Case Study 1

```
In [37]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from matplotlib import colors
import plotly.express as px # for USA map
from mpl_toolkits import mplot3d # for 3D graph
%config InlineBackend.figure_format = 'retina'

import seaborn as sns # for heatmap
from sklearn.model_selection import train_test_split # to split the dataset
import statsmodels.api as sm # Linear Regression Approach 1
from sklearn.linear_model import LinearRegression # Linear Regression Approach 2
from sklearn.metrics import r2_score # to evaluate predictions
```

1. Dataset Pre-processing

In [38]: df = pd.read_csv('loans_full_schema.csv')
df.head(10)

Out[38]:

	emp_title	emp_length	state	homeownership	annual_income	verified_income	debt_to_income	annual_income_joint	verification_income_joint	c
0	global config engineer	3.0	NJ	MORTGAGE	90000.0	Verified	18.01	NaN	NaN	_
1	warehouse office clerk	10.0	н	RENT	40000.0	Not Verified	5.04	NaN	NaN	
2	assembly	3.0	WI	RENT	40000.0	Source Verified	21.15	NaN	NaN	
3	customer service	1.0	PA	RENT	30000.0	Not Verified	10.16	NaN	NaN	
4	security supervisor	10.0	CA	RENT	35000.0	Verified	57.96	57000.0	Verified	
5	NaN	NaN	KY	OWN	34000.0	Not Verified	6.46	NaN	NaN	
6	hr	10.0	MI	MORTGAGE	35000.0	Source Verified	23.66	155000.0	Not Verified	
7	police	10.0	AZ	MORTGAGE	110000.0	Source Verified	16.19	NaN	NaN	
8	parts	10.0	NV	MORTGAGE	65000.0	Source Verified	36.48	NaN	NaN	
9	4th person	3.0	IL	RENT	30000.0	Not Verified	18.91	NaN	NaN	

10 rows × 55 columns

4

<class 'pandas.core.frame.DataFrame'> RangeIndex: 10000 entries, 0 to 9999 Data columns (total 55 columns): Column Non-Null Count Dtype 0 emp_title 9167 non-null object 1 emp_length 9183 non-null float64 2 state 10000 non-null object 3 homeownership 10000 non-null object annual_income 10000 non-null float64 4 verified_income 5 10000 non-null object debt_to_income 9976 non-null float64 6 1495 non-null float64 7 annual_income_joint 8 verification_income_joint 1455 non-null object 1495 non-null 9 debt_to_income_joint float64 10000 non-null int64 delinq_2y months_since_last_delinq 4342 non-null float64 11 earliest_credit_line 10000 non-null int64 12 13 inquiries_last_12m 10000 non-null int64 total_credit_lines 10000 non-null int64 14 15 open_credit_lines 10000 non-null int64 16 total_credit_limit 10000 non-null int64 17 total_credit_utilized 10000 non-null int64 num_collections_last_12m 10000 non-null int64 num_historical_failed_to_pay 10000 non-null int64 19 months_since_90d_late 2285 non-null 20 float64 21 current_accounts_deling 10000 non-null int64 total_collection_amount_ever 10000 non-null int64 22 23 current_installment_accounts 10000 non-null int64 10000 non-null int64 24 accounts_opened_24m months_since_last_credit_inquiry 8729 non-null float64 num_satisfactory_accounts 10000 non-null int64 num_accounts_120d_past_due 9682 non-null float64 27 ${\tt num_accounts_30d_past_due}$ 10000 non-null int64 28 10000 non-null int64 29 num_active_debit_accounts total_debit_limit 10000 non-null int64 30 num_total_cc_accounts 10000 non-null int64 31 num_open_cc_accounts 10000 non-null int64 num cc carrying balance 10000 non-null int64 10000 non-null int64 num_mort_accounts 34 10000 non-null float64 35 account_never_delinq_percent 10000 non-null int64 36 tax_liens 37 public_record_bankrupt 10000 non-null int64 38 loan_purpose 10000 non-null object 10000 non-null object 39 application_type 40 loan_amount 10000 non-null int64 41 term 10000 non-null int64 interest_rate 10000 non-null float64 42 10000 non-null float64 installment 43 10000 non-null object 44 grade 45 sub_grade 10000 non-null object 46 issue_month 10000 non-null object 47 loan_status 10000 non-null object 48 initial_listing_status 10000 non-null object disbursement_method 10000 non-null object 50 balance 10000 non-null float64 paid_total 10000 non-null float64 51 10000 non-null float64 paid_principal 52 53 paid_interest 10000 non-null float64 54 paid_late_fees 10000 non-null float64

dtypes: float64(17), int64(25), object(13)

memory usage: 4.2+ MB

1.1 Remove NULL values

Let's see how many NULL values we have in our dataset.

