

# Searches for charged lepton flavour violation at colliders

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Michael A. Schmidt

5 October 2019

Intensity Frontier in Particle Physics, NCTS, Hsinchu

based on work in collaboration with

Yi Cai 1510.02486

Yi Cai, German Valencia 1802.09822

Tong Li 1809.07924, 1907.06963



The Standard Model is very successful. . .

... but incomplete

In particular neutrinos are massive

many different possibilities – see Cai, Herrero-Garcia, MS, Vicente, Volkas 1706.08524

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Lepton flavour is not conserved

→ Flavour changing processes are a sensitive probe

- in  $\text{SM} + m_\nu$ , suppressed by unitarity,  $\mathcal{A} \sim G_F m_\nu^2 \simeq 10^{-26}$
- many neutrino mass models have large charged LFV due to non-unitarity or new contributions, e.g. inverse seesaw, radiative mass models
- could be completely unrelated to neutrino mass, e.g. SUSY

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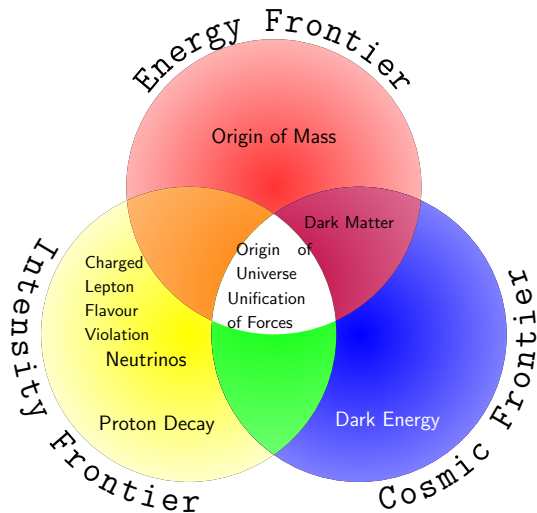
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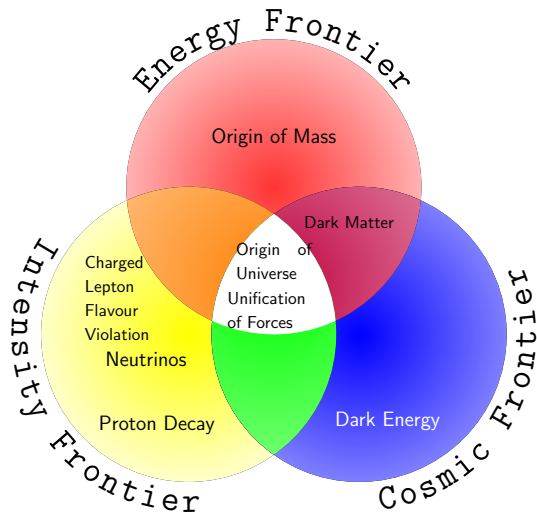
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# cLFV in scattering processes: overview

LHC:  $q\bar{q}, gg \rightarrow \ell\ell'$

Future lepton colliders:  $e^+e^- \rightarrow \ell\ell'$

Future lepton colliders:  $e^+e^- \rightarrow \ell\ell' + X$

Other searches

Conclusions

**LHC:**  $q\bar{q}, gg \rightarrow \ell\ell'$

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## D6 Operators with 2 Quarks and 2 Leptons

Buchmüller, Wyler NPB268(1986)621; Grzadkowski et al 1008.4884; Carpentier, Davidson 1008.0280; Petrov,Zhuridov 1308.6561

Vector

$$\begin{aligned} \mathcal{Q}_{lq}^{(1)} &= (\bar{L}\gamma_\mu L)(\bar{Q}\gamma^\mu Q) & \mathcal{Q}_{lq}^{(3)} &= (\bar{L}\gamma_\mu \tau^I L)(\bar{Q}\gamma^\mu \tau^I Q) \\ \mathcal{Q}_{eu} &= (\bar{\ell}\gamma_\mu \ell)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ed} &= (\bar{\ell}\gamma_\mu \ell)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{lu} &= (\bar{L}\gamma_\mu L)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ld} &= (\bar{L}\gamma_\mu L)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{qe} &= (\bar{Q}\gamma_\mu Q)(\bar{\ell}\gamma^\mu \ell) \end{aligned}$$

Scalar  $\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha) \quad \mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta u)$

with same-flavour quark

Tensor  $\mathcal{Q}_{lequ}^{(3)} = (\bar{L}^\alpha \sigma_{\mu\nu} \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta \sigma^{\mu\nu} u)$

## D8 Operators with 2 Gluons and 2 Leptons

$$\begin{aligned} \mathcal{O}_X^{ij} &= \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) & \mathcal{O}'_X{}^{ij} &= i \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) \\ \bar{\mathcal{O}}_X^{ij} &= i \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) & \bar{\mathcal{O}}'_X{}^{ij} &= \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) \\ \mathcal{O}_Y^{ij} &= i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{L}_i \gamma^\mu D^\nu L_j & \mathcal{O}_Z^{ij} &= i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{e}_{Ri} \gamma^\mu D^\nu e_{Rj} \end{aligned}$$

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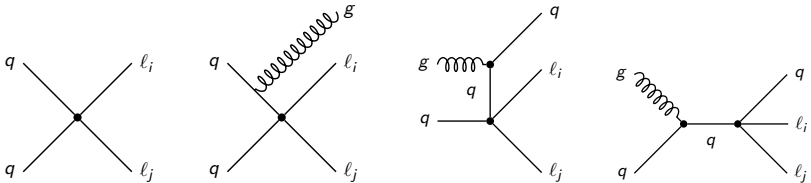
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Processes at LHC:  $pp \rightarrow \ell_i \ell_j + \text{jets}$



Signal: opposite-sign different flavour pair of leptons

Several existing searches:

- ATLAS 7 TeV: LFV heavy neutral particle decay to  $e\mu$  [ATLAS 1103.5559](#)
- CMS 8 TeV: LFV heavy neutral particle decay to  $e\mu$  [CMS-PAS-EXO-13-002](#)
- **ATLAS 7 TeV: LFV in  $e\mu$  continuum in  $\tilde{\chi}$  SUSY** [ATLAS 1205.0725](#)
- **ATLAS 8 TeV: LFV heavy neutral particle decay** [ATLAS 1503.04430](#)
- CMS 8 TeV: LFV heavy neutral particle decay to  $e\mu$  [CMS 1604.05239](#)
- ATLAS 13 TeV,  $3.2 \text{ fb}^{-1}$ : LFV heavy neutral particle decay [ATLAS 1607.08079](#)
- ATLAS 13 TeV,  $36.1 \text{ fb}^{-1}$  [ATLAS 1807.06573](#)

## Recast limits of most sensitive previous searches

ATLAS 1503.04430	ATLAS 1205.0725
8 TeV	7 TeV
20.3 fb <sup>-1</sup>	2.1 fb <sup>-1</sup>
$e\mu$ , $e\tau$ , $\mu\tau$	$e\mu$
inclusive	exclusive
including arbitrary number of jets	separated by number of jets

## Projection to 14 TeV

- Assume 300 fb<sup>-1</sup>
- Follow searching strategy of exclusive 7 TeV search

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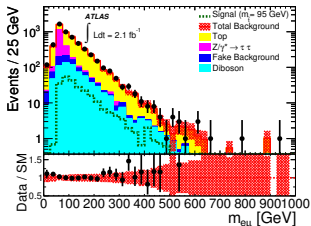


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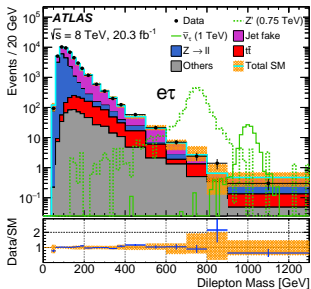
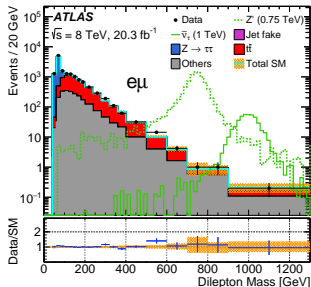
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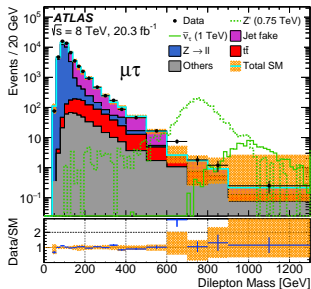
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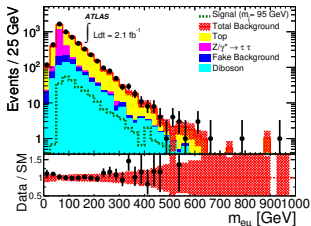
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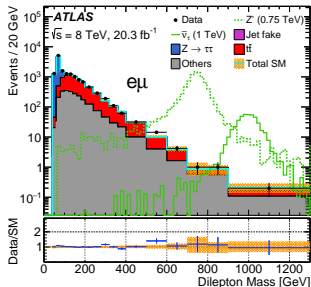
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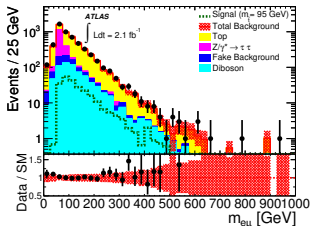
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also  $W/Z$  plus jets,  $WZ/ZZ$ , single top and  $W/Z + \gamma$

