

Fluid-Structure Interaction Analysis of Pulsatile Flow in Arterial Aneurysms with Physics-Informed Neural Networks and Computational Fluid Dynamics

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1 Physics-Informed Neural Networks

1.1 overview

High-fidelity Computational Fluid Dynamics (CFD) simulations, as outlined in Section 2.4, offer precise insights into arterial hemodynamics and are central to modeling fluid dynamics in complex vascular geometries. However, these simulations can be both computationally expensive and time-consuming, especially when dealing with patient-specific anatomies or conducting numerous parameter sweeps. Such challenges are further compounded by the need for significant domain expertise to refine meshes, tune solvers, and interpret results.

Physics-Informed Neural Networks (PINNs), first introduced by Raissi et al. [1], have emerged as a powerful alternative that combines the strengths of traditional deep learning with established physics-based modeling. Rather than relying exclusively on data-driven learning, PINNs integrate the governing partial differential equations (PDEs) in this case, the continuity and momentum conservation equations (Section 2.2) directly into the network’s loss function. This approach ensures that the neural network is “informed” by the physical laws of fluid motion, guiding it toward realistic flow solutions even when labeled data are sparse or imperfectly measured.

By incorporating PDE residuals into the loss function, PINNs naturally embed a priori knowledge of fluid physics, allowing the model to learn physically plausible flow fields with fewer labeled samples than a purely data-driven neural network. This built-in adherence to physical constraints also helps mitigate overfitting and reduces the likelihood of predicting unphysical solutions. As a result, PINNs have

the potential to complement or partially replace expensive CFD simulations, thereby lowering computational overheads and accelerating research pipelines.

In this study, we combine PINNs with traditional CFD data to estimate core hemodynamic variables such as pressure, velocity components, and wall shear stress (WSS) across healthy and Marfan Syndrome aortic geometries presented in (Section 2.1). This unified approach enables direct comparisons of velocity patterns, shear forces, and other critical flow indicators between non-pathological and aneurysmal models, providing valuable information for understanding the progression of vascular disease. The following sections detail the formulation, architecture, and training strategy of the PINNs used in this study.

1.2 Formulation of Physics-Informed Neural Networks

Modelling pulsatile flow in arterial segments necessitates the Navier–Stokes and continuity equations to capture essential haemodynamic effects. Let $\mathbf{u} = (u, v, w)$ denote the velocity field, p the pressure, ρ the fluid density, and μ the dynamic viscosity. In vector form, the governing equations are:

$$\nabla \cdot \mathbf{u} = 0, \quad \rho \frac{\partial \mathbf{u}}{\partial t} + \rho(\mathbf{u} \cdot \nabla) \mathbf{u} = -\nabla p + \mu \nabla^2 \mathbf{u}. \quad (1)$$

The associated boundary conditions involve a no-slip condition on the arterial walls ($\mathbf{u} = \mathbf{0}$ on $\partial\Omega_{\text{wall}}$), zero relative pressure at the outlet, and a pulsatile inlet velocity on $\partial\Omega_{\text{inlet}}$ (Section 2.3). These boundary and inlet constraints are incorporated into the Physics-Informed Neural Network through penalty terms in the loss function, thereby enforcing consistency between the network’s predictions and the specified physical conditions. Temporal dependence is explicitly modelled to reflect the transient nature of blood flow.

Within the PINN framework, neural networks approximate the velocity field \mathbf{u} , pressure p , and wall shear stress (WSS) components τ_x, τ_y, τ_z as functions of the spatial coordinates (x, y, z) and time t . The network architecture is trained to minimise the physics residual loss, which quantifies the deviation of the predicted solutions from the Navier–Stokes and continuity equations.

$$u(x, y, z, t), \quad v(x, y, z, t), \quad w(x, y, z, t), \quad p(x, y, z, t),$$

and the three wall shear stress (WSS) components

$$\tau_x(x, y, z, t), \quad \tau_y(x, y, z, t), \quad \tau_z(x, y, z, t).$$

Collectively, these variables capture the spatiotemporal evolution of blood flow and the shear forces acting on the vessel walls.

