Symmetry suppression of allowed transitions between energy eigenstates of a Hamiltonian perturbed from a high symmetry.

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Abstract

It has been observed in quantum dots with C_{3v} symmetry that certain electronic transitions allowed by the dipole approximation selection rule are unresolvable in the measured photoluminiscence (PL) spectrum. We provide a theoretical model that predicts these spectral lines to be severely weakened if the Hamiltonian is considered to be perturbed from one with a higher spatial symmetry. An expression for the suppressing factor of the spectral line intensity is given in 1st order perturbation theory.

1 Introduction

Karlsson et al [1] have studied the PL spectrum of InGaAs C_{3v}-symmetric quantum dots (QDs). Their model assumes that the QD-Hamiltonian eigenstates which interact with electromagnetic waves on the studied interval of the spectrum are given by considering the symmetry breaking of exciton complex fine structure, which splits total angular momentum J eigenstates into energy levels which transform as double group irreps. By using rudimentary group theory, the energy levels, their degeneracies, and their allowed transitions can be calculated for all excitonic complexes, as was done by this particular

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QD. However, it was found that the number of spectral lines resolvable in a spectral feature associated with a specific excitonic transition is smaller than the predicted number for several exciton complex transitions, namely $X_{10} \rightarrow vac., 2X_{20} \rightarrow X_{10}, 2X_{11} \rightarrow X_{10}, 2X_{11} \rightarrow X_{01}, 2X_{21}^+ \rightarrow X_{11}^+$. Since the number of allowed transitions lowers if the Hamiltonian is altered to commute with more rotations (e.g. to D_{3h} or C_{6v} point group symmetry), the effect was dubbed "symmetry elevation". However, no explanation for why symmetry elevation occurs was found.

What the previous work on symmetry elevation in QDs did not consider is the nanocrystallic lattice that constitutes the QDs inside the potential well. The InGaAs QDs are formed by a lattice which does possess a 6-fold rotation along the z-axis. Even though the full Hamiltonian still only possesses C_{3v} symmetry, since it is ultimately dominated by the lower-symmetry potential well boundary shape, it can be modelled as a high-symmetry Hamiltonian which underwent symmetry breaking with a small perturbation and enjoys certain approximate symmetries, which still turn out to have a considerate effect in 1st order expansion. To obtain a theoretical description of the effects of these approximate symmetries, we first consider 1st order perturbation theory and describe a surjective mapping of basis vectors of irreps of the larger point group onto the basis vectors of irreps of its point subgroup, which allows us to determine the mapping of high-symmetry Hamiltonian eigenstates onto the low-symmetry Hamiltonian eigenstates under symmetry breaking, and then we emply Fermi's golden rule to quantify the suppression of certain spectral lines. The manifestation of de-intensifying of specific spectral lines due to approximate symmetries will be named "symmetry suppression".

2 Theoretical model of symmetry suppression

We shall first outline a general approach to describing a non-specific minimally symmetry-broken Hamiltonian, and then argue for why the assumptions made are justified in the case of InGaAs QDs.

2.1 Symmetry breaking as basis vector surjection

$\left|E_{1/2};2\right\rangle$
picture here

2.2 Domain alteration and perturbation theory

optimization problem
multiple domain choices

2.3 Evaluation of transition rates

References

[1] Karlsson, K. F. *et al* (2015), Spectral signatures of high-symmetry quantum dots and effects of symmetry breaking. *New Journal of Physics*, **17** 103017

[2] Altmann, S. L., Herzig, P. (1994), *Point-Group Theory Tables.* Oxford: Clarendon Press