In [40]: | df.isnull().sum() Out[40]: emp_title 833 817 emp_length 0 state homeownership 0 annual_income 0 verified_income 0 debt_to_income 24 annual_income_joint 8505 verification_income_joint 8545 debt_to_income_joint 8505 delinq_2y 0 months_since_last_delinq 5658 earliest_credit_line 0 inquiries_last_12m 0 total_credit_lines 0 open_credit_lines total_credit_limit 0 total_credit_utilized 0 num_collections_last_12m 0 num_historical_failed_to_pay 0 months_since_90d_late 7715 current_accounts_delinq 0 total_collection_amount_ever 0 current_installment_accounts 0 accounts_opened_24m 0 months_since_last_credit_inquiry 1271 num_satisfactory_accounts 0 num_accounts_120d_past_due 318 num_accounts_30d_past_due 0 num_active_debit_accounts 0 total_debit_limit 0 num_total_cc_accounts num_open_cc_accounts 0 num_cc_carrying_balance 0 num_mort_accounts 0 account_never_delinq_percent tax_liens public_record_bankrupt loan_purpose application_type loan_amount 0 term 0 interest_rate 0 installment 0 grade 0 sub_grade 0 issue_month 0 loan_status 0 initial_listing_status 0 disbursement_method 0 balance 0 paid_total 0 paid_principal 0 paid_interest 0 paid_late_fees 0 dtype: int64

Unfortunately there are columns where most of values are NULLs. They are completely useless, so just remove those columns where more than 1% of the rows for that column contain a null value.

```
In [41]: df_cleaned = df[[label for label in df if df[label].isnull().sum() <= 0.01 * df.shape[0]]]</pre>
```

Let's see how it looks like now.

```
In [42]: | df_cleaned.isnull().sum()
Out[42]: state
                                           0
         homeownership
                                           0
         annual_income
                                           0
         verified income
                                           0
         debt_to_income
                                          24
         delinq_2y
                                           0
         earliest_credit_line
                                           0
         inquiries_last_12m
         total_credit_lines
                                           0
         open_credit_lines
                                           0
         total_credit_limit
                                           0
         total_credit_utilized
         num_collections_last_12m
                                           0
         num_historical_failed_to_pay
                                           0
         current_accounts_delinq
         total_collection_amount_ever
         current_installment_accounts
         accounts_opened_24m
                                           0
         num_satisfactory_accounts
         num_accounts_30d_past_due
         num_active_debit_accounts
                                           0
         total_debit_limit
                                           0
         num_total_cc_accounts
         num_open_cc_accounts
         num_cc_carrying_balance
                                           0
         num_mort_accounts
                                           0
         account_never_delinq_percent
         tax_liens
         public_record_bankrupt
         loan_purpose
                                           0
         application_type
         loan_amount
         term
         interest_rate
                                           0
         installment
                                           0
         grade
         sub_grade
                                           0
         issue_month
         loan_status
         initial_listing_status
         disbursement_method
                                           0
         balance
                                           0
         paid_total
         paid_principal
                                           0
         paid_interest
         paid_late_fees
         dtype: int64
```

Ok, much better. Now we have to do something with those NULL values. We can:

- remove rows cointain NULL values,
- fill them with median or mode value,
- or use some imputation and try to predict their missing values.

Let's try the first option and see what will happen.

```
In [43]: df_cleaned = df_cleaned.dropna()
df_cleaned.shape[0] / df.shape[0]
```

Out[43]: 0.9976

It looks good, we removed less than 0.3% of rows. I think it's good enough and there's no point to do something more with that.

1.2 Remove useless columns

Let's take a look on our cleaned dataset.

In [44]: df_cleaned.head(10)

Out[44]:

	state	homeownership	annual_income	verified_income	debt_to_income	delinq_2y	earliest_credit_line	inquiries_last_12m	total_credit_lines	opeı
0	NJ	MORTGAGE	90000.0	Verified	18.01	0	2001	6	28	
1	НІ	RENT	40000.0	Not Verified	5.04	0	1996	1	30	
2	WI	RENT	40000.0	Source Verified	21.15	0	2006	4	31	
3	PA	RENT	30000.0	Not Verified	10.16	0	2007	0	4	
4	CA	RENT	35000.0	Verified	57.96	0	2008	7	22	
5	KY	OWN	34000.0	Not Verified	6.46	1	1990	6	32	
6	МІ	MORTGAGE	35000.0	Source Verified	23.66	0	2004	1	12	
7	ΑZ	MORTGAGE	110000.0	Source Verified	16.19	1	2005	1	30	
8	NV	MORTGAGE	65000.0	Source Verified	36.48	1	1998	3	35	
9	IL	RENT	30000.0	Not Verified	18.91	0	2001	0	9	

10 rows × 46 columns



As we can see, "issue_month" only includes three values: "Jan-2018", "Feb-2018", and "Mar-2018". The time does not vary much and its impact to the applicant's credit profile is negligible. Thus column "issue month" can be dropped.

The same goes for "disbursement_method" which only includes two values: "Cash" and "DirectPay". The impact of these methods to the applicant's credit profile can also be neglected. Thus column "disbursement_method" can also be dropped.