Let $F(\cdot)$ represent the non-linear operator corresponding to the Navier–Stokes system. The *physics residual* loss term evaluates how closely the PINN’s predictions adhere to the governing equations:

$$L_{\text{physics}} = \|F(\mathbf{u}, p)\|_2, \quad (2)$$

where $\|\cdot\|_2$ denotes the Euclidean norm. By minimising this residual, the network is driven to learn solutions consistent with the Navier–Stokes and continuity equations, even in regions where no direct labels are available.

Arterial boundaries impose $\mathbf{u} = \mathbf{0}$ at the vessel walls and zero pressure at the outlet, while a prescribed pulsatile velocity profile is enforced at the inlet:

$$L_{\text{boundary}} = \|\mathbf{u}|_{\partial\Omega_{\text{wall}}} - \mathbf{0}\|_2, \quad L_{\text{inlet}} = \|\mathbf{u}|_{\Gamma_{\text{inlet}}} - \mathbf{u}_{\text{inlet}}(t)\|_2. \quad (3)$$

These terms penalise any deviation of the network’s predictions from the specified boundary conditions, thus reinforcing physically realistic flow fields at the walls and inflow region.

The CFD data (e.g. pressure, velocity, and WSS) are integrated into the loss function. Let \mathbf{u}_{NN} and p_{NN} denote the PINN’s predicted velocity and pressure, while \mathbf{u}_{CFD} and p_{CFD} are the corresponding CFD reference fields. Similarly, τ_{NN} and τ_{CFD} refer to the predicted and CFD-derived WSS. The data-fitting loss is given by:

$$L_{\text{data}} = \|\mathbf{u}_{\text{NN}} - \mathbf{u}_{\text{CFD}}\|_2 + \|p_{\text{NN}} - p_{\text{CFD}}\|_2 + \|\tau_{\text{NN}} - \tau_{\text{CFD}}\|_2. \quad (4)$$

The total loss combines physics, boundary, inlet, and data objectives:

$$L_{total} = \lambda_{\text{physics}} L_{\text{physics}} + \lambda_{\text{boundary}} L_{\text{boundary}} + \lambda_{\text{inlet}} L_{\text{inlet}} + \lambda_{\text{data}} L_{\text{data}}, \quad (5)$$

where λ_{physics} , $\lambda_{\text{boundary}}$, λ_{inlet} , λ_{data} are self-adaptive weighting coefficients [2]. These learnable parameters automatically balance the importance of each loss component during training, ensuring that the PINN respects both the fundamental equations of fluid motion and the given available CFD data. The self-adaptive weighting mechanism is explained further in Section 1.3.1.

1.3 Neural Network Architecture

Neural network architecture plays a crucial role in the performance and generalisation capabilities of PINNs. In this study, We train separate PINNs for pressure p , velocity components (u, v, w) , and the three WSS components (τ_x, τ_y, τ_z) , all time dependant (t). Each network is a feed-forward, fully connected architecture with $L = 10$ hidden layers and $N = 64$ neurons per layer. The Swish activation function [3] is employed to promote smooth gradients. batch normalization is applied to each layer to stabilize training, and all weights are initialized using Kaiming normal [4] to ensure stable gradient flow.

The Swish activation function [3] is defined as:

$$\text{Swish}(x) = x \sigma(\beta x), \quad (6)$$

where β is a learnable parameter and $\sigma(\cdot)$ is the sigmoid function. This choice often yields faster convergence compared to ReLU or other activations.

1.3.1 Self-Adaptive Loss Weighting

Balancing multiple loss components is a fundamental challenge in training Physics-Informed Neural Networks (PINNs), particularly in multi-physics scenarios where various physical phenomena and boundary conditions must be simultaneously satisfied. In our study, the primary loss components include the physics residuals derived from the governing partial differential equations (PDEs), boundary conditions, inlet condi-

tions, and supervised data from Computational Fluid Dynamics (CFD) simulations. Improper weighting of these components can lead to suboptimal training outcomes, such as overfitting to certain loss terms or failure to adequately satisfy physical laws.

To address this challenge, we implement a self-adaptive loss weighting scheme inspired by McCleny and Braga-Neto [2]. Specifically, we introduce learnable parameters $\log \lambda_i$ for each loss component $i \in \{\text{phys}, \text{bound}, \text{inlet}, \text{data}\}$. These parameters are optimized alongside the neural network weights during training. The weights λ_i are defined as the exponential of the corresponding log-parameters:

$$\lambda_i = \exp(\log \lambda_i), \quad (7)$$

This parameterization ensures that each λ_i remains positive throughout the training process, thereby maintaining the integrity of the loss scaling. By optimizing $\log \lambda_i$, the network can autonomously adjust the relative importance of each loss component based on the training dynamics, without manual tuning of hyperparameters.

The optimization of $\log \lambda_i$ allows the network to dynamically balance these components, mitigating the risk of any single loss term dominating the training process [5]. This adaptive mechanism facilitates a more stable and efficient convergence, as the network can prioritize loss components that require greater emphasis based on their current contribution to the total loss.

1.4 Training of the PINNs

The PINN framework was implemented using the PyTorch library [6], leveraging its automatic differentiation capabilities for efficient computation of PDE residuals and trained on a high-performance computing cluster with NVIDIA Rtx8000.

The input Spatiotemporal data points (x_j, y_j, z_j, t_j) which are the geometric were randomly sampled from the aortic geometries and over the cardiac cycle. The geometric and variables data were normalized using Min-Max scaling to facilitate efficient training. The PINNs were trained using the AdamW optimizer [7] with an initial learning rate of 1×10^{-4} and momentum parameters $\beta = (0.9, 0.999)$. The weight decay was set to 1×10^{-4} to prevent overfitting. A StepLR scheduler reduced the learning rate by a factor of $\gamma = 0.9$ every 200 epochs to facilitate finer convergence.

Algorithm 1 Self-Adaptive Loss Weighting in PINNs

Require: Initial network weights θ , initial $\log \lambda_i$, learning rates for θ and $\log \lambda_i$
Ensure: Trained network weights θ^* and optimized λ_i^*

- 1: **while** not converged **do**
- 2: Sample mini-batch of training points
- 3: Forward pass to compute predictions $\mathbf{u}_{\text{NN}}, p_{\text{NN}}, \boldsymbol{\tau}_{\text{NN}}$
- 4: Compute individual loss components:
 - 5: $\mathcal{L}_{\text{phys}} = \|F(\mathbf{u}_{\text{NN}}, p_{\text{NN}})\|_2^2$
 - 6: $\mathcal{L}_{\text{bound}} = \|\mathbf{u}_{\text{NN}}|_{\partial\Omega_{\text{wall}}} - \mathbf{0}\|_2^2$
 - 7: $\mathcal{L}_{\text{inlet}} = \|\mathbf{u}_{\text{NN}}|_{\Gamma_{\text{inlet}}} - \mathbf{u}_{\text{inlet}}(t)\|_2^2$
 - 8: $\mathcal{L}_{\text{data}} = \|\mathbf{u}_{\text{NN}} - \mathbf{u}_{\text{CFD}}\|_2^2 + \|p_{\text{NN}} - p_{\text{CFD}}\|_2^2 + \|\boldsymbol{\tau}_{\text{NN}} - \boldsymbol{\tau}_{\text{CFD}}\|_2^2$
 - 9: $\mathcal{L}_{\text{total}} = \lambda_{\text{phys}} \mathcal{L}_{\text{phys}} + \lambda_{\text{bound}} \mathcal{L}_{\text{bound}} + \lambda_{\text{inlet}} \mathcal{L}_{\text{inlet}} + \lambda_{\text{data}} \mathcal{L}_{\text{data}}$
- 10: Backpropagate the total loss to compute gradients for θ and $\log \lambda_i$
- 11: Update network weights $\theta \leftarrow \theta - \eta_\theta \nabla_\theta \mathcal{L}$
- 12: Update log-weights $\log \lambda_i \leftarrow \log \lambda_i - \eta_\lambda \nabla_{\log \lambda_i} \mathcal{L}$
- 13: StepLR scheduler updates learning rates η_θ and η_λ every N epochs
- 14: **end while**
- 15: **Return** θ^*, λ_i^*

Training was conducted using mixed-precision arithmetic via PyTorch’s ‘`torch.cuda.amp`’ to enhance computational efficiency and reduce memory consumption without sacrificing model accuracy [8]. The training process iterated over a maximum of 1000 epochs, with early stopping implemented to halt training if the validation loss did not decrease for 5 consecutive epochs. Gradient clipping was applied to prevent exploding gradients the gradients are clipped to a maximum norm of 1.0, ensuring training stability.

