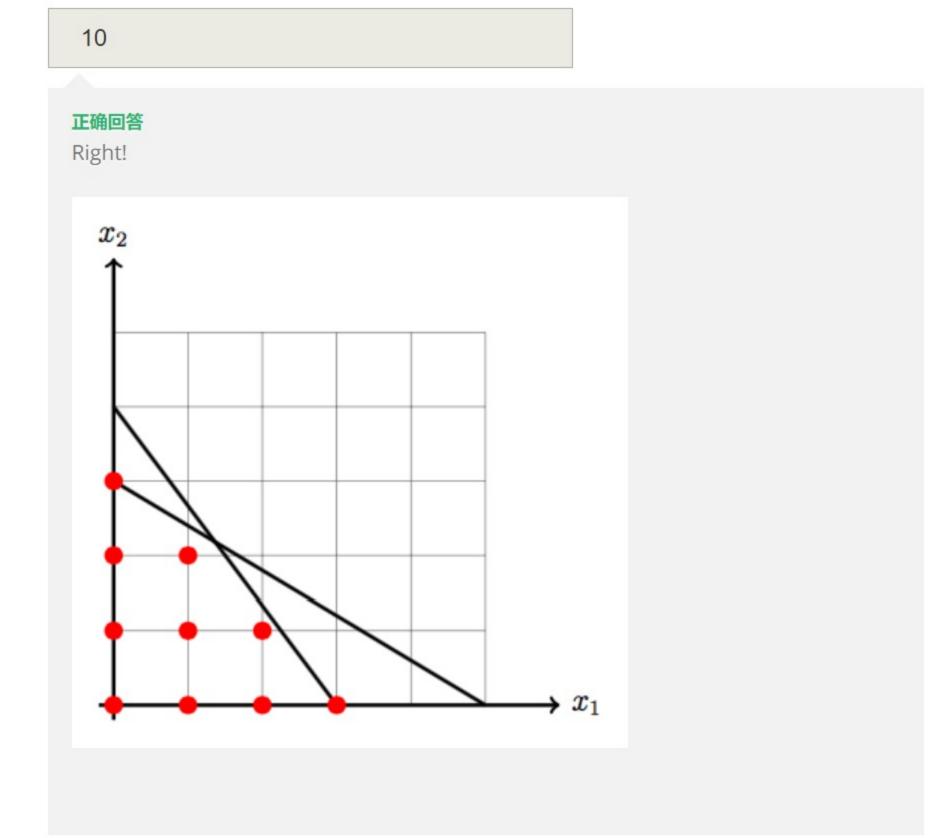
3

正确回答 That's right!

How many integer solutions does the following linear program have?

1/1分

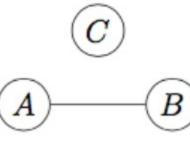
 $x_1 \ge 0$, $x_2 \ge 0$, $4x_1 + 3x_2 \le 12$, $3x_1 + 5x_2 \le 15$





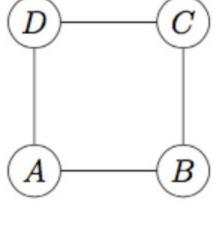
Consider the following graph:





How many different independent sets does the following graph have?

It has 6 different independent sets: empty set, $\{A\}$, $\{B\}$, $\{C\}$, $\{A,C\}$, $\{B,C\}$.



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正确回答

That's right! They are empty set, $\{A\}$, $\{B\}$, $\{C\}$, $\{D\}$, $\{A,C\}$, $\{B,D\}$.



one of three available colors to its vertices such that the ends of each edge of the graph receive different colors. This is clearly a search problem: given a graph and a coloring of its vertices, one can check in polynomial time whether there are only three different colors and that no edge is monochromatic. This problem is known to be NP-complete. Do we have a polynomial time algorithm for this problem? This is an open problem.

In the 3-coloring problem, you are given an undirected graph and the goal is to assign



That's right! We cannot find a polynomial time algorithm for any of NP-complete

Yes, this problem can be solved in polynomial time.

