



# A Basic Machine Learning Workflow



Representation



Evaluation



**Optimization** 

#### Choose:

- A feature representation
- Type of classifier to use

e.g. image pixels, with k-nearest neighbor classifier

#### Choose:

- What criterion distinguishes good vs. bad classifiers?
- e.g. % correct predictions on test set

#### Choose:

 How to search for the settings/parameters that give the best classifier for this evaluation criterion

e.g. try a range of values for "k" parameter in k-nearest neighbor classifier





```
In [2]: labeled_images = pd.read_csv('C:\\data\\digits_train.csv')
In [4]: labeled_images.head()
```

Out[4]:

Each row corresponds to a single data instance (sample)

The 'label' column contains the label for each data instance (sample)

	label	pixel0	pixel1	pixel2	pixel3	pixel4	pixel5	pixel6	pixel7	pixel8	
0	1	0	0	0	0	0	0	0	0	0	
1	0	0	0	0	0	0	0	0	0	0	
2	1	0	0	0	0	0	0	0	0	0	
3	4	0	0	0	0	0	0	0	0	0	
	0	0	0	0	0	0	0	0	0	0	

These columns contains the features of each data instance (sample)





- Capital X: features matrix
- Lower y: label

```
In [4]: #select images features from the second column to the last column.
   X = labeled_images.iloc[:,1:]

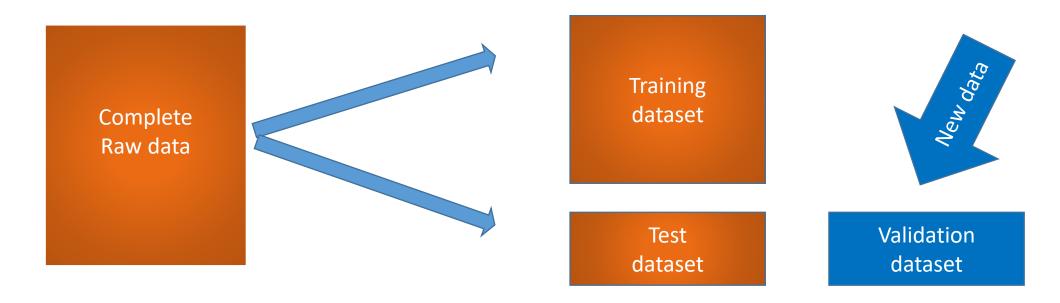
#select the first column which is the label, or the digit.
   y = labeled_images.iloc[:,:1]

print('The original input dataset shape is: ', labeled_images.shape)
   print('The X dataset shape is: ',X.shape)
   print('The y dataset shape is: ', y.shape)

The original input dataset shape is: (42000, 785)
   The X dataset shape is: (42000, 784)
   The y dataset shape is: (42000, 1)
```

## Splitting Input Data into Train/Test





Data used to build the machine learning model, are called the *training data*. The rest of the data will be used to assess how well the model works; these data are called *test data*.





#### **Create classifier object**

```
In [ ]: from sklearn.neighbors import KNeighborsClassifier

knn = KNeighborsClassifier(n_neighbors = 5)

Train the classifier (fit the estimator) using the training data

In [ ]: knn.fit(X_train, y_train)

Estimate the accuracy of the classifier on future data, using the test data

In [ ]: knn.score(X_test, y_test)
```

Use the trained classifier model to classify (predict) new, previously unseen data

```
In [ ]: predictd_y=knn.predict(y_test)
```

# Questions?





# Overfitting and Underfitting



	Classifier	Score on to	raining data	Score on test data
0	Logistic Regression Classifier		1.000000	0.835000
1	Support Vector Machine		1.000000	0.120000
2	Decision Tree Classifier		1.000000	0.680000
3	Random Forest classifier		0.998750	0.847500
4	Ridge Classifier		0.973750	0.745000
5	K-Nearest Neighbors Classifier		0.930000	0.870000
6	SGD Classifier		0.903750	0.835000
7	Naive Bayes Multinomial Classifier		0.843750	0.805000
8	ElasticNet Classifier		0.663894	0.531748
9	Lasso Classifier		0.639250	0.535359