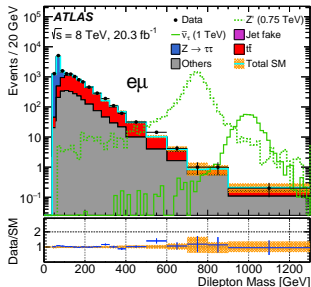
⇒ Efficiently reduced in exclusive 7 TeV analysis  
by rejecting jets and  $E_T^{miss} < 20$  GeV

- Modelling of main background agrees with ATLAS
- Fake background estimated from data

⇒ Use background from ATLAS publications



ATLAS 7TeV 1205.0725



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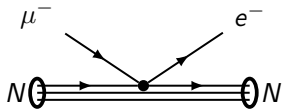
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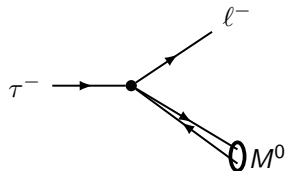
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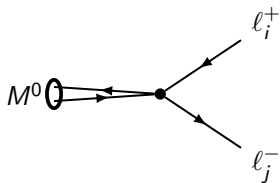
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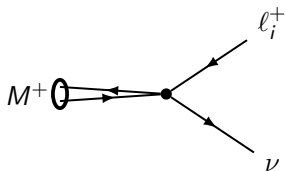
$\mu - e$  conversion in nuclei



$\tau \rightarrow \ell M^0$



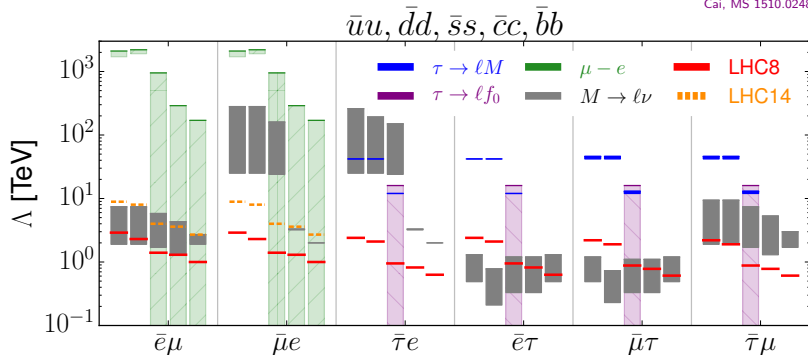
$M^0 \rightarrow \ell_i^+ \ell_j^-$



$M^+ \rightarrow \ell_i^+ \nu$

# cLFV at hadron colliders: quarks

Cai, MS 1510.02486



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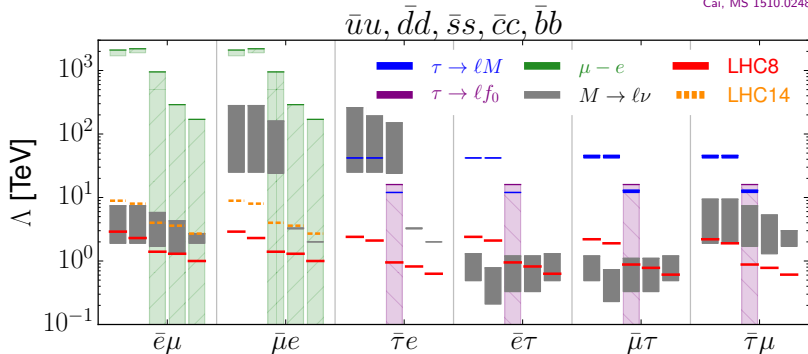
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LHC more interesting for vector operators with right-handed quark currents due to weaker constraints from intensity frontier

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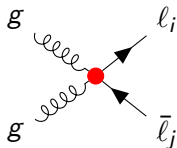


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Signal:  
opposite-sign different flavour pair of leptons

## Most sensitive searches

ATLAS 1607.08079

CMS-PAS-EXO-16-058 1802.01122

13 TeV

13 TeV

3.2 fb<sup>-1</sup>

35.9 fb<sup>-1</sup>

$e\mu$ ,  $e\tau$ ,  $\mu\tau$

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inclusive

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newer ATLAS search: 13 TeV, 36.1 fb<sup>-1</sup> 1807.06573

EFT scattering amplitudes

$$\mathcal{A}(s) \simeq \frac{s}{\Lambda^2} \xrightarrow{s \rightarrow \infty} \infty$$

⇒ Violation of perturbative unitarity

## Solutions:

- UV-complete models/simplified models
- apply unitarization procedure, e.g. K-matrix unitarization

Wigner 1964; Wigner, Eisenbud 1947; Gupta 1950

Recent application to monojets: Bell, Busoni, Kobakhidze, Long, MS 1606.02722

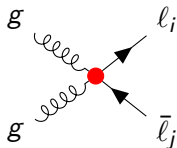
- couplings → form factor

Baur, Zeppenfeld hep-ph/9309227

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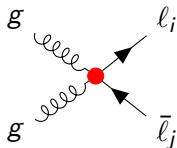
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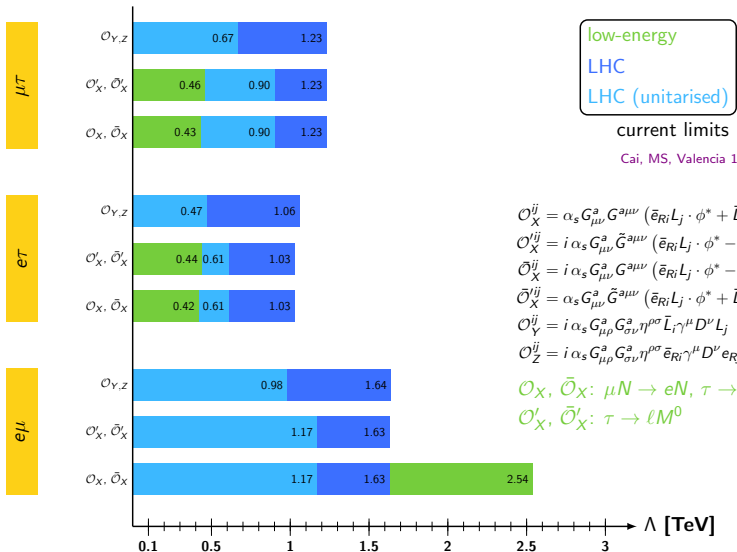
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# cLFV at hadron colliders: gluons



See also Bhattacharya et al 1802.06082 for a related analysis

**Future lepton colliders:  $e^+e^- \rightarrow \ell\ell'$**

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$$\Delta L = 0$$

complex scalar  $H_2 \sim (2, \frac{1}{2})$

$$\mathcal{L} = y_2^{ij} H_2 \bar{L}_i P_R \ell_j + h.c.$$

LH singlet vector  $H_1 \sim (1, 0)$

$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{L}_i \gamma^\mu P_L L_j$$

LH triplet vector  $H_3 \sim (3, 0)$

$$\mathcal{L} = y_3^{ij} \bar{L}_i \gamma^\mu \vec{\sigma} \cdot H_{3\mu} P_L L_j$$

right-handed vector  $H'_1 \sim (1, 0)$

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$$\Delta L = 2$$

right-handed scalar  $\Delta_1 \sim (1, 2)$

$$\mathcal{L} = \lambda_1^{ij} \Delta_1 \ell_i^T C P_R \ell_j + h.c.$$

left-handed scalar  $\Delta_3 \sim (3, 1)$

$$\mathcal{L} = -\frac{\lambda_3^{ij}}{\sqrt{2}} L_i^T C i \sigma_2 \vec{\sigma} \cdot \vec{\Delta}_3 P_L L_j + h.c.$$

vector  $\Delta_2 \sim (2, \frac{3}{2})$

$$\mathcal{L} = \lambda_2^{ij} \Delta_{2\mu\alpha} L_{i\beta}^T \gamma^\mu P_R \ell_j \epsilon_{\alpha\beta} + h.c.$$

assumption: CP conservation,  
symmetric Yukawa couplings ( $H_2, \Delta_2$ )

related work: Dev, Mohapatra, Zhang 1711.08430, also 1712.03642, 1803.11167

$$\Delta L = 0$$

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vector  $\Delta_2 \sim (2, \frac{3}{2})$

$$\mathcal{L} = \lambda_2^{ij} \textcolor{red}{\Delta}_{2\mu\alpha} L_{i\beta}^T \gamma^\mu P_R \ell_j \epsilon_{\alpha\beta} + h.c.$$

assumption: CP conservation,  
symmetric Yukawa couplings ( $H_2, \Delta_2$ )

related work: Dev, Mohapatra, Zhang 1711.08430, also 1712.03642, 1803.11167

$$\Delta L = 0$$

complex scalar  $H_2 \sim (2, \frac{1}{2})$

$$\mathcal{L} = y_2^{ij} \textcolor{red}{H}_2 \bar{L}_i P_R \ell_j + h.c.$$

LH singlet vector  $H_1 \sim (1, 0)$

$$\mathcal{L} = y_1^{ij} \textcolor{red}{H}_{1\mu} \bar{L}_i \gamma^\mu P_L L_j$$

