

Soal 1

Kompleksitas Waktu Analisis Algoritma

Perhatikan algoritma pencarian elemen minimum dalam sebuah array berikut (dalam pseudocode):

```

procedure FindMin(A : array of n elements)
    min ← A[0]
    for i ← 1 to n - 1 do
        if A[i] < min then
            min ← A[i]
        end if
    end for
    return min
end procedure

```

Berdasarkan algoritma di atas, implementasikan dan analisis kompleksitasnya

Ingat!

$$\begin{aligned}
T_{min}(n) &= c_1 + c_2(n-1) + c_3(n-1) \\
&\approx an + b \\
&\rightarrow O(n)
\end{aligned}$$

$$\begin{aligned}
T_{max}(n) &= c_1 + c_2(n-1) + c_3(n-1) + c_4(n-1) \\
&\approx 2n - 1 \\
&\rightarrow O(n)
\end{aligned}$$

Best Case

Baris	Pseudocode	COST	FREKUENSI	TOTAL COST
1	procedure FindMin	C1	1	C1
2	min ← A[0]	c2	1	c2
3	for i ← 1 to n - 1 do	C3	n	c3(n)
4	if A[i] < min then	C4	n-1	c4(n-1)
5	min ← A[i]	C5	0	0
6	end if	c6	n-1	c6(n-1)
7	end for	c7	n	c7(n)
8	return min	c8	1	c8
9	end procedure	c9	1	c9

$$T(n) = \\ C1 + C2 + C3n + C4(n-1) + 0 + C6(n-1) + C7n + C8 + C9$$

$$C4(n-1) \rightarrow C4n - C4 \\ C6(n-1) \rightarrow C6n - C6$$

$$T(n) = C1 + C2 + C3n + C4n - C4 + 0 + C6n - C6 + C7n + C8 + C9$$

$$T(n) = (C3 + C4 + C6 + C7)n + (C1 + C2 + C8 + C9 - C4 - C6)$$

Jika semua Ci = 1:

$$T(n) = (1+1+1+1)n + (1+1+1+1-1-1)$$

$$T(n) = 4n + 2$$

Karena berbentuk fungsi linear, maka:

$$T(n)=O(n)$$

Worst Case

Baris	Pseudocode	COST	FREKUENSI	TOTAL COST
1	procedure FindMin	C1	1	C1
2	min \leftarrow A[0]	c2	1	c2
3	for i \leftarrow 1 to n - 1 do	C3	n	c3(n)
4	if A[i] < min then	C4	n-1	c4(n-1)
5	min \leftarrow A[i]	C5	n-1	c5(n-1)
6	end if	c6	n-1	c6(n-1)
7	end for	c7	n	c7(n)
8	return min	c8	1	c8
9	end procedure	c9	1	c9

$$T(n) = \\ C1 + C2 + C3n + C4(n-1) + C5(n-1) + C6(n-1) + C7n + C8 + C9$$

$$C4(n-1) \rightarrow C4n - C4$$

$$C5(n-1) \rightarrow C5n - C5$$

$$C6(n-1) \rightarrow C6n - C6$$

Maka:

$$T(n) = (C3 + C4 + C5 + C6 + C7)n + (C1 + C2 + C8 + C9 - C4 - C5 - C6)$$

Jika semua $C_i = 1$:

$$T(n) = (1+1+1+1+1)n + (1+1+1+1-1-1-1)$$

$$T(n) = 5n + 1$$

Karena berbentuk fungsi linear, maka:

$$T(n)=O(n)$$

OUTPUT

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Nilai minimum = 1
Indeks minimum = 0
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