	Number of compo	nents	Classifier	Score on training data	Score on test data	
0		50	Support Vector Machine	0.994375	0.920000	
1		90	Support Vector Machine	0.998125	0.920000	
2		30	Support Vector Machine	0.985000	0.915000	
3		70	Support Vector Machine	0.996250	0.915000	
4		110	Support Vector Machine	0.998125	0.910000	
5		130	Support Vector Machine	0.998125	0.905000	
6		150	Support Vector Machine	0.998125	0.902500	
7		170	Support Vector Machine	0.998750	0.895000	
8		190	Support Vector Machine	0.998750	0.887500	
9		10	Support Vector Machine	0.928750	0.882500	





- **Generalization** ability refers to an algorithm's ability to give accurate predictions for **new**, **previously unseen** data.
- **Assumptions**: Future unseen data (test set) will have the same properties as the current training sets.
  - Thus, models that are accurate on the training set are expected to be accurate on the test set.
  - But that may not happen if the trained model is tuned too specifically to the training set.
- Models that are too complex for the amount of training data available are said to overfit and are not likely to generalize well to new examples.
- Models that are too simple, that don't even do well on the training data, are said to underfit and also not likely to generalize well.





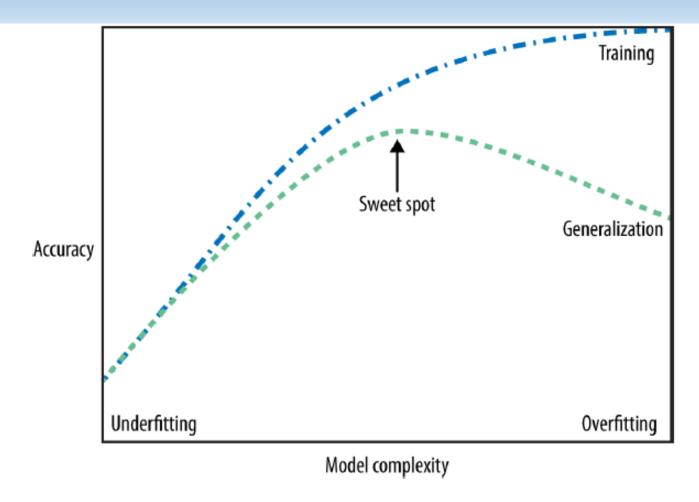
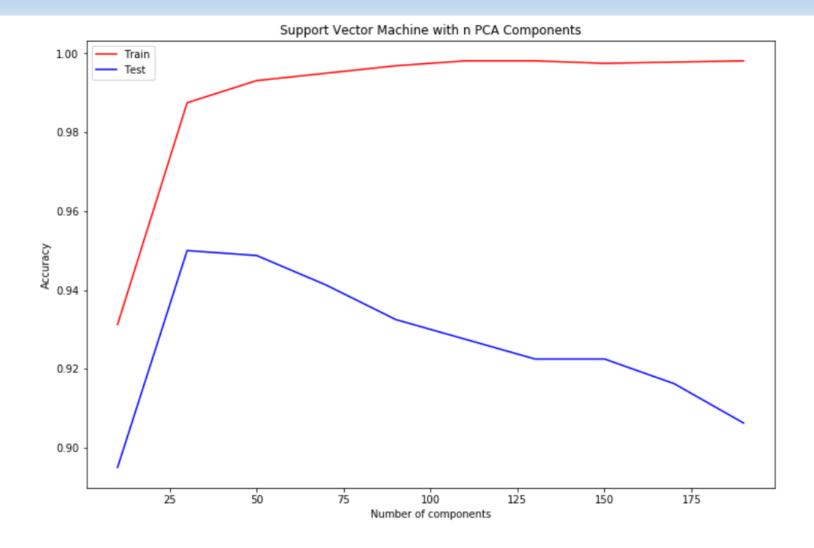


Figure 2-1. Trade-off of model complexity against training and test accuracy











### For each supervised learning method we'll explore:

- How the method works conceptually at a high level.
- What kind of feature preprocessing is typically needed.
- Key parameters that control model complexity, to avoid under-and overfitting.
- Positives and negatives of the learning method.