Since "sub_grade" (a grade assigned to the loan applicant based on his credit profile which determines the interest rate) has fully included the information of "grade", column "grade" can be dropped as well. A detailed explanation of subgrade can be found here:

https://www.lendingclub.com/public/rates-and-fees.action (https://www.lendingclub.com/public/rates-and-fees.action)

Since the three major US credit bureaus no longer include tax liens on your credit reports, a tax lien is no longer able to affect your credit. Thus, column "tax_liens" can be dropped. Details can be found here: https://www.bankrate.com/finance/credit-cards/how-tax-liens-affect-your-credit-score/),

Out[45]:

	state	homeownership	annual_income	verified_income	debt_to_income	delinq_2y	earliest_credit_line	inquiries_last_12m	total_credit_lines	opei		
0	NJ	MORTGAGE	90000.0	Verified	18.01	0	2001	6	28			
1	Н	RENT	40000.0	Not Verified	5.04	0	1996	1	30			
2	WI	RENT	40000.0	Source Verified	21.15	0	2006	4	31			
3	PA	RENT	30000.0	Not Verified	10.16	0	2007	0	4			
4	CA	RENT	35000.0	Verified	57.96	0	2008	7	22			
5	KY	OWN	34000.0	Not Verified	6.46	1	1990	6	32			
6	MI	MORTGAGE	35000.0	Source Verified	23.66	0	2004	1	12			
7	ΑZ	MORTGAGE	110000.0	Source Verified	16.19	1	2005	1	30			
8	NV	MORTGAGE	65000.0	Source Verified	36.48	1	1998	3	35			
9	IL	RENT	30000.0	Not Verified	18.91	0	2001	0	9			
10 r	10 rows × 42 columns											

1.3 Remove columns including values with insignificant frequencies and outlier rows

```
In [46]: for label in list(df cleaned):
              if len(df_cleaned[label].unique()) < 20:</pre>
                  print(df_cleaned[label].value_counts())
                  print("\n")
         MORTGAGE
                      4778
                      3848
         RENT
         OWN
                      1350
         Name: homeownership, dtype: int64
         Source Verified
                              4115
         Not Verified
                              3573
         Verified
                              2288
         Name: verified_income, dtype: int64
         0
                8556
         1
                1008
                 257
         2
         3
                  88
                  34
          5
                  10
          8
                   7
```

We can see that features "current_accounts_delinq" and "num_accounts_30d_past_due" have only two possible values: 0 and 1, but with only 1 occurrences of 1 (less than 1%), so definitely they are insignificant.

The same goes for "num collections last 12m" feature (non-zero values have only 1.3% frequency).

Therefore we can drop these three columns.

Since >1 values in "num_historical_failed_to_pay", >1 values in "public_record_bankrupt", >2 values in "delinq_2y", >6 values in "num_mort_accounts" and values other than "Current" and "Fully Paid" in "loan_status" have very low frequency (less than 2%), we can remove these outliers. The same goes with "moving", "vacation" and "renewable energy" values in "loan_purpose".

Out[4	7]:
-------	-----

	state	homeownership	annual_income	verified_income	debt_to_income	delinq_2y	earliest_credit_line	inquiries_last_12m	total_credit_lines	opei
C	NJ	MORTGAGE	90000.0	Verified	18.01	0	2001	6	28	
1	HI	RENT	40000.0	Not Verified	5.04	0	1996	1	30	
2	. WI	RENT	40000.0	Source Verified	21.15	0	2006	4	31	
3	PA	RENT	30000.0	Not Verified	10.16	0	2007	0	4	
4	CA	RENT	35000.0	Verified	57.96	0	2008	7	22	
5	KY	OWN	34000.0	Not Verified	6.46	1	1990	6	32	
6	MI	MORTGAGE	35000.0	Source Verified	23.66	0	2004	1	12	
7	AZ	MORTGAGE	110000.0	Source Verified	16.19	1	2005	1	30	
8	NV	MORTGAGE	65000.0	Source Verified	36.48	1	1998	3	35	
9	IL	RENT	30000.0	Not Verified	18.91	0	2001	0	9	

10 rows × 39 columns

```
In [48]: df_cleaned.shape[0] / df.shape[0]
```

Out[48]: 0.9541

So the removed records are no more than 5%, which means the cleaned dataset can still represent the original dataset well.

1.4 Categorical features

To use any machine learning model we have to have only numerical data. So, let's do something with our non-numerical features.

```
In [49]: df_cleaned.select_dtypes(include=["object"]).head()
```

Out[49]:

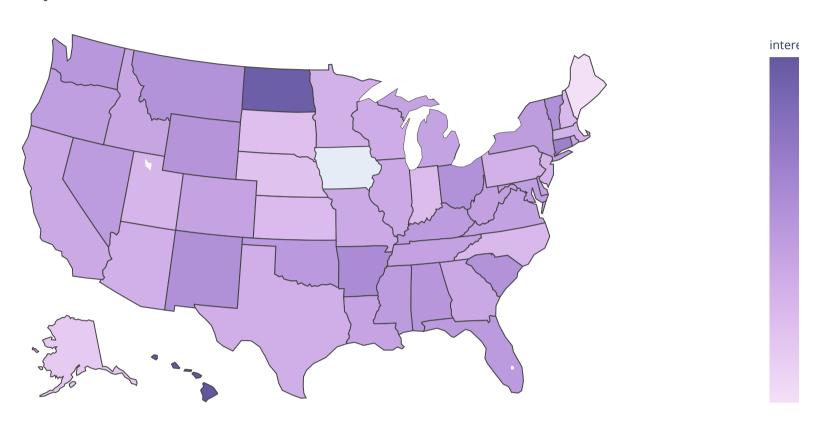
	state	homeownership	verified_income	loan_purpose	application_type	sub_grade	loan_status	initial_listing_status
0	NJ	MORTGAGE	Verified	moving	individual	C3	Current	whole
1	HI	RENT	Not Verified	debt_consolidation	individual	C1	Current	whole
2	WI	RENT	Source Verified	other	individual	D1	Current	fractional
3	PA	RENT	Not Verified	debt_consolidation	individual	А3	Current	whole
4	CA	RENT	Verified	credit_card	joint	C3	Current	whole

