

Recap

For this chapter, it is important to understand the concepts of thermodynamics before balancing. You can also use these concepts to see if your work/answer make sense in the end.

1. At which conditions can you assume ideal gas?

- a. Low temperature and low pressure
- b. High temperature and low pressure
- c. High Pressure and low temperature
- d. High temperature and high pressure

2. What does it mean if a vapor is superheated?

- a. Its temperature is above the bubble point
- b. Its temperature is above the dew point
- c. Its temperature is below the bubble point
- d. Its temperature is below the dew point

3. What is gauge pressure relative to?

- a. Full vacuum
- b. atmospheric
- c. absolute zero
- d. standardized pump

4. If a gas is assumed incompressible, what is its density a function of?

- a. Nothing (it is constant)
- b. Temperature only
- c. Pressure only
- d. Both temperature and pressure

5. What does a compressibility factor of >1 mean?

- a. Ideal gas law can be used
- b. Ratio of PV/RT is > 1
- c. Ratio of PV/RT is < 1
- d. None of the above

Gibbs Phase Rule

$$F = 2 + (c - r) - \pi$$

where c is the number of chemical species, r is the number of chemical reactions, and π is the number of phases

Clausius-Clapeyron Equation

Look at its derivation and its approximations.

1. 3 approximation and the reasoning behind them
2. derivation from differential form to algebraic

This was on the second midterm and also on the final for last years exam.

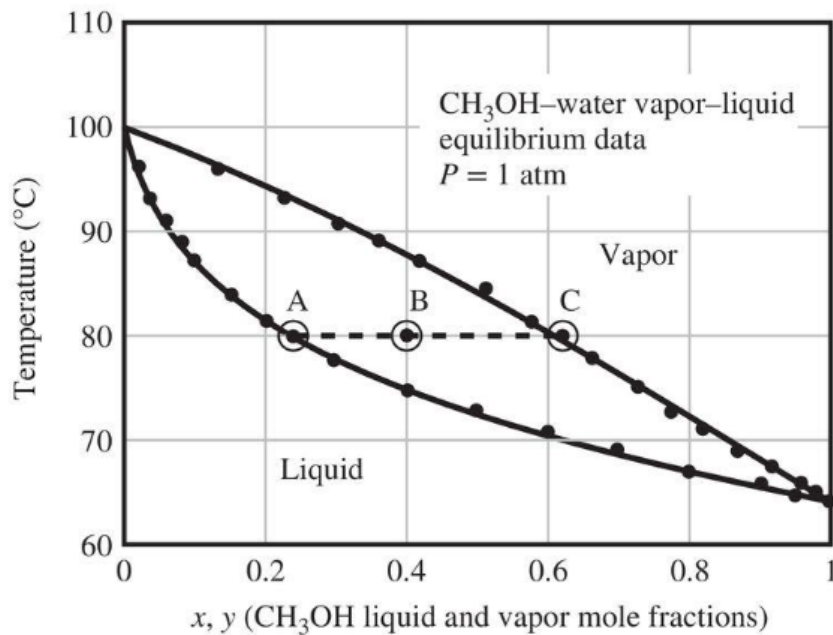
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In [1]: from IPython.display import YouTubeVideo
        YouTubeVideo('Adr9_2LnQdw', width=800, height=300)
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Out[1]:



Example Problem 1

A methanol–water feed stream is introduced to a vaporizer in which a molar fraction of the feed is vaporized. The feed has a methanol mole fraction of $x_F=0.4$, and the vaporizer operates at a pressure of 1 atm absolute and 80°C . Vapor and liquid leaving the device are in equilibrium at the temperature and pressure of the system and have methanol mole fractions of y and x , respectively. A Txy diagram for methanol–water mixtures at 1 atm absolute is shown below. The feed to the vaporizer and the liquid and vapor product streams are shown as points B, A, and C, respectively.



a) Prove that f can be determined from the equation: where V : mole of vapor, L : mole of liquid, F : mole of feed. Use this result to determine f for the specific conditions cited above ($x_F = 0.4$, $T = 80^\circ\text{C}$).

$$f = \frac{V}{L} = \frac{x_F - x}{y - x_F}$$

b) Use the T_{xy} diagram to estimate the minimum and maximum temperatures at which the given feed stream could be separated into vapor and liquid fractions at 1 atm. In each case, what fraction of the feed would be vaporized?

c) The vapor at C is sent to a condenser operated at constant pressure (1 atm) and temperature 78°C . At this temperature, the pure methanol vapor pressure is 1.66 atm. The liquid (L_2) and vapor (V_2) product streams leaving the condenser are in equilibrium and in a ratio of 1 mol vapor/1 mol liquid. Estimate the methanol compositions (x_2 and y_2) in the two streams leaving the condenser.