#### • This week:

- K-nearest neighbors
- Linear model fit using least-squares
- Logistic regression

### K-nearest Neighbors



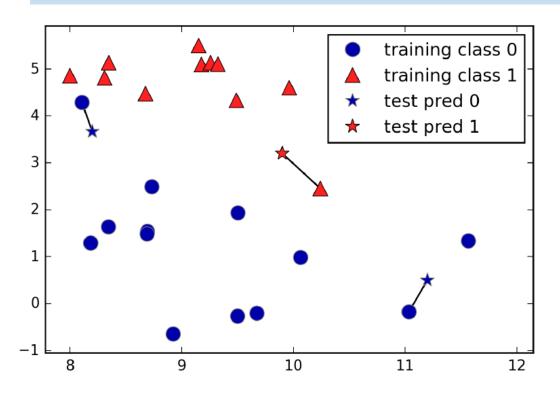
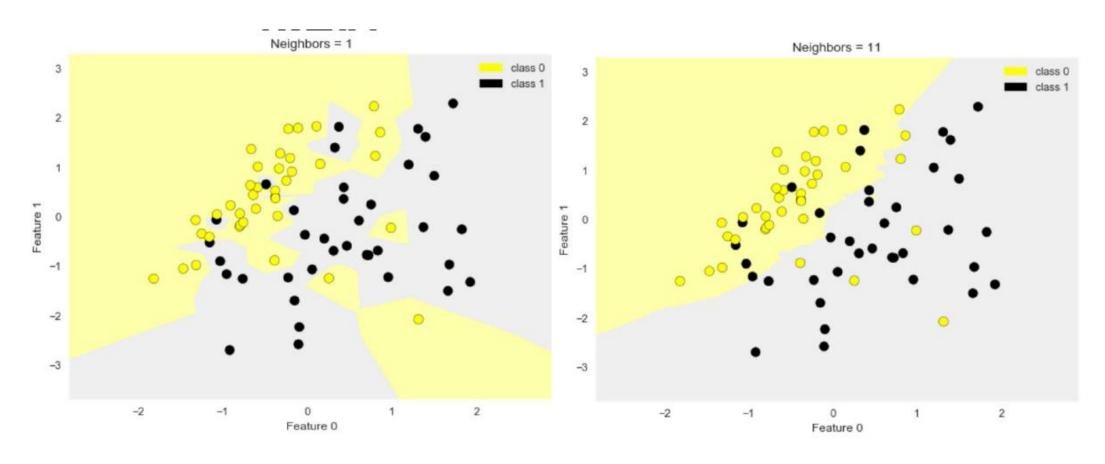


Figure 2-4. Predictions made by the one-nearest-neighbor model on the forge dataset

- To predict, find the closest data points in the training dataset—its "nearest neighbors."
- Import parameters:
  - Model complexity
    - n\_neighbors
  - Model fitting
    - Metric: distance between data points
      - Default: Euclidean

# Less Neighbors, More Complex





### Pros and Cons



#### Pros

- Easy to understand
- Easy to interpret
- Fast training

#### Cons

- With large training dataset, prediction can be very slow
- Does not perform well on many features
- Does not perform well on sparse data (data with majority 0s)

## Applications of KNN in Real World



- Useful in comparing similarities.
  - Concept search
  - Recommender systems
- Use as a benchmark for other more advanced algorithms
- Find out outliers

### Linear Models



- y = b + wX
- y is the label, or target to be predicted, or dependent variable
- *b* is the intercept
- w is a weight vector, or coefficient vector
- X is the feature matrix, or predictors matrix, or independent

• 
$$X = (x_0, x_1, x_2, x_3, ... x_{n-1}, x_n), w = (w_0, w_1, w_2, w_3, ... w_{n-1}, w_n)$$

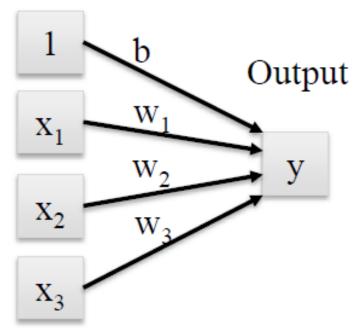
• 
$$\hat{y} = \hat{b} + \hat{w}_0 x_0 + \hat{w}_1 x_1 + \dots + \hat{w}_{n-1} x_{n-1} + \hat{w}_n x_n$$