Since each grade (A, B, C, D, E, F) and the associated subgrade have its own sequence, we can map them into integers.

```
In [50]: def subgrade_mapping(lst: list) -> dict:
             mapping = {}
             for subgrade in lst:
                 subgrade = subgrade.strip()
                 letter = subgrade[0]
                 num = int(subgrade[1])
                 if letter == 'A':
                     m = 0
                 elif letter == 'B':
                     m = 1
                 elif letter == 'C':
                     m = 2
                 elif letter == 'D':
                     m = 3
                 elif letter == 'E':
                     m = 4
                 elif letter == 'F':
                     m = 5
                 elif letter == 'G':
                     m = 6
                 else:
                     m = np.nan
                 mapping[subgrade] = m*5+num
             return mapping
         df_cleaned["sub_grade"] = df_cleaned["sub_grade"].map(subgrade_mapping(df_cleaned["sub_grade"].unique()))
```

To show the impact of states, let's plot the average interest rate by states on the US map:

Interest Rate by States



As we can see from the plot above, the average interest rate has no significant difference among different states, and there is also no significant trend on the map. Thus, we decide to drop this feature otherwise too many dummy indicators will be created.

```
In [52]: df_cleaned = df_cleaned.drop(["state"], axis=1)
```

The rest of the categorical features can be either mapped to integers, or to dummy indicators.

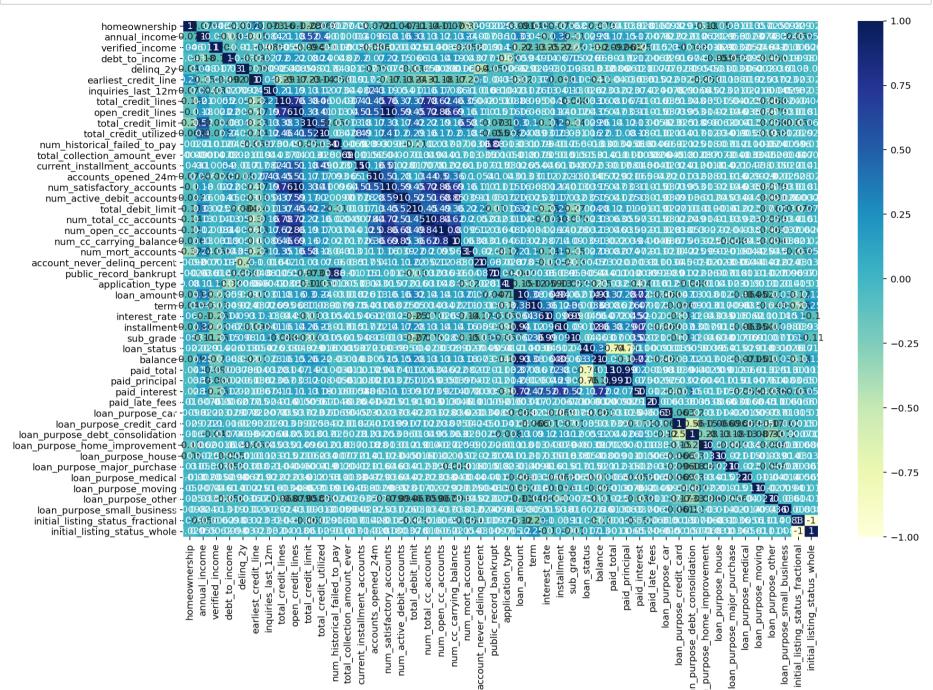
We can calculate the correlation matrix for the cleaned dataset, and then plot the values int the heatmap:

```
In [54]: C = df_cleaned.corr()
C
```

Out[54]:

