

# Exam 4 - Rotational Dynamics

Date: \_\_\_\_ / \_\_\_\_ / \_\_\_\_

Class Number: PHYS 1061 H002 Instructor: Michael Haas

Name: \_\_\_\_\_

Please read and follow all instructions carefully. Use the back of the sheet if necessary.

Indefinite evaluation of  $\int (x + 3x^2)dx = x^3 + \frac{x^2}{2} + C$

Score: \_\_\_\_\_ / 42 + Bonus: \_\_\_\_\_ / 6 = Total: \_\_\_\_\_ / 42 || Final: \_\_\_\_\_ % -> [A, B, C, D, F]

## Problem #1 (3 points)

Two wheels, A and B, have the same shape and size, but wheel A has half the mass of wheel B. How do the moments of inertia (around the axis of symmetry) of the two wheels relate to each other?

- A.  $I_A = I_B$
- B.  $I_A = 2I_B$
- C.  $I_A = 4I_B$
- D.  $I_A = \frac{1}{2}I_B$
- E.  $I_A = \frac{1}{4}I_B$

## Problem #2 (3 points)

Two wheels (same mass, same radius, same width) are rolled without slipping down an incline. Wheel A is a solid disk and wheel B is a hoop. Which wheel reaches the bottom first?

- A. Wheel A
- B. Wheel B
- C. They reach the bottom at the same time
- D. It depends on the incline angle

## Problem #3 (3 points)

A solid sphere and a solid cube are raced down a slide. The sphere rolls without slipping and the box slides without friction. Which object reaches the bottom first?

- A. Sphere
- B. Cube
- C. They reach the bottom at the same time
- D. It depends on the incline angle

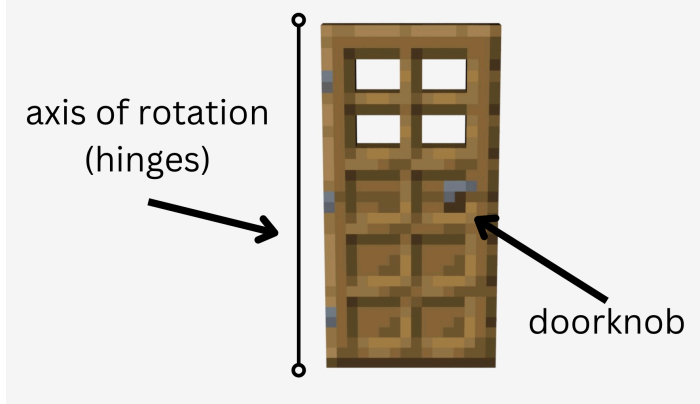
## Bonus #4 (3 points)

Will you vote tomorrow? (no wrong answer)

yes | no | maybe | I don't know | other | none of your business

### Problem #5 (3 points)

Steve is pushing a door open (applying a force into the page at the doorknob), what direction is the torque applied relative to the axis of rotation (the hinges).



- A. Into the page ( $-z$ )
- B. Out of the page ( $+z$ )
- C. Up ( $+y$ )
- D. Down ( $-y$ )
- E. Left ( $-x$ )
- F. Right ( $+x$ )

### Problem #6 (3 points)

A person is sitting on a spinning stool rotating at  $10.0 \frac{\text{rad}}{\text{s}}$ . They are holding weights close to their chest. The person then extends their arms outwards. What happens to the stool's angular velocity?

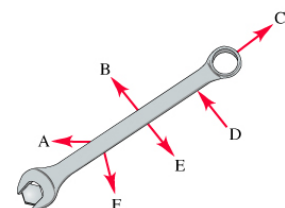
- A. It increases
- B. It decreases
- C. It stays the same
- D. It depends on the mass of the weights

### Problem #7 (3 points)

The wrench in the figure has six forces of equal magnitude acting on it.

#### Question #1 (3 points)

Rank these forces (A through F) on the basis of the magnitude (greatest to least) of the torque they apply to the wrench, measured about an axis centered on the bolt. If two are the same, list them alphabetically



**Problem #8 (12 points)**

A DVD (disc) has a mass of 16.0g and a diameter of 12.0cm. The player is spinning it at an angular speed of 9280.rpm (one rotation is  $2\pi$  radians) when it is turned off and slows to a stop in 2.50s.

**Question #1 (3 points)**

What is the moment of inertia of the DVD?

**Question #2 (3 points)**

What is the magnitude and direction of the torque felt by the DVD?

**Question #3 (3 points)**

What is the initial angular momentum of the DVD?

**Question #4 (3 points)**

What is the linear (straight line) speed of two points on the DVD: a point at the edge of the DVD, and a point 2.00cm from the center?

**Bonus #9 (3 points)**


Evaluate the definite integral  $\int_0^2 (x + 3x^2) dx$ . (recall: integral means anti-derivative, or area under a curve)

**Problem #10 (12 points)**

A rubber ball (solid sphere) with a diameter of  $0.314\text{m}$  is rolling without slipping with an initial linear speed  $v = 5.00 \frac{\text{m}}{\text{s}}$  from the top of a hill,  $325\text{m}$  high, to the bottom.

**Question #1 (3 points)**

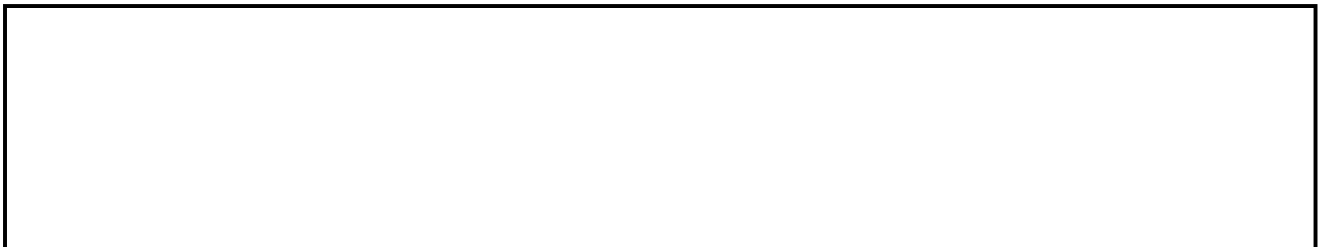
Draw a diagram showing this situation. Include a before and after picture labeling all relevant quantities.

**Question #2 (3 points)**

Derive an equation for the total kinetic energy in terms of  $m$  and  $v$ .

**Question #3 (3 points)**

When the ball reaches the bottom of the hill what will its linear speed be?

**Question #4 (3 points)**

What will be the rotational speed of the ball at the bottom of the hill?