•  $\hat{b}$ ,  $\hat{w}$  are the parameters to be estimated





### Input features



$$y = b + wX^T$$

$$w = (w_1, w_2, w_3, \dots w_{n-1}, w_n)$$

$$X = (x_1, x_2, x_3, \dots x_{n-1}, x_n),$$

$$\hat{y} = \hat{b} + \hat{w}_1 \cdot x_1 + \cdots \hat{w}_n \cdot x_n$$

### Linear Models



### • Regressions:

- Linear regression (ordinary least squares)
- Ridge regression
- Lasso regression
- ElasticNet regression
- SGD regression (large numbers of samples and features)

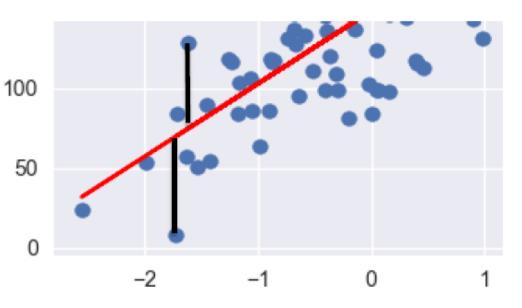
#### • Classifications:

- LinearSVC
- Logistic regression
- ElasticNet classifier
- SGD classifier

# Linear Regression (Ordinary Least Squares)



- Finds w and b that minimizes the sum of squared differences(RSS) over the training data between predicted target and actual target values.
- a.k.a. mean squared error of the linear model
- No parameters to control model complexity



$$RSS(w,b) = \sum_{\{i=1\}}^{N} (y_i - (w \cdot x_i + b))^2$$

Loss function

## Linear Regression (Ordinary Least Squares)



- Parameters are estimated from training data.
- There are many different ways to estimate w and b:
  - Different methods correspond to different "fit" criteria and goals and ways to control model complexity.
- The learning algorithm finds the parameters that optimize an <u>objective function</u>, typically to minimize some kind of <u>loss function</u> of the predicted target values vs. actual target values.

#### Fit linear regression model

```
clf=LinearRegression()
clf.fit(X_train,y_train)
LinearRegression(copy X=True, fit intercept=True, n jobs=1, normalize=False)
```



#### Check the R square of the regression model on training data

```
clf.score(X_train,y_train)
```

0.77297187265711575

#### Check the R square of the regression model on test data

```
clf.score(x_test,y_test) y = b + wX 0.58920115191864408 y = 38.14 - 0.1184X_0 + 0.0448X_1 + 0.0059X_2 + \dots - 0.4936X_{12}
```

#### Display the intercept and coefficients





Ridge regression learns w, b using the same least-squares criterion but adds a penalty for large variations in w parameters

$$RSS_{RIDGE}(\mathbf{w}, b) = \sum_{\{i=1\}}^{N} (\mathbf{y}_i - (\mathbf{w} \cdot \mathbf{x}_i + b))^2 + \alpha \sum_{\{j=1\}}^{p} w_j^2$$

Once the parameters are learned, the ridge regression <u>prediction</u> formula is the <u>same</u> as ordinary least-squares.

The addition of a parameter penalty is called <u>regularization</u>. Regularization prevents overfitting by restricting the model, typically to reduce its complexity.

Ridge regression uses <u>L2 regularization</u>: minimize sum of squares of w entries

The influence of the regularization term is controlled by the  $\alpha$  parameter.

Higher alpha means more regularization and simpler models.