	homeownership	annual_income	verified_income	debt_to_income	delinq_2y	earliest_credit_line	inquiries_last_12n
homeownership	1.000000	-0.079151	0.046019	-0.042820	-0.046980	0.211652	-0.072834
annual_income	-0.079151	1.000000	-0.010704	-0.178030	0.048327	-0.149604	0.08384
verified_income	0.046019	-0.010704	1.000000	-0.104378	-0.016718	-0.028915	-0.085276
debt_to_income	-0.042820	-0.178030	-0.104378	1.000000	-0.030423	-0.091753	0.026617
delinq_2y	-0.046980	0.048327	-0.016718	-0.030423	1.000000	-0.079991	0.009196
earliest_credit_line	0.211652	-0.149604	-0.028915	-0.091753	-0.079991	1.000000	0.045049
inquiries_last_12m	-0.072834	0.083841	-0.085276	0.026617	0.009196	0.045049	1.000000
total_credit_lines	-0.157440	0.213732	-0.005464	0.200139	0.053625	-0.292755	0.211719
open_credit_lines	-0.104927	0.183229	-0.020913	0.216616	0.008526	-0.171671	0.190512
total_credit_limit	-0.283807	0.516991	-0.094120	0.079804	0.047853	-0.227273	0.132627
total_credit_utilized	-0.068260	0.404094	-0.070793	0.238920	-0.017248	-0.138721	0.12271(
num_historical_failed_to_pay	-0.002658	0.010090	-0.011963	0.004759	-0.043315	-0.055915	0.073274
total_collection_amount_ever	-0.004945	-0.000138	-0.000731	0.019678	0.020699	-0.018980	0.043737
current_installment_accounts	0.043023	0.099841	-0.005425	0.199417	-0.017115	0.016830	0.082437
accounts_opened_24m	-0.071533	0.095786	-0.085576	0.070386	-0.049808	0.027144	0.430137
num_satisfactory_accounts	-0.104639	0.183401	-0.020235	0.216519	0.007397	-0.169864	0.190106
num_active_debit_accounts	-0.047257	0.162406	-0.014165	0.146236	-0.022765	-0.126503	0.053699
total_debit_limit	-0.114023	0.332041	0.025117	0.065923	-0.084205	-0.236824	0.010620
num_total_cc_accounts	-0.138289	0.128651	0.014430	0.128460	0.054412	-0.310141	0.15844
num_open_cc_accounts	-0.107153	0.118596	-0.008414	0.135926	0.008561	-0.182461	0.165867
num_cc_carrying_balance	-0.076228	0.132248	-0.031361	0.188512	0.000160	-0.165881	0.085907
num_mort_accounts	-0.321788	0.239187	-0.057784	0.043056	0.065874	-0.286874	0.110957
account_never_delinq_percent	0.009235	-0.006972	-0.001943	0.077484	-0.403156	0.099801	-0.01567{
public_record_bankrupt	-0.002558	-0.035825	-0.013765	0.013845	-0.059265	-0.042526	0.080800
application_type	0.080238	0.106248	0.111252	-0.318629	-0.006613	0.045813	0.00416
loan_amount	-0.090876	0.327749	-0.220700	0.058515	-0.029017	-0.118449	0.03104
term	-0.049457 0.065004	0.045115 -0.104302	-0.130138 -0.247306	0.049488 0.142798	-0.024053 0.092866	-0.037255 0.103934	0.026177 0.12756
interest_rate installment	-0.073472	0.318780	-0.221725	0.142798	-0.009993	-0.098462	0.04050
sub_grade	0.067836	-0.109953	-0.250659	0.146867	0.098128	0.110941	0.132838
loan_status	0.021573	-0.028886	0.014012	0.026220	-0.012819	0.005429	-0.025729
balance	-0.078949	0.281012	-0.204414	0.068380	-0.032429	-0.108358	0.023200
paid_total	-0.041171	0.166830	-0.091650	-0.003740	0.008633	-0.040014	0.031759
paid_principal	-0.038193	0.147156	-0.060669	-0.019796	0.006073	-0.035979	0.022577
paid_interest	-0.028390	0.172583	-0.247743	0.121262	0.020649	-0.036245	0.07401
paid_late_fees	0.015689	-0.007632	-0.015268	-0.006199	-0.007722	0.015065	0.023854
loan_purpose_car	0.009826	-0.022375	0.023286	-0.029387	0.007828	0.021914	-0.00783
loan_purpose_credit_card	0.028877	-0.021906	0.103593	0.015702	-0.028821	0.032448	-0.029106
loan_purpose_debt_consolidation	0.015785	-0.011737	-0.047814	0.074237	0.009500	-0.041879	-0.006617
loan_purpose_home_improvement	-0.127068	0.062172	0.000157	-0.014206	0.045316	-0.053206	0.04508
loan_purpose_house	-0.050094	0.002867	-0.029334	-0.054975	-0.010271	-0.011045	0.022800
loan_purpose_major_purchase	0.030829	0.055108	-0.003245	-0.055496	-0.003097	0.037923	0.02093(
loan_purpose_medical	-0.012787	-0.002275	-0.005214	-0.009831	-0.006186	-0.019169	-0.021809
loan_purpose_moving	0.057043	-0.007368	-0.046367	-0.013856	-0.002045	0.024761	0.016098
loan_purpose_other	0.024794	-0.032712	-0.042363	-0.055895	-0.003603	0.037019	-0.000452
loan_purpose_small_business	0.009756	0.023846	-0.013484	-0.018991	-0.010292	0.022811	0.002927
initial_listing_status_fractional	0.029464	-0.055484	-0.006187	0.009768	0.030267	0.023377	0.03157{
initial_listing_status_whole	-0.029464	0.055484	0.006187	-0.009768	-0.030267	-0.023377	-0.03157{

48 rows × 48 columns

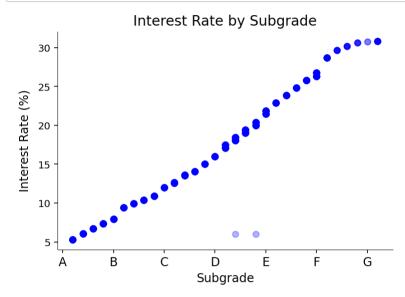


In [56]: C['interest_rate']

