The Q Function and Baseband Data Communication

Eren Can Gungor Riccardo Miccini Technical University of Denmark - DTU

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1 Eye Diagram for a Digital Communication Channel

1.1 Eye diagram

1.2 c5ce2.m: explanation

Here follows a thoroughly commented version of the provided c5ce2.m MAT-LAB script. The code below generates and plots the eye diagrams of four band-limited signals composed of random sequences of bits.

```
% clean figure and load signal package (only for Octave)
clf
pkg load signal
\% simulation parameters:
\% - nr of symbols (must be divisible by 4)
\% - nr of samples per symbol
\% - filter cutoff values (normalized values)
nsym = 100;
nsamp = 50;
bw = [0.4 \ 0.6 \ 1 \ 2];
% for each filter..
for k = 1: length(bw)
  % generate filter coefficients
  lambda = bw(k);
  [b,a] = butter(3,2*lambda/nsamp);
  l = nsym*nsamp;
  % Total sequence length
  y = zeros(1, l-nsamp+1);
  \% Initalize random output vector with +1 and -1
  x = 2*round(rand(1, nsym)) - 1;
  % for each overlap ...
  for i = 1:nsym
    % place symbols into vector y
    kk = (i-1)*nsamp+1;
```

```
y(kk) = x(i);
  end
  % zero-order hold
  datavector = conv(y, ones(1, nsamp));
  % apply filter to complite sequence
  filtout = filter(b, a, datavector);
  % splice sequence into sub-sequences of 4 symbols
  datamatrix = reshape(filtout, 4*nsamp, nsym/4);
  % discart the first 6 sub-sequences
  datamatrix1 = datamatrix(:, 6:(nsym/4));
  % plot and format
  \mathbf{subplot}(\mathbf{length}(\mathbf{bw}), 1, \mathbf{k})
  plot(datamatrix1, 'k')
  ylabel('Amplitude')
  axis ([0 200 -1.4 1.4])
  legend(['Bn=-', num2str(lambda)])
  if k == 4
    xlabel ('t/Tsamp')
  end
end
```

1.3 Channel model

1.4 c5ce2.m: different bandwidths

1.5 c5ce2.m: plots

This section will elaborate on the results and implications of the plots generated by the two scripts.

2 The Q function

2.1 Normal probability density function 2.1

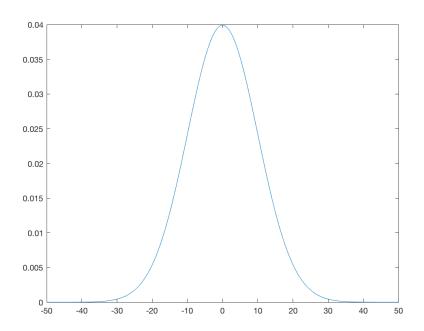


Figure 1: Normal Gaussian pdf graph with defined intervals

Normal gaussian distribution is one of the most important concept in Communication system and in statistics. It is used as a powerful tool when investigating random signals in communication systems. Such as investigating behaviour and application of noise signals.

The other reason is that because it is characterised by the limited variables. Such as mean μ and σ . It is easier compute and understand when we apply on communication systems.

All the variables that has been used in graphingpdf.m has been explained below;

mu. This is the mean value (μ) for the normal probability density function.

sigma This the sensible standard deviation number. (σ) .

MAX 50; Maximum x value that x vector will get

MIN -50; Minimum x value that x vector will get

Also general formula for gaussian pdf is; $y=f(x|\mu,\sigma)=(\frac{1}{\sigma\sqrt{2\pi}})e^{\frac{-(x-\mu)^2}{2(\mu)^2}}$ As we can see and understand from the variables above and the formula that all variables has been specified and we only need σ , μ and range.

2.2 Explanation of Q(u) function in relation to the normal probability density function

As we have explained and investigated probability density density function above. We can easily link Q(u) function by exploiting the properties of cumulative distribution function and Probability density function.

- Q function is the 1- minus the cumulative distribution function of the standardised normal variable.
- Gaussian pdf with unit variance and zero mean is $R = (\frac{1}{\sqrt{2\pi}})e^{\frac{-(x)^2}{2}}$
- And corresponding cumulative distribution function become; $P = \int_{-\inf}^{x} Z$
- In last step Gaussian Q function defined as $Q(x) = 1 P(x) = \int_x^{-\inf} Z$

2.2.1 Inverse Q function

2.2.2 Complementary error function

2.3 Plots

3 Source Code

Here we have the properly prepared MATLAB codes for the second part of the second project. It has been used for observations, calculations and comparing with specified commands that given in this project.

The code belows computes and graphs normal (Gaussian) probability density function (pdf) in an appropriate intervals

```
%graphing PDF function with random variables mu=0; sigma=10; MAX = 50; MIN = -50; STEP = (MAX - MIN) / 1000; PDF = normpdf(MIN:STEP:MAX, mu, sigma); plot(MIN:STEP:MAX, PDF)
```

- 4 The Matched Filter Base Band Receiver
- 4.1 Additive white gaussian noise model
- 4.2 c8cela.m: explanation
- 4.3