Solution:

a)

1. write out balances:

$$\text{Mole balance: } F = V + L$$

$$\text{MeOH mole balance: } x_F F = yV + xL$$

1. derive equations:

$$x_F F = yV + xL$$

$$\begin{aligned} x_F(V + L) &= yV + xL \\ (y - x_F)V &= (x_F - x)L \\ f &= \frac{V}{L} = \frac{x_F - x}{y - x_F} \end{aligned}$$

1. Find x and y.

use T_{xy} diagram to find x and y at $T=80^\circ\text{C}$

1. Solve for f

plug in $x_F = 0.4$, x, and y to find f

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In [1]: xf = 0.4  
x = 0.23  
y = 0.62  
f = (0.4-0.23)/(0.62-0.4)  
f
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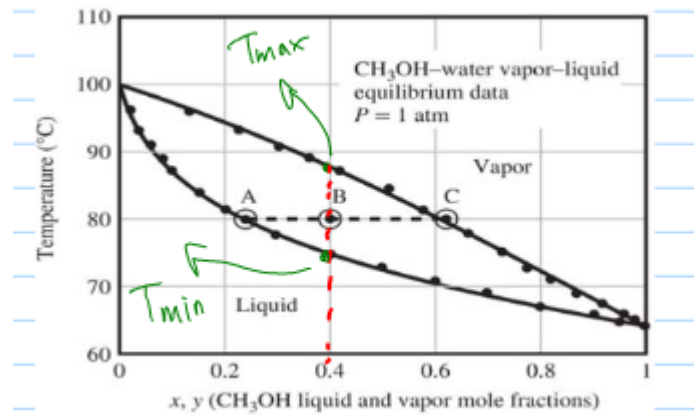
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Out[1]: 0.7727272727272729
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b)

1. recognize that the two phase must exist in equilibrium since there are both vapor and liquid fractions

This implies that it has to be within the two-phase region of the T_{xy} diagram

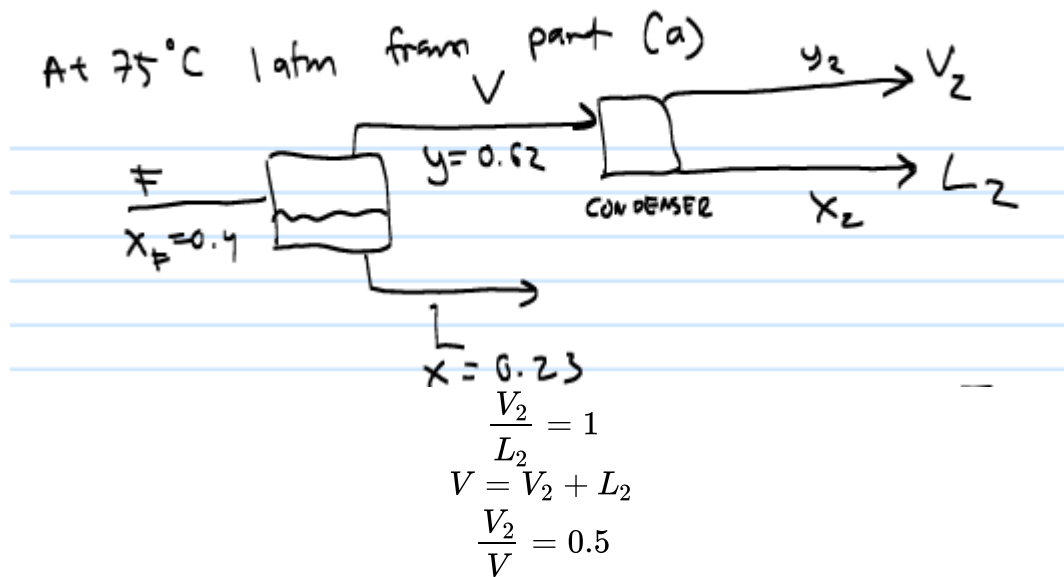
1. use the T_{xy} diagram to find T_{max} and T_{min}