No, this problem cannot be solved in polynomial time for sure.

problems. Nor we can prove that there is no such algorithm. Thus, the existence

of a polynomial time algorithm for an NP-complete problem is an open problem.

0/1分

can then use the fact that SAT reduces to 3-SAT. In the Independent Set problem we are given a graph G with n vertices $\{1,2,\ldots,n\}$ and a positive integer b. Our goal is to check whether the graph has b vertices

In the lectures, we constructed a reduction from 3-SAT to Independent Set. Now, we

show the reverse reduction. For this, we are going to reduce Independent set to SAT. We

 $\{u_1,u_2,\ldots,u_b\}\subseteq\{1,2,\ldots,n\}$ with no edge between any pair of them. We are going to construct a CNF formula ${\cal F}$ that is satisfiable if and only if the graph ${\cal G}$ contains such an independent set. There will be bn Boolean variables: for $1 \leq i \leq b$ and $1 \leq j \leq n$, $x_{ij}=1$ if and only if the i-th vertex of the required independent set is the j-th vertex of the graph (that is, $u_i = j$). We then introduce the following constraints:

2. u_i is equal to exactly one vertex of the graph: for all $1 \leq i \leq b$ and all $1 \leq j \neq j' \leq n$, $(\bar{x}_{ij} \lor \bar{x}_{ij'});$

1. u_i is equal to some vertex of the graph: for all $1 \leq i \leq b$, $(x_{i1} \vee x_{i2} \vee \cdots \vee x_{in})$;

- 3. $u_i \neq u_{i'}$: for all $1 \leq i \neq i' \leq b$ and all $1 \leq j \leq n$, $(\bar{x}_{ij} \vee \bar{x}_{i'j})$;
- 4. no two vertices from the independent set are joined by an edge: for all $1 \leq i \neq i' \leq b$ and all $\{j,j'\}\in E(G)$, $(\bar{x}_{ij}\vee \bar{x}_{i'j'})$.

The resulting formula is satisfiable if and only if the initial graph has an independent set

No, it is not correct, because for a graph that does not have an independent set of size b it might produce an a satisfiable formula.

Is this reduction correct?

No, it is not correct, because it is not a polynomial time reduction.

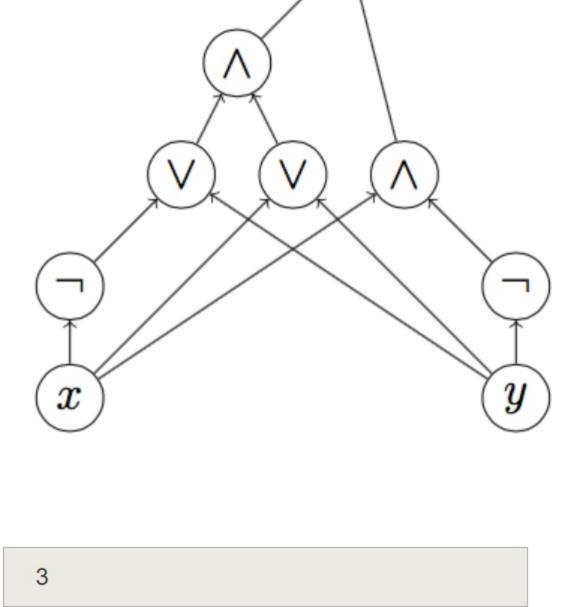
这个选项的答案不正确

No, it is correct, in fact. The running time of the reduction is polynomial since the total length of the resulting formula is bounded by a polynomial in the number of vertices and edges of the graph: the total number of clauses is at most

No, it is not correct, because it might produce an unsatisfiable formula for a graph that has an independent set of size b. Yes, the reduction is correct.

1/1分

How many satisfying assignments does the following circuit have?



正确回答 That's right! The only falsifying assignment is x=y=0.

of size b.

 $b+bn^2+b^2n+bn^2=O(n^3)$ (since $b\leq n$ and the number of edges is at most

 n^2).