Out[56]: homeownership 0.065004 annual_income -0.104302 verified_income -0.247306 0.142798 debt_to_income delinq_2y 0.092866 earliest_credit_line 0.103934 inquiries_last_12m 0.127561 total_credit_lines -0.044336 open_credit_lines -0.010868 total_credit_limit -0.131637 total_credit_utilized 0.030728 num_historical_failed_to_pay 0.053766 total_collection_amount_ever 0.014539 current_installment_accounts 0.046329 accounts_opened_24m 0.121979 num_satisfactory_accounts -0.011504 num_active_debit_accounts 0.031269 total_debit_limit -0.254728 num_total_cc_accounts -0.070805 num_open_cc_accounts -0.026397 num_cc_carrying_balance 0.086763 num_mort_accounts -0.140148 account_never_delinq_percent -0.121952 public_record_bankrupt 0.050280 application_type -0.058784 loan_amount 0.063872 0.360431 term interest_rate 1.000000 $in stall {\tt ment}$ 0.095762 sub_grade 0.992881 loan_status -0.045264 balance 0.064318 paid_total 0.072036 paid_principal 0.004505 paid_interest 0.522166 paid_late_fees 0.019839 loan_purpose_car -0.007848 loan_purpose_credit_card -0.106871 loan_purpose_debt_consolidation 0.124058 loan_purpose_home_improvement -0.042889 loan_purpose_house -0.035385 loan_purpose_major_purchase -0.015513 loan_purpose_medical -0.006185 loan_purpose_moving 0.010780 loan_purpose_other -0.001368 loan_purpose_small_business 0.015426 initial_listing_status_fractional 0.104154 initial_listing_status_whole -0.104154 Name: interest_rate, dtype: float64

As we can see from the graph and table above, the most relevant variable is sub_grade (0.993) and paid_interest(0.522) We can plot them as scatter plots to see the data distribution!

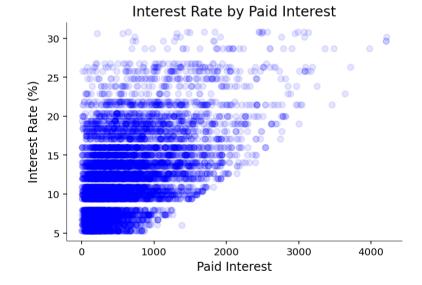
```
In [57]: | fig, ax = plt.subplots(figsize = (6,4))
         ax.scatter(df_cleaned['sub_grade'], df_cleaned['interest_rate'], color='blue', alpha=0.3)
         ax.set_xlabel('Subgrade', fontsize=12)
         ax.set_ylabel('Interest Rate (%)', fontsize=12)
         ax.set_title("Interest Rate by Subgrade", size=14)
         # Set numerical y axis
         ax.yaxis.set_label_coords(-0.08, 0.5)
         # Set categorical ticks for x axis
         ax.set_xticks(np.arange(7)*5)
         ax.set_xticklabels(['A','B','C','D', 'E', 'F', 'G'], size=12)
         #ax.tick_params(axis='x', Length=0)
                                                #Hide ticks in x axis
         ax.spines['top'].set_visible(False)
         ax.spines['right'].set_visible(False)
         ax.spines['left'].set_linewidth(.5)
         ax.spines['bottom'].set_linewidth(.5)
         plt.show()
```



```
In [58]: fig, ax = plt.subplots(figsize = (6,4))
    ax.scatter(df_cleaned['paid_interest'], df_cleaned['interest_rate'], color='blue', alpha=0.1)

ax.set_xlabel('Paid Interest', fontsize=12)
    ax.set_ylabel('Interest Rate (%)', fontsize=12)
    ax.set_title("Interest Rate by Paid Interest", size=14)

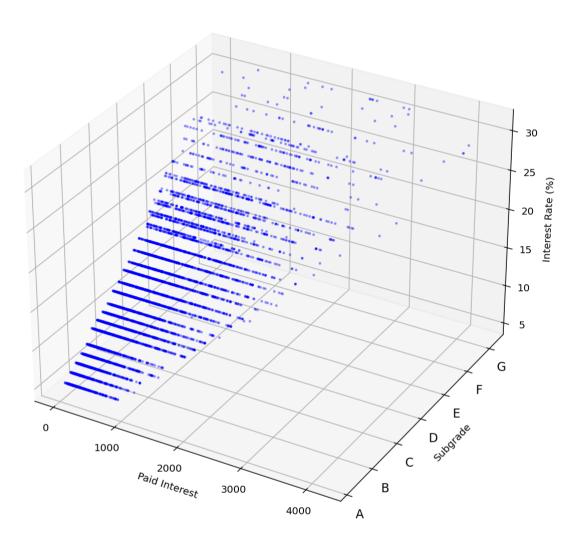
# Set numerical y axis
    ax.yaxis.set_label_coords(-0.08, 0.5)
    ax.spines['top'].set_visible(False)
    ax.spines['top'].set_visible(False)
    ax.spines['left'].set_linewidth(.5)
    ax.spines['bottom'].set_linewidth(.5)
```



We can even plot them into 3D graph:

```
In [59]:
         # Creating figure
         fig = plt.figure(figsize = (30, 10))
         ax = plt.axes(projection ="3d")
         # Creating plot
         ax.scatter3D(df_cleaned['paid_interest'], df_cleaned['sub_grade'], df_cleaned['interest_rate'],
                      color = 'blue', s=3,alpha=0.3)
         # Set categorical ticks for y axis
         ax.set_yticks(np.arange(7)*5)
         ax.set_yticklabels(['A','B','C','D', 'E', 'F', 'G'], size=12)
         ax.set_xlabel('Paid Interest')
         ax.set_ylabel('Subgrade')
         ax.set_zlabel('Interest Rate (%)')
         plt.title("Interest Rate Distribution with Subgrade and Paid Interest")
         # show plot
         plt.show()
```

Interest Rate Distribution with Subgrade and Paid Interest



As we can see from the graphs above, subgrade has a strong linear correlation to interest rate; paid interest mainly determine the lower limit of the interest rate, but has no restraint to the upper limit.