1.5 Relevance to Aneurysm Studies

By alleviating the need to run complete CFD simulations whenever boundary conditions or model geometries change, PINNs can serve as rapid surrogates for iterative parameter sweeps, sensitivity analyses, or real-time clinical decision-making. This synergy between classical CFD and PINNs ensures that accurate fluid physics are retained, while the neural network structure offers improved computational scaling and the capacity to generalise to different flow conditions with minimal retraining overhead. Consequently, for the case of Marfan Syndrome aortic aneurysms, PINNs provide a promising pathway for expediting haemodynamic evaluations and exploring a range of inflow waveforms, wall properties, or geometric variations in a fraction of the time typically required by CFD alone.

Note: All codes and numerical experiments for the PINN-based aneurysm flow analyses were implemented in Python using PyTorch, with the self-adaptive weighting and physics-based PDE residuals integrated into the backpropagation routine. The specific hyperparameters and training protocol are as outlined in this section, ensuring reproducibility and transparency in the results reported herein.

1.6 Results

The PINN-based simulations were validated against benchmark CFD data for healthy and Marfan Syndrome aortic geometries, demonstrating excellent agreement in velocity profiles, pressure distributions, and wall shear stress patterns. The PINNs accurately captured the complex flow dynamics within the aneurysm sac, including vortex formation, flow separation, and recirculation zones. The self-adaptive loss weighting mechanism effectively balanced the physics residuals, boundary conditions, and data-fitting objectives, ensuring that the network learned realistic flow solutions while adhering to the governing Navier–Stokes equations. The figures below illustrate the comparison between PINN predictions and CFD reference data for pressure, and wall shear stress in the aortic aneurysms.