LH triplet vector  $H_3 \sim (3, 0)$

$$\mathcal{L} = y_3^{ij} \bar{L}_i \gamma^\mu \vec{\sigma} \cdot \textcolor{red}{H}_{3\mu} P_L L_j$$

right-handed vector  $H'_1 \sim (1, 0)$

$$\mathcal{L} = y_1'^{ij} \textcolor{red}{H}'_{1\mu} \bar{\ell}_i \gamma^\mu P_R \ell_j$$

$$\Delta L = 2$$

right-handed scalar  $\Delta_1 \sim (1, 2)$

$$\mathcal{L} = \lambda_1^{ij} \textcolor{red}{\Delta}_1 \ell_i^T C P_R \ell_j + h.c.$$

left-handed scalar  $\Delta_3 \sim (3, 1)$

$$\mathcal{L} = -\frac{\lambda_3^{ij}}{\sqrt{2}} L_i^T C i \sigma_2 \vec{\sigma} \cdot \textcolor{red}{\vec{\Delta}}_3 P_L L_j + h.c.$$

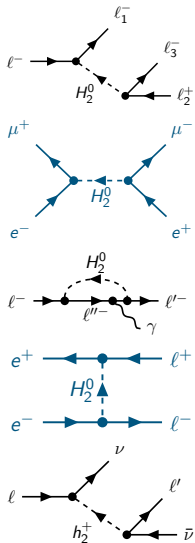
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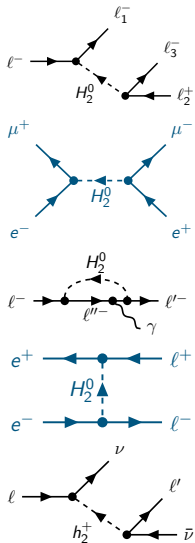
- LFV trilepton decays,  $\ell \rightarrow \ell_1 \bar{\ell}_2 \bar{\ell}_3$
- Muonium antimuonium conversion,  $\mu^+ e^- \rightarrow \mu^- e^+$
- anomalous magnetic dipole moments,  $a_\ell$
- LEP/LHC searches
- lepton flavour non-universality,  $\ell \rightarrow \ell' \nu \bar{\nu}$
- electroweak precision observables



Future sensitivity improvements at e.g. Belle 2, Mu3E, ...



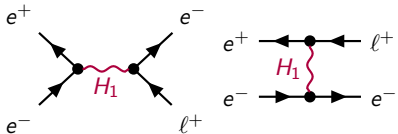
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Future sensitivity improvements at e.g. Belle 2, Mu3E, ...

# Off-shell production $H_{1\mu}$ : $e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp)$ [Li,MS 1809.07924]

$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{L}_i \gamma^\mu P_L L_j$$



Basic cuts:  $p_T > 10$  GeV and  $|\eta| < 2.5$

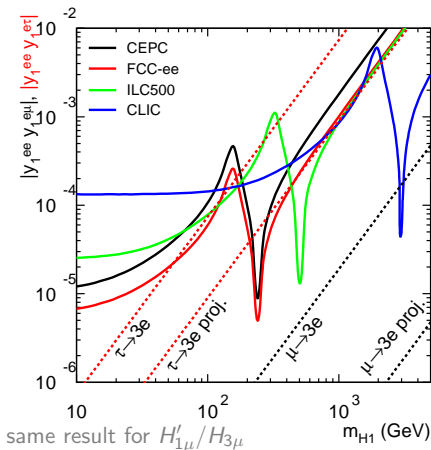
Four collider configurations:

CEPC:  $5 \text{ ab}^{-1}$  at 240 GeV

FCC-ee:  $16 \text{ ab}^{-1}$  at 240 GeV

ILC500:  $4 \text{ ab}^{-1}$  at 500 GeV

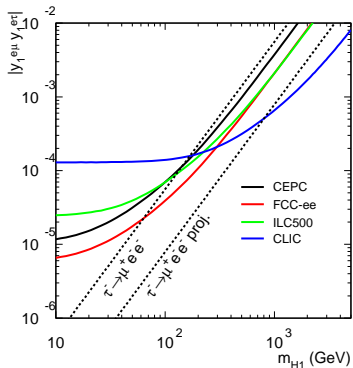
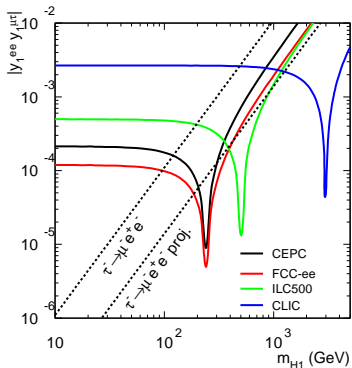
CLIC:  $5 \text{ ab}^{-1}$  at 3 TeV



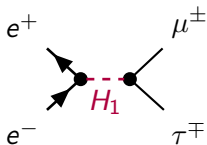
$\tau$  efficiency not included in figure

60%  $\tau$  eff.  $\Rightarrow$  77% sensitivity reduction for 1  $\tau$

$$H_{1\mu}: e^+e^- \rightarrow \mu^\pm\tau^\mp \quad [\text{Li,MS 1809.07924}]$$



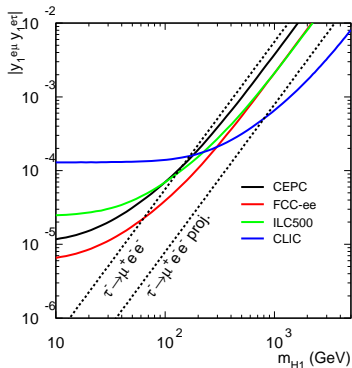
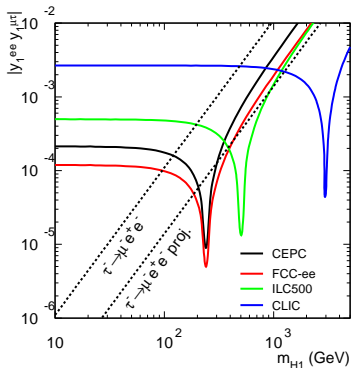
rel. couplings  $|y_1^{ee} y_1^{\mu\tau}|$



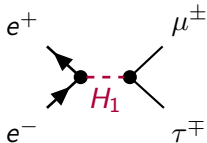
rel. couplings  $|y_1^{e\mu} y_1^{e\tau}|$



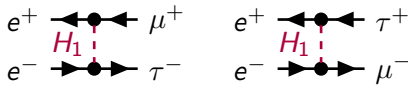
$$H_{1\mu}: e^+e^- \rightarrow \mu^\pm\tau^\mp \quad [\text{Li,MS 1809.07924}]$$



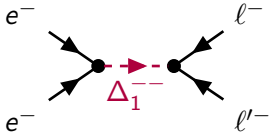
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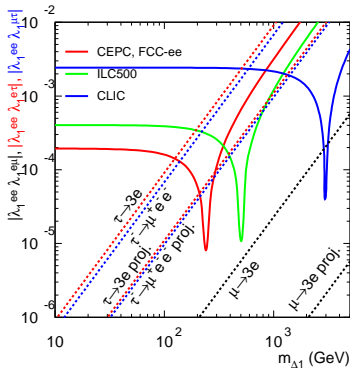


# Same-sign lepton collider - $\Delta_1$ : $e^-e^- \rightarrow \ell^- \ell'^-$ [Li,MS 1809.07924]



relevant couplings

$$|\lambda_1^{ee} \lambda_1^{e\ell}| \text{ and } |\lambda_1^{ee} \lambda_1^{\mu\tau}|$$



same centre of mass energies

smaller integrated luminosity

$$\mathcal{L} = 500 \text{ fb}^{-1}$$

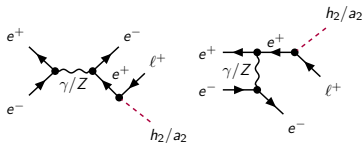
## Future lepton colliders:

$$e^+e^- \rightarrow \ell\ell' + X$$

---

# On-shell production $H_2$ : $e^+e^- \rightarrow e^\pm \mu^\mp + h_2/a_2$ [Li,MS 1907.06963]

$$\mathcal{L} = y_2^{ij} H_{2\alpha} \bar{L}_i^\alpha P_R \ell_j + h.c.$$



Cuts:  $p_T > 10$  GeV and  $|\eta| < 2.5$   
100%  $h/a$  reconstruction efficiency

Five collider configurations:

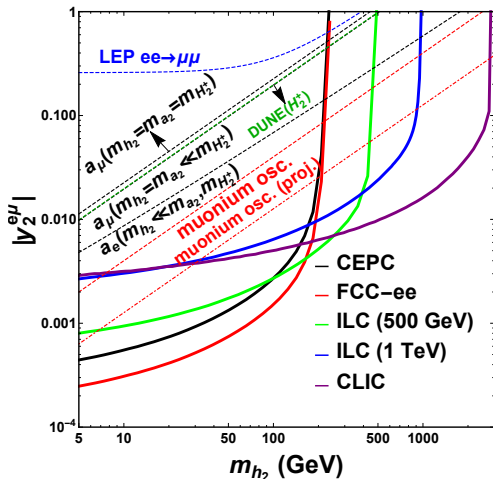
CEPC:  $5 \text{ ab}^{-1}$  at 240 GeV

FCC-ee:  $16 \text{ ab}^{-1}$  at 240 GeV

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ILC (1TeV):  $1 \text{ ab}^{-1}$  at 1 TeV

CLIC:  $5 \text{ ab}^{-1}$  at 3 TeV

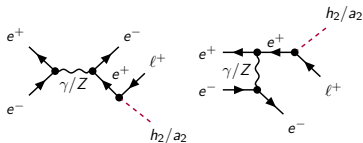


$\tau$  efficiency not included in figure

60%  $\tau$  eff.  $\Rightarrow$  77% sensitivity reduction for 1  $\tau$

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Cuts:  $p_T > 10$  GeV and  $|\eta| < 2.5$   
10%  $h/a$  reconstruction efficiency

Five collider configurations:

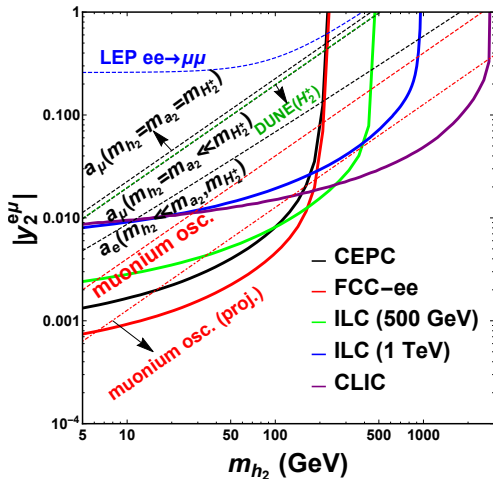
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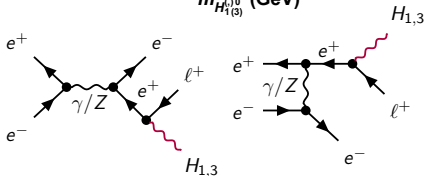
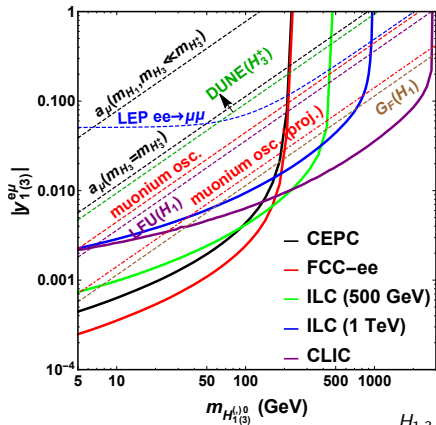


$\tau$  efficiency not included in figure

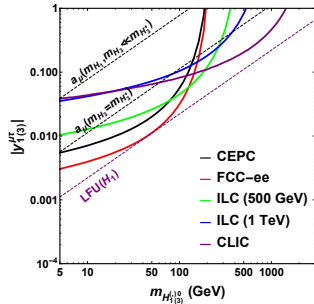
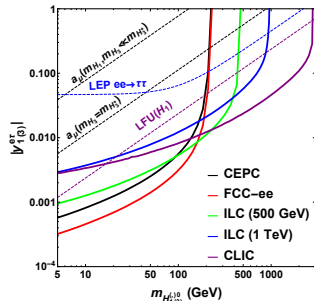
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# On-shell production $H_{1,3\mu}$ : $e^+e^- \rightarrow \ell^\pm \ell^\mp + H_{1,3}$ [Li,MS 1907.06963]



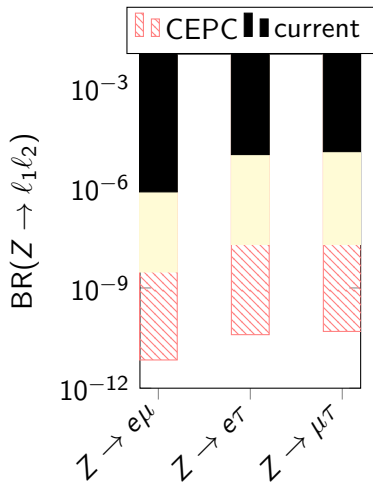
$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{L}_i \gamma^\mu P_L L_j + y_3^{ij} \bar{L}_i \gamma^\mu \vec{\sigma} \cdot H_{3\mu} P_L L_j$$



## Other searches

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# Searches for cLFV in decays of $Z$ and Higgs boson

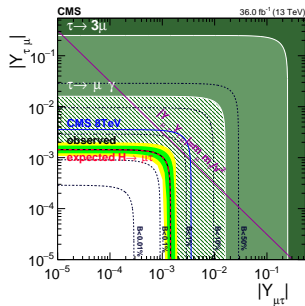


$Z \rightarrow e\mu$ : ATLAS 1408.5774, CMS EXO-13-005

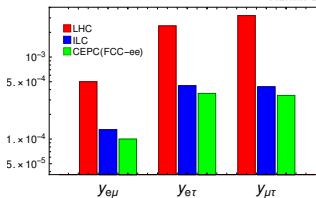
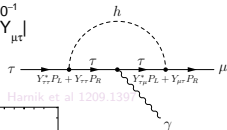
$Z \rightarrow \ell\tau$ : DELPHI ( $\mu\tau$ ), OPAL ( $e\tau$ )

ATLAS, 13 TeV,  $36.1 \text{ fb}^{-1}$  1804.09568

almost same sensitivity for  $\mu\tau$



CMS 1712.07173



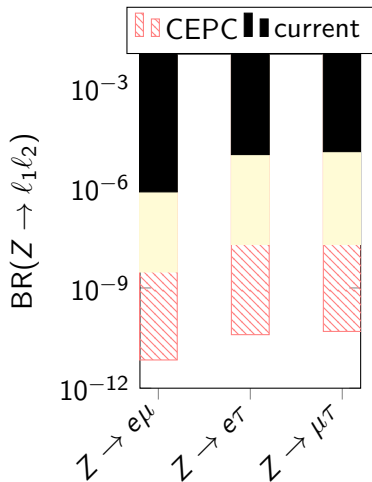
Qin et al 1711.07243

LHC CMS-PH-13-005, CMS EXO-13-005

ILC  $\sqrt{s} = 250 \text{ GeV}$ , 4 polarizations,  $\mathcal{L} = 2 \text{ ab}^{-1}$

CEPC  $\sqrt{s} = 240 \text{ GeV}$ ,  $\mathcal{L} = 5 \text{ ab}^{-1}$

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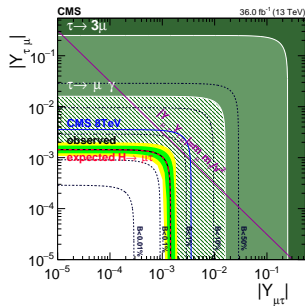


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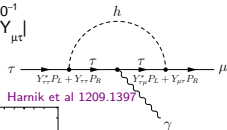
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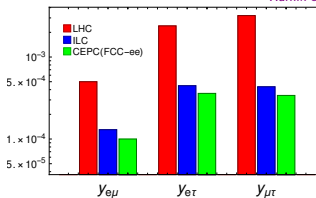
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CMS 1712.07173



Hamik et al 1209.1397



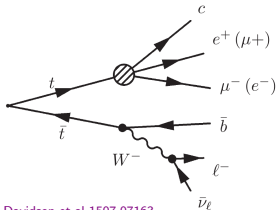
Qin et al 1711.07243

LHC CMS-PAS-HIG-16-005, CMS 1607.03561

ILC  $\sqrt{s} = 250 \text{ GeV}$ , 4 polarizations,  $\mathcal{L} = 2 \text{ ab}^{-1}$

CEPC  $\sqrt{s} = 240 \text{ GeV}$ ,  $\mathcal{L} = 5 \text{ ab}^{-1}$

# Searches for cLFV in decays of top and heavy resonance



Davidson et al 1507.07163

cross section  $\sigma \propto \sum_{X,Y} |\epsilon_{XY}|^2$

Main backgrounds:

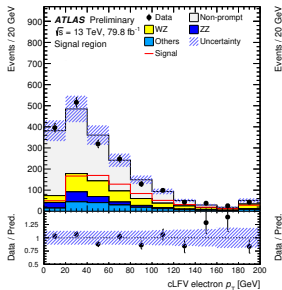
- $t\bar{t}$  with non-prompt lepton
- $Z$  + jets

Multi-variate analysis w/ 13 var's using BDT

observed limit

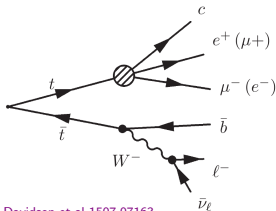
$$BR(t \rightarrow \ell\ell'[e\mu]q) < 1.86[6.6] \times 10^{-5}$$