### Lasso Regression



Lasso regression is another regularized linear regression that uses an L1 regularization penalty for training (instead of ridge's L2 penalty)

L1 penalty: Minimize the sum of the <u>absolute values</u> of the coefficients

$$RSS_{LASSO}(\mathbf{w}, b) = \sum_{\{i=1\}}^{N} (\mathbf{y}_i - (\mathbf{w} \cdot \mathbf{x}_i + b))^2 + \alpha \sum_{\{j=1\}}^{p} |w_j|$$

This has the effect of setting parameter weights in w to zero for the least influential variables. This is called a sparse solution: a kind of feature selection

The parameter  $\alpha$  controls amount of L1 regularization (default = 1.0). The prediction formula is the same as ordinary least-squares. When to use ridge vs lasso regression:

- Many small/medium sized effects: use ridge.
- Only a few variables with medium/large effect: use lasso.

### ElasticNet Regression



• Linear regression with combined L1 and L2 priors as regularizer.

$$\min_{w} \frac{1}{2n_{samples}} ||Xw - y||_{2}^{2} + \alpha \rho ||w||_{1} + \frac{\alpha(1 - \rho)}{2} ||w||_{2}^{2}$$

- This combination allows for learning a sparse model where few of the weights are non-zero like Lasso, while still maintaining the regularization properties of Ridge.
- Parameters:
  - Alpha: High  $\alpha$  means more regularization.
  - l1\_ratio: with 0 <= l1\_ratio <= 1. For l1\_ratio = 0 the penalty is an L2 penalty. For l1\_ratio = 1 it is an L1 penalty. For 0 < l1\_ratio < 1, the penalty is a combination of L1 and L2.

# Polynomial Features with Linear Regression



$$x=(x_0,x_1)$$
  $x'=(x_0,x_1,x_0^2,x_0x_1,x_1^2)$ 

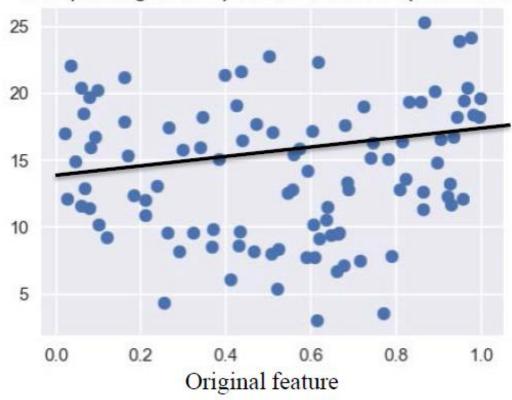
$$\hat{y} = \hat{w}_0 x_0 + \hat{w}_1 x_1 + \hat{w}_{00} x_0^2 + \hat{w}_{01} x_0 x_1 + \hat{w}_{11} x_1^2 + b$$

- Generate new features consisting of all polynomial combinations of the original two features  $(x_0, x_1)$ .
- The degree of the polynomial specifies how many variables participate at a time in each new feature (above example: degree 2)
- This is still a weighted linear combination of features, so it's <u>still a linear</u> <u>model</u>, and can use same least-squares estimation method for w and b.

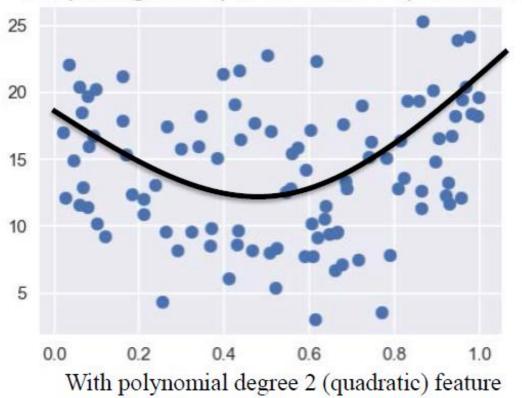
# Polynomial Features with Linear Regression







#### Complex regression problem with one input variable



# Polynomial Features with Linear Regression



### Why would we want to transform our data this way?

- To capture interactions between the original features by adding them as features to the linear model.
- To make a classification problem easier (we'll see this later).

# More generally, we can apply other non-linear transformations to create new features

(Technically, these are called non-linear basis functions)

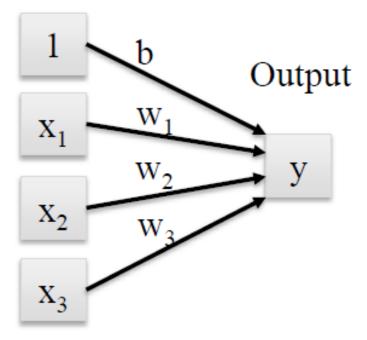
# Beware of polynomial feature expansion with high as this can lead to complex models that overfit

 Thus, polynomial feature expansion is often combined with a regularized learning method like ridge regression.