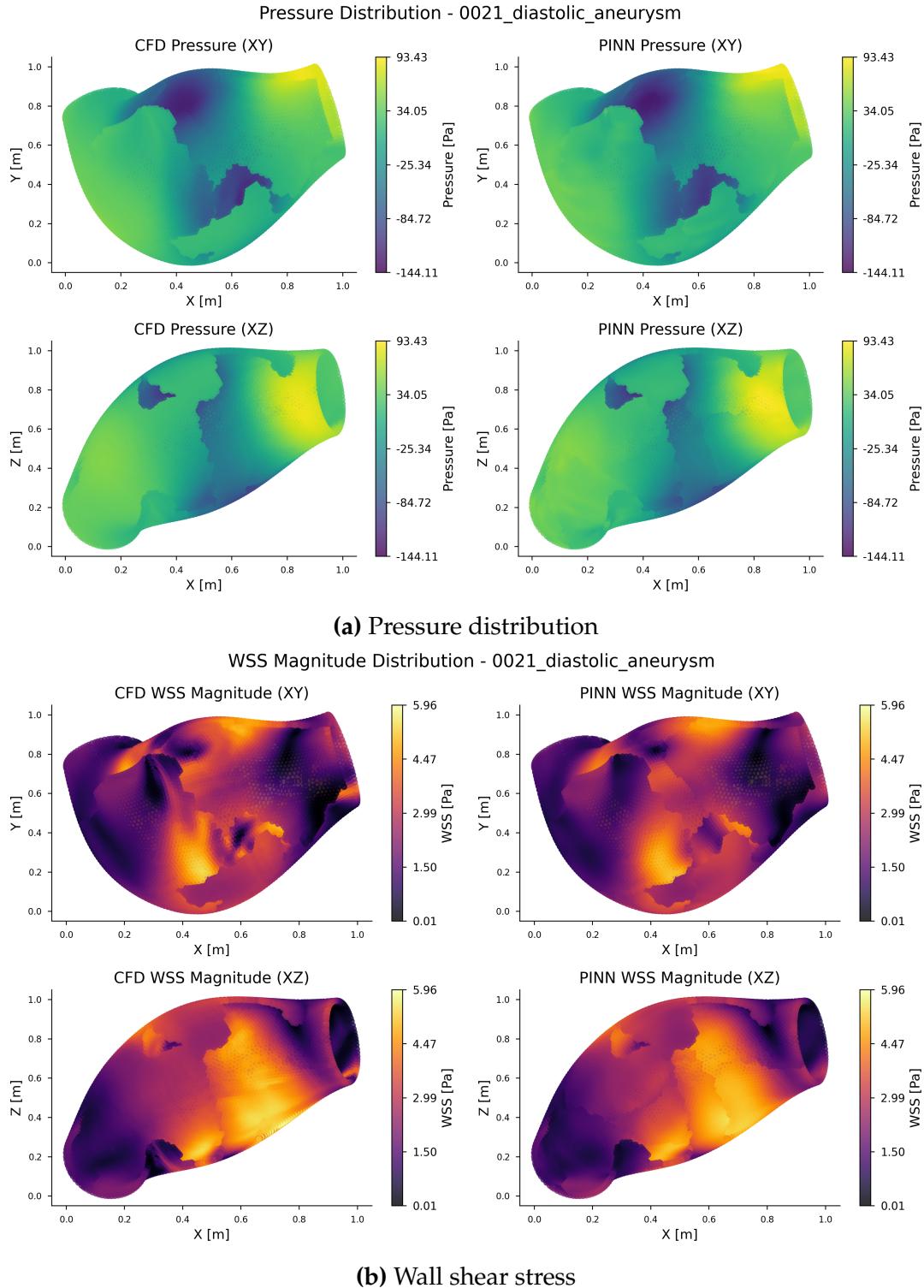


Figure 1: Von Mises stress (Pa) and wall shear stress contours for diseased cases. Figures a–d in each show the xy and xz planes for case 0021 diastolic aneurysm comparison between CFD and PINN results.

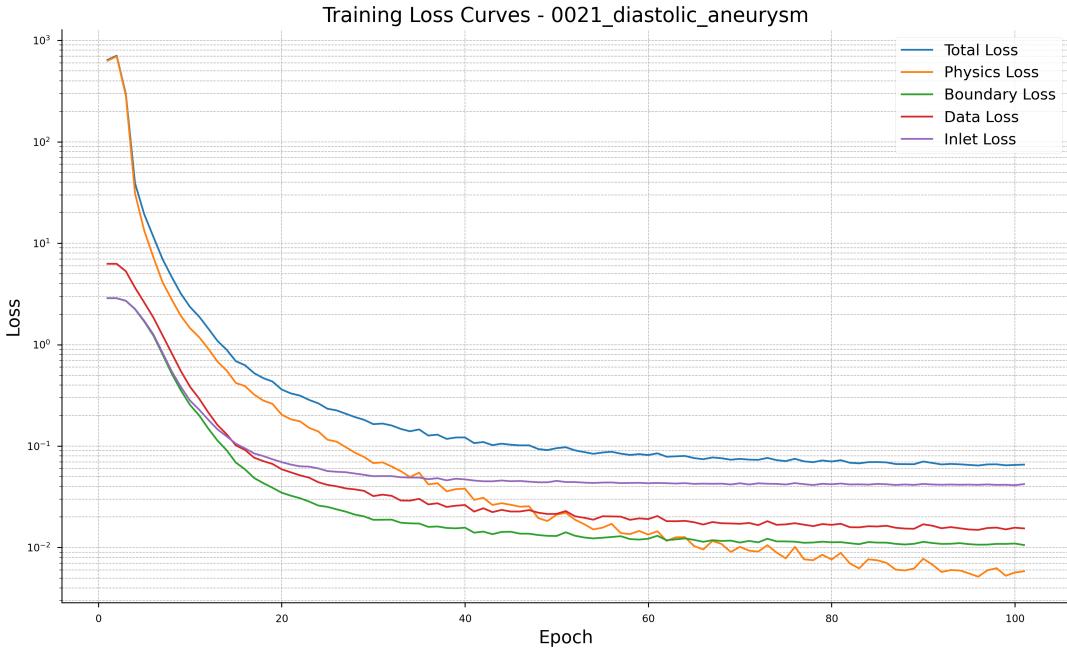


Figure 2: Loss curves for the PINN training process, showing the evolution of the physics, boundary, inlet, and data-fitting losses over 1000 epochs. The self-adaptive loss weighting mechanism effectively balances the contributions of each loss component, ensuring that the network learns realistic flow solutions while adhering to the governing Navier–Stokes equations.

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