$\rightarrow |\epsilon| \lesssim 0.1$ , more stringent for  $t \rightarrow \tau + X$



ATLAS-CONF-2018-044

# Searches for cLFV in decays of top and heavy resonance



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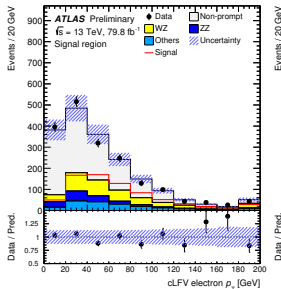
Main backgrounds:

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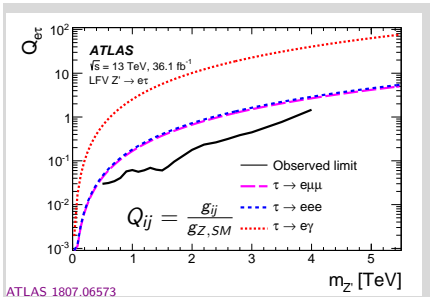
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ATLAS-CONF-2018-044



ATLAS 1807.06573

## Conclusions

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# Conclusions

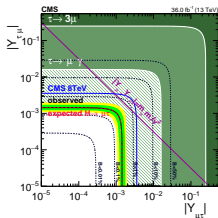
colliders complementary way to search for charged LFV

$\mu \leftrightarrow e$  flavour: stringent limits from low-energy precision exp.

$\tau \leftrightarrow \ell$  flavour complementary sensitivity at colliders

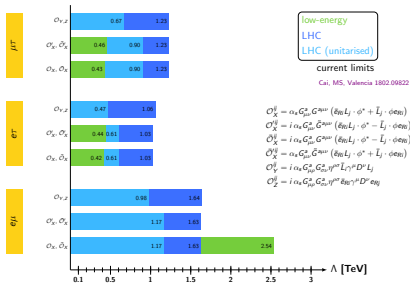
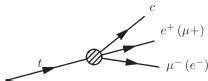
colliders test more Lorentz structures

best for operators which are difficult to constrain at low energy



cLFV Higgs decay

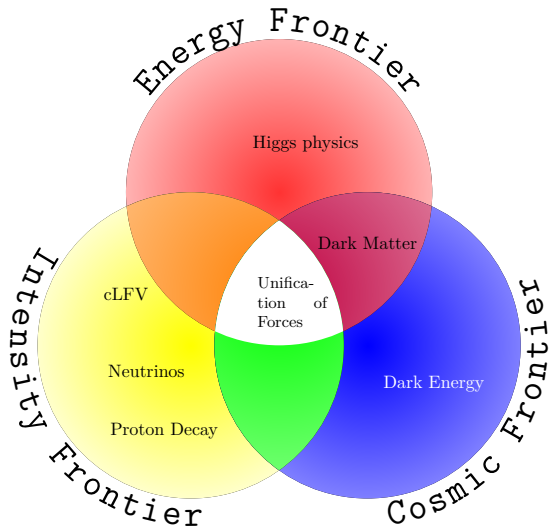
cLFV top decay



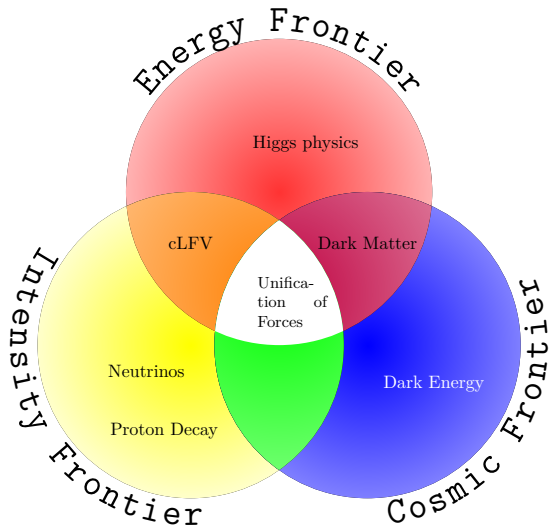
cLFV scattering with initial state gluons



## Conclusions cont.



## Conclusions cont.



# Neutrino masses

## Classification in terms of effective $\Delta L = 2$ operators

Babu, Leung hep-ph/0106054; deGouvea, Jenkins 0708.1344 Bonnet, Hernandez, Ota, Winter 0907.3143

→ no information on  $\Delta L = 0$  processes

## Systematic construction of models

Angel, Rodd, Volkas 1212.5862; Cai, Clarke, MS, Volkas 1308.0463; Gargalionis, Volkas (in prep)

Bonnet, Hirsch, Ota, Winter 1204.5862; Aristizabal Sierra, Degee, Dorame, Hirsch 1411.7038; Cepedello, Fonseca, Hirsch 1807.00629

Volkas (NuFact 2019): "exploding!  $\Delta L = 2$  operators" ... "1000s of models"

→ too many models!

## Hybrid scheme Herrero-Garcia, MS 1903.10552

- SM + one particle with  $L \neq 0$  and renormalizable  $\Delta L = 0$  op.
- add  $\Delta L = 2$  operator with this particle
- neutrino masses in terms of both operators
- $L$ -conserving pheno in terms of  $\Delta L = 0$  operator

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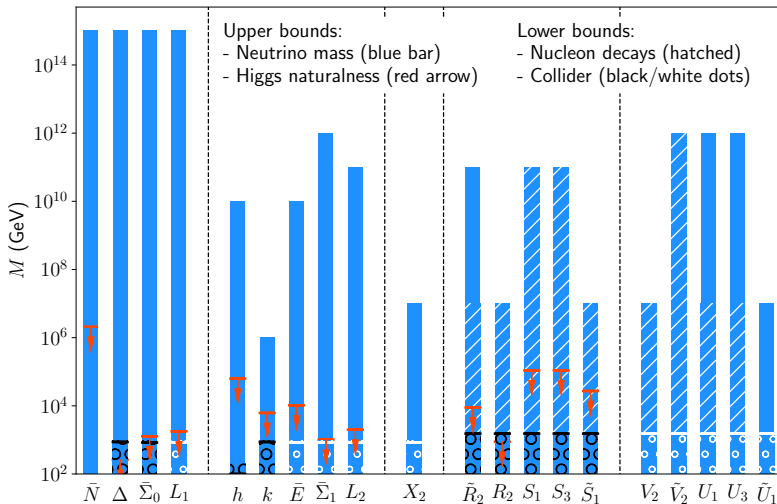
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# Mass range for lightest new particles [Herrero-Garcia, MS 1903.10552]



# TeV Particle Astrophysics 2019

Sydney, 2 - 6 Dec, 2019



Satellite meetings:

Second Sydney spring school, UNSW, 26-29 Nov 2019

pre-TeVPA CTA workshop, University of Adelaide, 28-29 Nov 2019

Registration and further details under <https://indico.cern.ch/event/828038/>

LOC: Archil Kobakhidze (USyd), Csaba Balazs (Monash), Nicole Bell (UMelb), Celine Boehm (USyd), Roland Crocker (ANU), Paul Jackson (Adelaide), Geraint Lewis (USyd), Tara Murphy (USyd), Gavin Rowell (Adelaide), Martin White (Adelaide), Yvonne Wong (UNSW)

**Backup slides**



# Scalar Operators

$$\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha) \qquad \mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell) \epsilon_{\alpha\beta} (\bar{Q}^\beta u)$$

Relevant Wilson coefficients  $\Xi^{u,d}$  of SM EFT

$$- \mathcal{L} = \Xi_{ij,kk}^d (\mathcal{Q}_{ledq})_{ij,kk} + \Xi_{ij,kk}^u (\mathcal{Q}_{lequ}^{(1)})_{ij,kk} + \text{h.c.} .$$

Effective four fermion Lagrangian

$$\begin{aligned} \mathcal{L}_{4f} = & \Xi_{ij,kl}^{Cd} (\bar{\nu}_{Li} \ell_{Rj}) (\bar{d}_{Rk} u_{Li}) + \Xi_{ij,kl}^{Nd} (\bar{\ell}_{Li} \ell_{Rj}) (\bar{d}_{Rk} d_{Li}) \\ & + \Xi_{ij,kl}^{Cu} (\bar{\nu}_{Li} \ell_{Rj}) (\bar{d}_{Lk} u_{Rl}) + \Xi_{ij,kl}^{Nu} (\bar{\ell}_{Li} \ell_{Rj}) (\bar{u}_{Lk} u_{Rl}) . \end{aligned}$$

We do not consider top quark because of different phenomenology.

# Scalar Operators

$$\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha) \quad \mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell) \epsilon_{\alpha\beta} (\bar{Q}^\beta u)$$

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Effective four fermion Lagrangian

$$\begin{aligned} \mathcal{L}_{4f} = & \Xi_{ij,kl}^{Cd} (\bar{\nu}_{Li} \ell_{Rj}) (\bar{d}_{Rk} u_{Li}) + \Xi_{ij,kl}^{Nd} (\bar{\ell}_{Li} \ell_{Rj}) (\bar{d}_{Rk} d_{Li}) \\ & + \Xi_{ij,kl}^{Cu} (\bar{\nu}_{Li} \ell_{Rj}) (\bar{d}_{Lk} u_{Rl}) + \Xi_{ij,kl}^{Nu} (\bar{\ell}_{Li} \ell_{Rj}) (\bar{u}_{Lk} u_{Rl}) . \end{aligned}$$

Thus the most general four fermion coefficients are

$$\begin{aligned} \Xi_{ij,kl}^{Nd} &= U_{ii'}^{\ell*} V_{lk}^d \Xi_{ij,kk}^d & \Xi_{ij,kl}^{Cd} &= U_{ii'}^{\nu*} V_{lk}^u \Xi_{i'j,kk}^d \\ \Xi_{ij,kl}^{Nu} &= -U_{ii'}^{\ell*} V_{kl}^{u*} \Xi_{ij,ll}^u & \Xi_{ij,kl}^{Cu} &= U_{ii'}^{\nu*} V_{kl}^{d*} \Xi_{i'j,ll}^u \end{aligned}$$

In general there is quark flavour violation.

We do not consider top quark because of different phenomenology.

# Scalar Operators

$$\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha) \quad \mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell) \epsilon_{\alpha\beta} (\bar{Q}^\beta u)$$

Relevant Wilson coefficients  $\Xi^{u,d}$  of SM EFT

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Choose basis in which charged lepton mass matrix is diagonal as well as  $\Xi_{ij,kk}^{N?}$

$$\begin{aligned} \Xi_{ij,kl}^{Nd} &= \delta_{kl} \Xi_{ij,kk}^d & \Xi_{ij,kl}^{Cd} &= U_{ii'}^* V_{kl}^* \Xi_{i'j,kk}^d \\ \Xi_{ij,kl}^{Nu} &= -\delta_{kl} \Xi_{ij,kk}^u & \Xi_{ij,kl}^{Cu} &= U_{ii'}^* V_{kl}^* \Xi_{i'j,ll}^u \end{aligned}$$

$\Rightarrow$  No tree-level FCNC processes.

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# Scalar Operators

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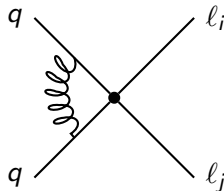
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# Renormalization Group Corrections

- Main effect are **QCD corrections**



- Following the standard discussion at NLO

Buchalla, Buras, Lautenbacher hep-ph/9512380

$$\Xi(\mu) = \Xi(\mu_0) \left( \frac{\alpha_s(\mu)}{\alpha_s(\mu_0)} \right)^{\frac{\gamma_0}{2\beta_0}}$$

with coefficients

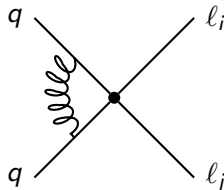
$$\beta_0 = 11 - 2n_F/3 \quad \text{and} \quad \gamma_0 = 6C_2(3) = 8$$

- Wilson coefficients become larger at smaller scales.

⇒ **Increases reach of precision experiments**

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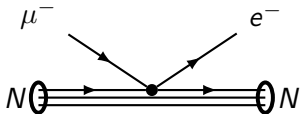
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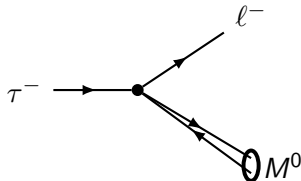
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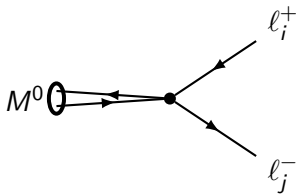
# Precision Experiments



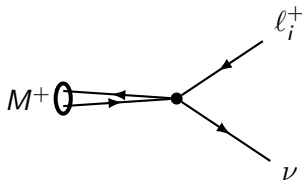
$\mu - e$  conversion in nuclei



$\tau \rightarrow l M^0$



$M^0 \rightarrow \ell_i^+ \ell_j^-$

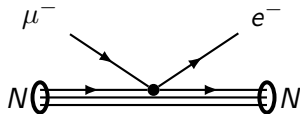


$M^+ \rightarrow \ell_i^+ \nu$

# $\mu - e$ Conversion

- Agnostic about mediation mechanism
- Following discussion in

Gonzalez, Gutsche, Helo, Kovalenko, Lyubovitskij, Schmidt 1303.0596



Dimensionless  $\mu - e$  conversion rate

$$R_{\mu e}^{(A,Z)} \equiv \frac{\Gamma(\mu^- + (A, Z) \rightarrow e^- + (A, Z))}{\Gamma(\mu^- + (A, Z) \rightarrow \nu_\mu + (A, Z - 1))}$$

with muon conversion rate

$$\Gamma(\mu^- + (A, Z) \rightarrow e^- + (A, Z)) = \left| \Xi_{ij,kl}^{Nu,Nd} \right|^2 \times \mathcal{F} \times \frac{p_e E_e (\mathcal{M}_p + \mathcal{M}_n)^2}{2\pi}$$

$\mathcal{F}$  depends on mediation mechanism

No dependence on phase of  $\Xi$  if there is only one operator.

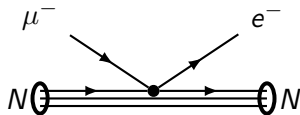
Strongest limit for first generation quarks,  
but non-negligible for other quarks if pure direct nuclear mediation



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	$^{48}\text{Ti}$	$^{197}\text{Au}$	$^{208}\text{Pb}$
$R_{\mu e}^{\text{max}}$	$4.3 \times 10^{-11}$	$7.0 \times 10^{-13}$	$4.6 \times 10^{-11}$
$\bar{u}u$	1100 [870]	2100 [1700]	760 [610]
$\bar{d}d$	1100 [930]	2200 [1900]	780 [680]
$\bar{s}s$	480 [-]	950 [-]	340 [-]
$\bar{c}c$	150 [-]	290 [-]	110 [-]
$\bar{b}b$	84 [-]	170 [-]	61 [-]

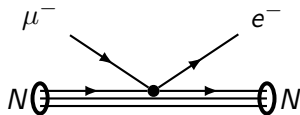
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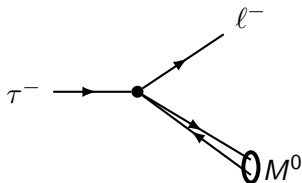
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Direct nuclear mediation [Meson mediation]

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# LFV Semileptonic $\tau$ Decays

- Only light quarks u,d,s
- Weak dependence on phase
- $f_0$ :  $\varphi_m$  parameterises quark content
- Quark FCNC parameterised by  $\lambda$



$$\Xi_{ij,kl}^u = \lambda \Xi_{ij,ll}^u V_{kl} \quad \Xi_{ij,kl}^d = \lambda \Xi_{ij,kk}^d V_{kl}$$

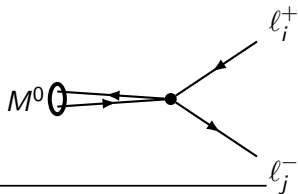
decay	$\text{Br}_i^{\text{max}}$	cutoff scale $\Lambda$ [TeV]		
		$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$
$\tau^- \rightarrow e^- \pi^0$	$8.0 \times 10^{-8}$	10	10	-
$\tau^- \rightarrow e^- \eta$	$9.2 \times 10^{-8}$	34	34	7.9
$\tau^- \rightarrow e^- \eta'$	$1.6 \times 10^{-7}$	42	42	12
$\tau^- \rightarrow e^- K_S^0$	$2.6 \times 10^{-8}$	-	$7.8 \sqrt{\lambda}$	$7.8 \sqrt{\lambda}$
$\tau^- \rightarrow e^- (f_0(980) \rightarrow \pi^+ \pi^-)$	$3.2 \times 10^{-8}$	$13 \sqrt{\sin \varphi_m}$	$13 \sqrt{\sin \varphi_m}$	$16 \sqrt{\cos \varphi_m}$
$\tau^- \rightarrow \mu^- \pi^0$	$1.1 \times 10^{-7}$	9.0 – 9.6	9.0 – 9.6	-
$\tau^- \rightarrow \mu^- \eta$	$6.5 \times 10^{-8}$	36 – 38	36 – 38	8.4 – 8.9
$\tau^- \rightarrow \mu^- \eta'$	$1.3 \times 10^{-7}$	42 – 46	42 – 46	12 – 13
$\tau^- \rightarrow \mu^- K_S^0$	$2.3 \times 10^{-8}$	-	$(7.8 - 8.3) \sqrt{\lambda}$	$(7.8 - 8.3) \sqrt{\lambda}$
$\tau^- \rightarrow \mu^- (f_0(980) \rightarrow \pi^+ \pi^-)$	$3.4 \times 10^{-8}$	$(12 - 14) \sqrt{\sin \varphi_m}$	$(12 - 14) \sqrt{\sin \varphi_m}$	$(15 - 16) \sqrt{\cos \varphi_m}$

# Leptonic Neutral Meson Decays $M^0 \rightarrow \ell_i^+ \ell_j^-$

Quark FCNC parameterised by  $\lambda$


$$\Xi_{ij,kl}^u = \lambda \Xi_{ij,ll}^u V_{kl} \quad \Xi_{ij,kl}^d = \lambda \Xi_{ij,kk}^d V_{kl}$$

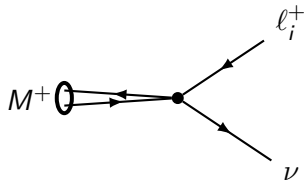
For  $\lambda = 0$  only constraints from  $\pi^0, \eta^{(\prime)}$  decays





























decay	$\text{Br}_i^{\text{max}}$	cutoff scale $\Lambda$ [TeV]				
		$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$	$\Xi_{ij,cc}^u$	$\Xi_{ij,bb}^d$
$\pi^0 \rightarrow \mu^+ e^-$	$3.8 \times 10^{-10}$	2.2	2.2	-	-	-
$\pi^0 \rightarrow \mu^- e^+$	$3.4 \times 10^{-9}$	1.2	1.2	-	-	-
$\pi^0 \rightarrow \mu^+ e^- + \mu^- e^+$	$3.6 \times 10^{-10}$	2.6	2.6	-	-	-
$\eta \rightarrow \mu^+ e^- + \mu^- e^+$	$6 \times 10^{-6}$	0.52	0.52	0.12	-	-
$\eta' \rightarrow e\mu$	$4.7 \times 10^{-4}$	0.091	0.091	0.026	-	-
$K_L^0 \rightarrow e^\pm \mu^\mp$	$4.7 \times 10^{-12}$	-	$86 \sqrt{\lambda}$	$86 \sqrt{\lambda}$	-	-
$D^0 \rightarrow e^\pm \mu^\mp$	$2.6 \times 10^{-7}$	$6.4 \sqrt{\lambda}$	-	-	$6.4 \sqrt{\lambda}$	-
$B^0 \rightarrow e^\pm \mu^\mp$	$2.8 \times 10^{-9}$	-	$10 \sqrt{\lambda}$	-	-	$6.6 \sqrt{\lambda}$
$B^0 \rightarrow e^\pm \tau^\mp$	$2.8 \times 10^{-5}$	-	$0.97 \sqrt{\lambda}$	-	-	$0.62 \sqrt{\lambda}$
$B^0 \rightarrow \mu^\pm \tau^\mp$	$2.2 \times 10^{-2}$	-	$0.18 \sqrt{\lambda}$	-	-	$0.12 \sqrt{\lambda}$

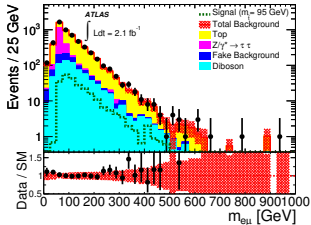
# Leptonic Charged Meson Decays $M^+ \rightarrow \ell_i^+ \nu$

- $R_M = \frac{\text{Br}(M^+ \rightarrow e^+ \nu)}{\text{Br}(M^+ \rightarrow \mu^+ \nu)}$
- Theoretical error for  $R_\pi$  ( $R_K$ ) about 5%
- Improvement by factor 20 (2) possible
-  indicates constraints
- Second index of  $\Lambda$  corresponds to charged lepton

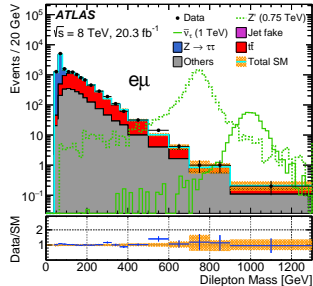


decay	constraint	cutoff scale $\Lambda$ [TeV]		Wilson coefficients				
		$\Lambda_{\mu e, e\mu, e\tau}$	$\Lambda_{\tau e, \tau\mu, \mu\tau}$	$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$	$\Xi_{ij,cc}^u$	$\Xi_{ij,bb}^d$
$R_\pi$	$R_\pi^{\text{exp}} \pm 5\%$	25 – 280	25 – 260			-	-	-
$R_K$	$R_K^{\text{exp}} \pm 5\%$	24 – 160	24 – 150		-		-	-
$\text{Br}(D^+ \rightarrow e^+ \nu)$	$< 8.8 \times 10^{-6}$	2.8 – 2.9	2.9	-		-		-
$\text{Br}(D_s^+ \rightarrow e^+ \nu)$	$< 8.3 \times 10^{-5}$	3.2 – 3.3	3.2 – 3.3	-	-			-
$\text{Br}(B^+ \rightarrow e^+ \nu)$	$< 9.8 \times 10^{-7}$	2.0	2.0		-	-	-	
$\text{Br}(\pi^+ \rightarrow \mu^+ \nu)$	$\text{Br}^{\text{exp}} \pm 5\%$	1.9 – 7.4	1.9 – 9.4			-	-	-
$\text{Br}(K^+ \rightarrow \mu^+ \nu)$	$\text{Br}^{\text{exp}} \pm 5\%$	1.7 – 5.8	1.7 – 7.4		-		-	-
$\text{Br}(D^+ \rightarrow \mu^+ \nu)$	$(3.82 \pm 0.33) \times 10^{-4}$	1.1 – 2.7	1.1 – 3.4	-		-		-
$\text{Br}(D_s^+ \rightarrow \mu^+ \nu)$	$(5.56 \pm 0.25) \times 10^{-3}$	1.3 – 4.3	1.3 – 5.3	-	-			-
$\text{Br}(B^+ \rightarrow \mu^+ \nu)$	$< 1.0 \times 10^{-6}$	1.9 – 2.7	1.7 – 3.0		-	-	-	
$\text{Br}(D^+ \rightarrow \tau^+ \nu)$	$< 1.2 \times 10^{-3}$	0.21 – 0.78	0.23 – 0.73	-		-		-
$\text{Br}(D_s^+ \rightarrow \tau^+ \nu)$	$(5.54 \pm 0.24) \times 10^{-2}$	0.33 – 1.2	0.33 – 1.1	-	-			-
$\text{Br}(B^+ \rightarrow \tau^+ \nu)$	$(1.14 \pm 0.27) \times 10^{-4}$	0.49 – 1.3	0.49 – 1.2		-	-	-	

# SM Background



ATLAS 7TeV 1205.0725



ATLAS 8TeV 1503.04430

- **Main backgrounds:**  $t\bar{t}$ ,  $WW$ ,  $Z/\gamma^* \rightarrow \tau\tau$

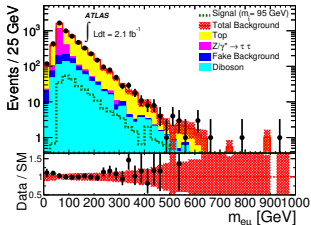
also  $W/Z$  plus jets,  $WZ/ZZ$ , single top and  $W/Z + \gamma$

⇒ Efficiently reduced in exclusive 7 TeV analysis  
by rejecting jets and  $E_T^{miss} < 20$  GeV

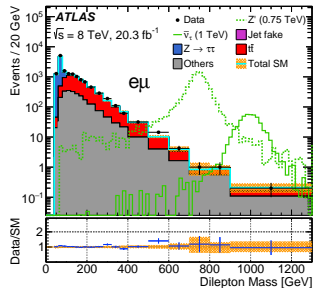
- Modelling of main background agrees with ATLAS
- Fake background estimated from data

⇒ Use background from ATLAS publications

# SM Background



ATLAS 7TeV 1205.0725



ATLAS 8TeV 1503.04430

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- Modelling of main background **agrees with ATLAS**
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# Selection Criteria

Same selection criteria as in ATLAS 7 and 8 TeV analyses.

- oppositely charged leptons
- Electrons:  $E_T > 25$  GeV,  $|\eta| < 1.37$  or  $1.52 < |\eta| < 2.47$ , tight identification criteria
- Muons:  $p_T > 25$  GeV,  $|\eta| < 2.4$
- Tau:  $E_T > 25$  GeV,  $0.03 < |\eta| < 2.47$
- Lepton isolation: scalar sum of lepton  $p_T$  within cone of  $\Delta R = 0.2(0.4)$  is less than 10% (6%) of lepton  $p_T$  for 7 (8) TeV search
- Jets reconstructed anti- $k_T$  algorithm with radius parameter 0.4
- 7 TeV analysis: jets rejected if  $p_T > 30$  GeV or  $E_T^{miss} < 25$  GeV
- Invariant mass of lepton pair:  $> 100(200)$  GeV in 7(8) TeV analysis
- azimuthal angle difference  $\Delta\phi > 3(2.7)$  in 7 (8) TeV analysis

## 14 TeV projection

Same as 7 TeV exclusive analysis and  $p_T(\ell) > 300$  GeV and  $E_T^{miss} < 20$  GeV



# Limits from LHC on Cutoff Scale in TeV

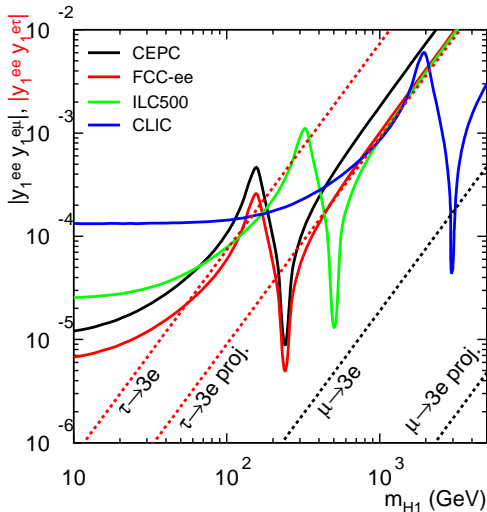
$\bar{q}q$ \ $\bar{\ell}_i \ell_j$	$\bar{e}\mu$			$\bar{e}\tau$	$\bar{\mu}\tau$
	7 TeV	8 TeV	14 TeV	8 TeV	8 TeV
$\bar{u}u$	2.6	2.9	8.9	2.4	2.2
$\bar{d}d$	2.3	2.3	8.0	2.1	1.9
$\bar{s}s$	1.1	1.4	4.0	0.95	0.88
$\bar{c}c$	0.97	1.3	3.6	0.82	0.78
$\bar{b}b$	0.74	1.0	2.7	0.63	0.61

- 8 TeV analysis gives only a slight improvement compared to 7 TeV despite 10 times more data because of large background
- $e\tau$  and  $\mu\tau$  limits weaker than  $e\mu$  because of low  $\tau$ -tagging rate and higher fake background
- 14 TeV projection: same search strategy as 7 TeV exclusive search

# cLFV D8 operator with 2 gluons and 2 leptons

process	exp. limit	operator	$\Lambda$ [TeV]
$e\mu$			
$\text{Br}(\mu^- {}^{48}_{22}\text{Ti} \rightarrow e^- {}^{48}_{22}\text{Ti})$	$< 4.3 \times 10^{-12}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	2.11
$\text{Br}(\mu^- {}^{197}_{79}\text{Au} \rightarrow e^- {}^{197}_{79}\text{Au})$	$< 7 \times 10^{-13}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	2.54
$e\tau$			
$\text{Br}(\tau^+ \rightarrow e^+ \pi^+ \pi^-)$	$< 2.3 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.42
$\text{Br}(\tau^- \rightarrow e^- K^+ K^-)$	$< 3.4 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.37
$\text{Br}(\tau^- \rightarrow e^- \eta)$	$< 9.2 \times 10^{-8}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.40
$\text{Br}(\tau^- \rightarrow e^- \eta')$	$< 1.6 \times 10^{-7}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.44
$\mu\tau$			
$\text{Br}(\tau^- \rightarrow \mu^- \pi^+ \pi^-)$	$< 2.1 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.43
$\text{Br}(\tau^- \rightarrow \mu^- K^+ K^-)$	$< 4.4 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.36
$\text{Br}(\tau^- \rightarrow \mu^- \eta)$	$< 6.5 \times 10^{-8}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.42
$\text{Br}(\tau^- \rightarrow \mu^- \eta')$	$< 1.3 \times 10^{-7}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.46

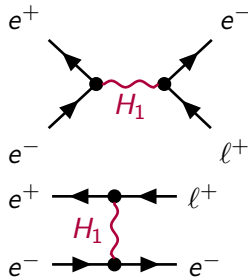
$$H_{1\mu}: e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp)$$



$\tau$  efficiency not included in figure

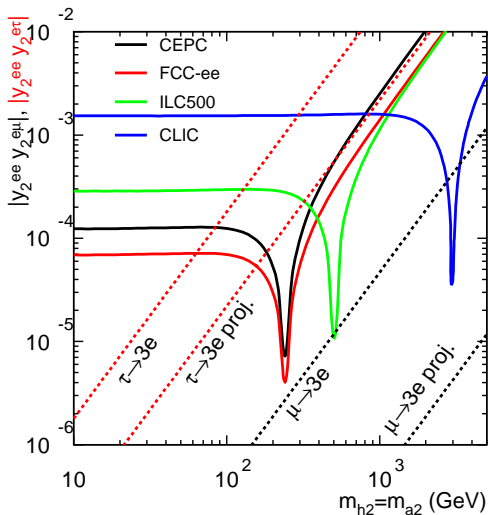
60%  $\tau$  eff.  $\Rightarrow$  77% (60%) sensitivity reduction for 1 (2)  $\tau$  leptons

$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{\ell}_i \gamma^\mu P_L \ell_j$$

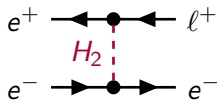
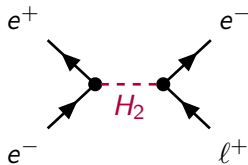


same result for  
right-handed  $H'_{1\mu}$

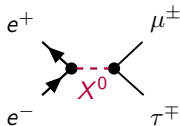
$$H_2: e^+e^- \rightarrow e^\pm \mu^\mp (e^\pm \tau^\mp)$$



$$\mathcal{L} = y_2^{ij} H_2^0 \bar{\ell}_i P_R \ell_j + h.c.$$

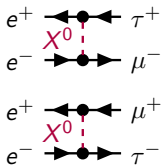
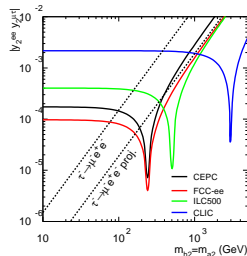
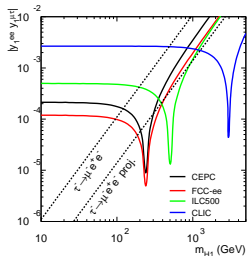


$$H_{1\mu}, H_2: e^+e^- \rightarrow \mu^\pm\tau^\mp$$



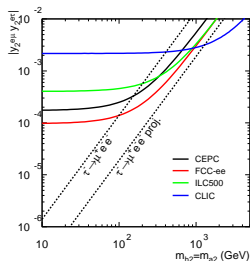
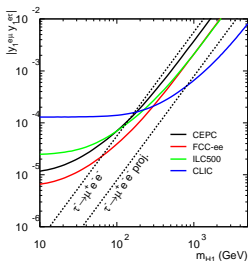
rel. couplings

$$|y^{ee}y^{\mu\tau}|$$

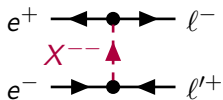


rel. couplings

$$|y^{e\mu}y^{e\tau}|$$

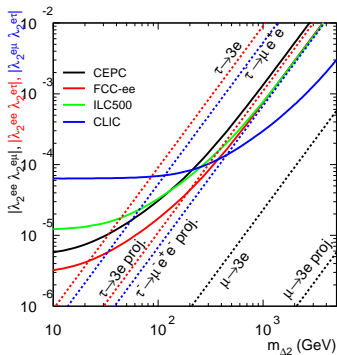
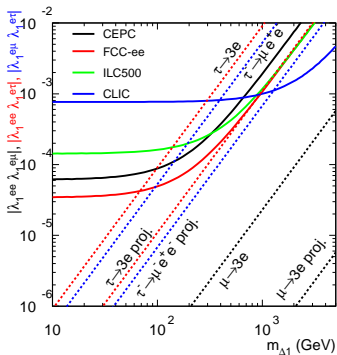


$$\Delta_1, \Delta_{2\mu}: e^+e^- \rightarrow \ell^+\ell'^-$$

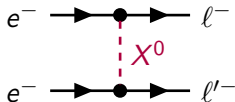


relevant couplings

$$|\lambda^{ee}\lambda^{e\ell}| \text{ and } |\lambda^{e\mu}\lambda^{e\tau}|$$

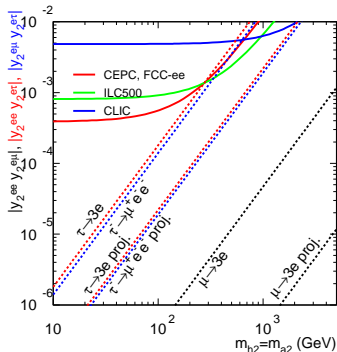
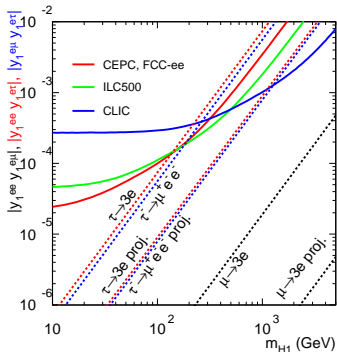


$$H_{1\mu}, H_2: e^-e^- \rightarrow \ell^- \ell'^-$$

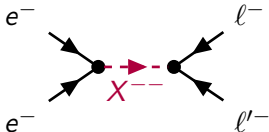


relevant couplings

$$|y^{ee}y^{e\ell}| \text{ and } |y^{e\mu}y^{e\tau}|$$



$$\Delta_1, \Delta_{2\mu}: e^-e^- \rightarrow \ell^- \ell'^-$$



relevant couplings

$$|\lambda^{ee}\lambda^{e\ell}| \text{ and } |\lambda^{ee}\lambda^{\mu\tau}|$$