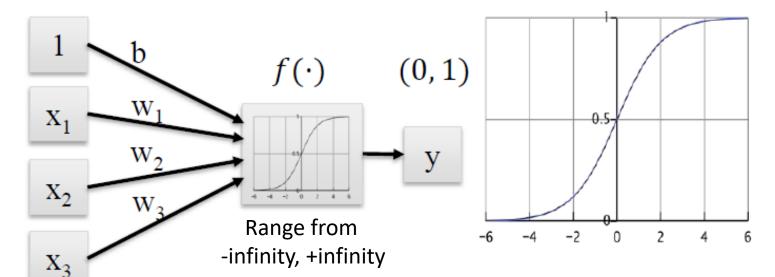
### Input features



$$\hat{y} = \hat{b} + \hat{w}_1 \cdot x_1 + \cdots \hat{w}_n \cdot x_n$$

### Logistic Regression





The logistic function transforms real-valued input to an output number y between 0 and 1, interpreted as the <u>probability</u> the input object belongs to the positive class, given its input features  $(x_0, x_1, ..., x_n)$ 

$$\hat{y} = \underset{1}{\text{logistic}} (\hat{b} + \widehat{w}_1 \cdot x_1 + \cdots \widehat{w}_n \cdot x_n)$$

$$= \frac{1}{1 + \exp\left[-\left(\hat{b} + \widehat{w}_1 \cdot x_1 + \cdots \widehat{w}_n \cdot x_n\right)\right]}$$



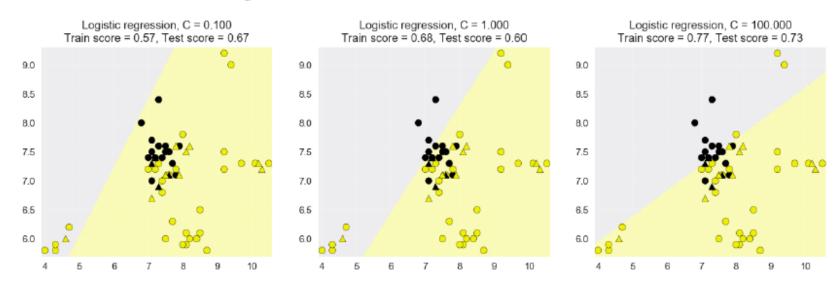


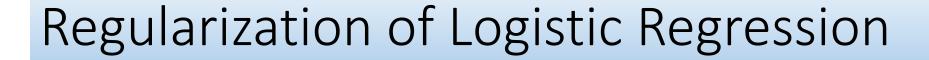
L2 regularization is 'on' by default (like ridge regression)

Parameter C controls amount of regularization (default 1.0)

Parameter C controls amount of regularization (default 1.0)

As with regularized linear regression, it can be important to normalize all features so that they are on the same scale.







# The strength of regularization is determined by C Larger values of C: less regularization

- Fit the training data as well as possible
- Each individual data point is important to classify correctly

### Smaller values of C: more regularization

More tolerant of errors on individual data points





### Model complexity

- alpha: weight given to the L1 or L2 regularization term in regression models
  - default = 1.0
- C: regularization weight for LinearSVC and LogisticRegression classification models
  - default = 1.0





- Important for some machine learning methods that all features are on the same scale (e.g. faster convergence in learning, more uniform or 'fair' influence for all weights)
  - e.g. regularized regression, k-NN, support vector machines, neural networks

### Linear Models



#### Pros:

- Simple and easy to train.
- Fast prediction.
- Scales well to very large datasets.
- Works well with sparse data.
- Reasons for prediction are relatively easy to interpret.

#### Cons:

- For lower-dimensional data, other models may have superior generalization performance.
- For classification, data may not be linearly separable (more on this in SVMs with non-linear kernels)

# Questions?