2. Modeling Approach 1: Linear Regression Using statsmodel

2.1 Perform Linear Regression

In [62]: # Performing a summary to list out all the different parameters of the regression line fitted
lr.summary()

Out[62]: OLS Regression Results

dtype: float64

Dep. Variable: 0.986 interest_rate R-squared: Model: OLS Adj. R-squared: 0.986 Least Squares Method: **F-statistic:** 4.809e+05 Date: Tue, 12 Apr 2022 Prob (F-statistic): 0.00 Time: 21:19:51 Log-Likelihood: -5802.8 No. Observations: 6678 **AIC:** 1.161e+04 **Df Residuals:** 6676 **BIC:** 1.162e+04 Df Model: **Covariance Type:** nonrobust t P>|t| [0.025 0.975] coef std err 3.865 **const** 3.8372 0.014 271.123 0.000 3.809 0.001 693.494 0.000 sub_grade 0.8457 0.843 0.848 **Omnibus:** 2067.897 **Durbin-Watson:** 2.023 Prob(Omnibus): 0.000 Jarque-Bera (JB): 286826.053

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

0.00

23.4

Prob(JB):

Cond. No.

Discussions:

Skew:

Kurtosis:

-0.331

35.100

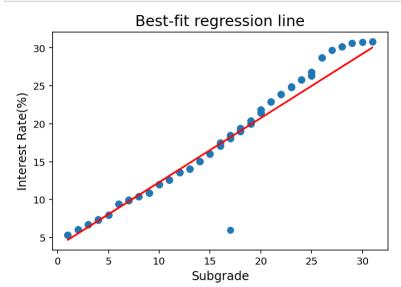
- The coefficient for sub_grade is 0.8457, and its corresponding p-value is very low (almost 0). That means the coefficient is statistically significant.
- R-squared value is 0.986, which means that 98.6% of the interest rate variance can be explained by the subgrade column using this line.
- Prob (F-statistic) has a very low p-value, practically zero, which gives us that the model fit is statistically significant.

Since the fit is significant, let's go ahead and visualize how well the straight-line fits the scatter plot between sub_grade and interest_rate columns.

2.2 Visualization of the Regression Line

From the parameters shown above, we have obtained the values of the intercept and the slope of the straight line. The equation of the line is $interest\ rate = 3.8372 + 0.8457 * subgrade$

```
In [63]: # Visualizing the regression line
fig, ax = plt.subplots(figsize=(6,4))
ax.scatter(X_train, y_train)
ax.plot(X_train, 3.8372 + 0.8457*X_train, 'r')
ax.set_title('Best-fit regression line', fontsize = 15)
ax.set_xlabel('Subgrade', fontsize = 12)
ax.set_ylabel('Interest Rate(%)', fontsize = 12)
plt.show()
```



2.3 Residual Analysis

One of the major assumptions of the linear regression model is the error terms are normally distributed.

```
Error = y - \hat{y}
```

where y is the actual y value, and \hat{y} is the predicted y value.

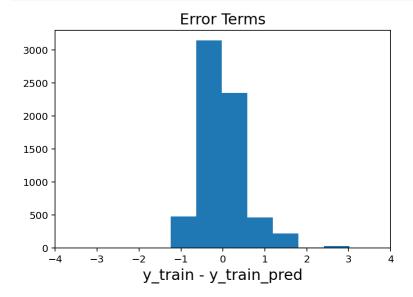
Now from the dataset, we have to predict the y value from the training dataset of X using the predict attribute. After that, we'll create the error terms(Residuals) from the predicted data.

```
In [64]: # Predicting y_value using traingn data of X
y_train_pred = lr.predict(X_train_sm)

# Creating residuals from the y_train data and predicted y_data
res = (y_train - y_train_pred)
```

Now, let's plot the histogram of the residuals and see whether it looks like normal distribution or not.

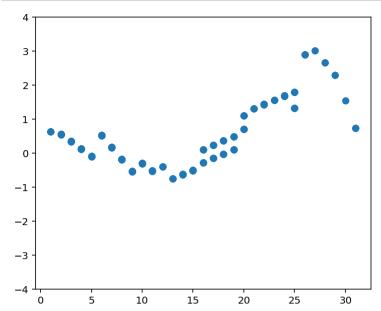
```
In [65]: # Plotting the histogram using the residual values
fig, ax = plt.subplots(figsize=(6,4))
n, bins, patches = ax.hist(res, bins=25)
ax.set_title('Error Terms', fontsize = 15)
ax.set_xlabel('y_train - y_train_pred', fontsize = 15)
ax.set_xlim(-4, 4)
plt.show()
```



As we can see, the residuals are following the normal distribution graph with a mean 0.