At $T_{max} = 87$, $f = 1$ and at $T_{min} = 75$, $f = 0$ for $x_F = 0.4$

c)

1. Draw process diagram



1. Use given condition and derive equation for MeOH balance

$$yV = y_2V_2 + x_2L_2$$

$$y \frac{V}{V_2} = y_2 + x_2 \frac{L_2}{V_2}$$

$$y \frac{V}{V_2} = y_2 + x_2 f$$

plug in values from part a

$$0.62(2) = x_2(1) + y_2$$

$$1.24 = x_2 + y_2$$

Two unknowns so we need some law that can relate the two unknowns

1. Use Raoult's law

$$y_2P = x_2P_{MeOH}^*(T)$$

1. Combine two equations and solve

$$1.24 = x_2 + x_2 \frac{P_{MeOH}^*}{P}$$

$$x_2 = \frac{1.24}{1 + \frac{P_{MeOH}^*}{P}}$$

$$x_2 = 0.47$$

$$y_2 = 0.77$$

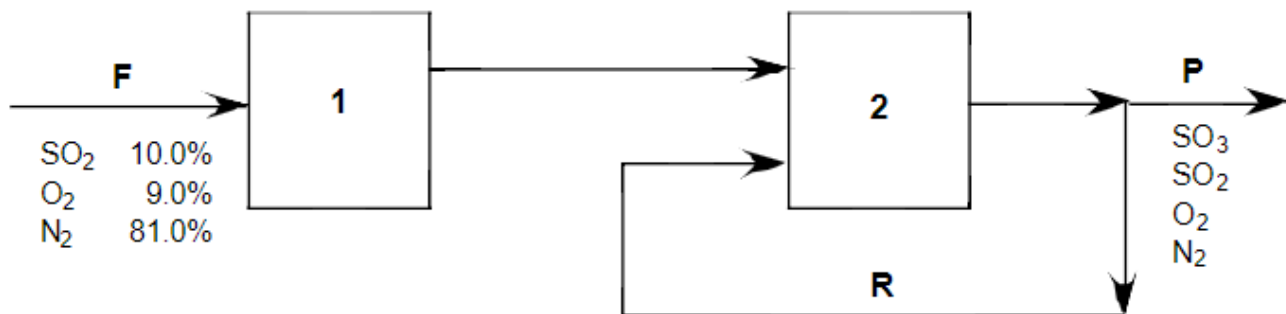
Mass Balance Question

Sulfur dioxide may be converted to SO_3 , which has many uses including the production of H_2SO_4 and the sulphonation of fatty acids to make detergent. A gas stream having the molar composition shown in the figure below is to be passed through a two-stage converter (reactor). The single-pass fractional conversion of SO_2 to SO_3 in the first stage is 0.77 and in the second stage, 0.63. To boost the overall process conversion to 0.95, some of the exit gas from stage 2 is recycled back to the stage 2 inlet.

- a) Draw and label the flowchart given that 100 kmol/h of feed gas, F, is fed.
- b) Write the balanced stoichiometric equation for the SO_2 reaction with O_2 to produce SO_3 .
- c) Determine how much gas is recycled in kmol/h.

Solutions

a)



Put the basis of 100 kmol/hr at F

At 1, $f = 0.77$

At 2, $f = 0.63$

Overall, $f = 0.95$

b)

SO2:

$$y_{PSO_2}P = m_{SO_{20}} - \zeta$$

SO3:

$$y_{PSO_3}P = m_{SO_{30}} + \zeta$$

O2:

$$y_{SO_2}P = m_{O_{20}} - 0.5\zeta$$

N2:

$$y_{PNO_2} = (1 - y_{PSO_2} - y_{PSO_3} - y_{PO_2})$$