Now, make sure that the residuals are not following any specific pattern.

```
In [66]: # Looking for any patterns in the residuals
fig, ax = plt.subplots(figsize=(6,5))
ax.scatter(X_train, res)
ax.set_ylim(-4, 4)
plt.show()
```



Since the Residuals follow a normal distribution and do not follow any specific pattern, we can use the linear regression model we have built to evaluate test data.

2.4. Predictions on the Test Data and Evaluations

Now that we have fitted the regression line on our train dataset, we can make some predictions to the test data. Similar to the training dataset, we have to add_constant to the test data and predict the y values using the predict attribute present in the statsmodel.

```
In [67]: # Adding a constant to X_test
X_test_sm = sm.add_constant(X_test)

# Predicting the y values corresponding to X_test_sm
y_test_pred = lr.predict(X_test_sm)

# Printing the first 15 predicted values
y_test_pred
Out[67]: 2044 13.985098
```

```
3989
        13.985098
4833
        15.676416
5141
         9.756804
1861
         5.528510
          . . .
8123
        12.293781
1380
         9.756804
9262
         9.756804
6231
        16.522075
1699
        13.139439
Length: 2863, dtype: float64
```

Now, let's calculate the R2 value for the above-predicted y-values. We can do that by merely importing the r2_score library from sklearn.metrics package.

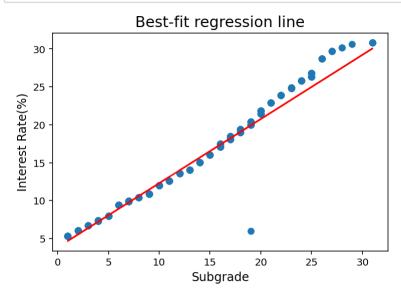
```
In [68]: # Checking the R-squared value
r_squared = r2_score(y_test, y_test_pred)
r_squared
```

Out[68]: 0.9846913347652099

Since the R2 value on training data is 0.986, the R2 value on test data is within 5% of the R2 value on training data. In this case we can conclude that the model is pretty stable. This means, what the model has learned on the training set can generalize on the unseen test set.

Let's visualize the line on the test data.

```
In [69]: fig, ax = plt.subplots(figsize=(6,4))
    ax.scatter(X_test, y_test)
    ax.plot(X_test, y_test_pred, 'r')
    ax.set_title('Best-fit regression line', fontsize = 15)
    ax.set_xlabel('Subgrade', fontsize = 12)
    ax.set_ylabel('Interest Rate(%)', fontsize = 12)
    plt.show()
```



3. Modeling Approach 2: Linear Regression Using sklearn

3.1 Perform Linear Regression

For simple linear regression, we need to add a column to perform the regression fit properly.

```
In [71]: # Shape of the train set without adding column
    print("The shape of X_train before adding a column is ", X_train_lm.shape)

# Adding additional column to the train and test data
    X_train_lm = X_train_lm.values.reshape(-1,1)
    X_test_lm = X_test_lm.values.reshape(-1,1)

print("The shape of X_train after adding a column is ", X_train_lm.shape)
    print("The shape of X_test after adding a column is ", X_test_lm.shape)
```

The shape of X_train before adding a column is (6678,)
The shape of X_train after adding a column is (6678, 1)
The shape of X_test after adding a column is (2863, 1)

Now we can conduct the linear regression using sklearn.linear_model

```
In [72]: # Creating an object of Linear Regression
lm = LinearRegression()

# Fit the model using .fit() method
lm.fit(X_train_lm, y_train_lm)

# Intercept value
print("Intercept :",lm.intercept_)

# Slope value
print('Slope :',lm.coef_)
```

Intercept : 3.8371927815254256
Slope : [0.84565879]

The straight-line equation we get for the above values is,

 $interest\ rate = 3.8372 + 0.8467 * subgrade$

If we observe, the equation we got here is the same as the one we got in the statsmodel .

3.2 Predictions on the Test Data and Evaluations¶

```
In [73]: # Making Predictions of y_value
y_train_pred = lm.predict(X_train_lm)
y_test_pred = lm.predict(X_test_lm)

# Comparing the r2 value of both train and test data
print(r2_score(y_train,y_train_pred))
print(r2_score(y_test,y_test_pred))
```

0.9863087206973497
0.9846913347652099

Same as the statesmodel, the R² value on test data is within 5% of the R² value on training data. We can apply the model to the unseen test set in the future.

4. Conclusions

- Data cleaning is performed to the original dataset. Unrelevant columns and outlier rows are removed.
- After calculating the correlation coefficients, it is found that sub_grade is able to dominate the target variable interest_rate .
- In this case, we can simply use numerized sub_grade value to build up linear regression model in statsmodel and sklearn. Both of the model predictions have shown good agreement with the actual values.
- Model evaluations are made to both modeling approaches and r2 score is used to prove the model has enough robustness and stability.

5. Reference

https://towardsdatascience.com/simple-linear-regression-model-using-python-machine-learning-eab7924d18b4 (https://towardsdatascience.com/simple-linear-regression-model-using-python-machine-learning-eab7924d18b4)

In []: