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```
% Chan
function Chan_HW4()

l1=.030;
l2=.050;
l3=.10;
b = 0.5;
bodyVel = 0.1;
h=.1; %(m) height of the robot.
D=l1+l2; %(m) Distance between the foot tip and hip joint from top
view
R=.220; % distance of foot tip to COG or center of rotation
u=(b/(1-b))*bodyVel; % average swing velocity of the leg wrt the body
u=bodyVel/(1-b); % average swing velocity of the leg wrt the ground
a=pi/6; % Crab Angle
L=.16; % Stride Length which is the amount of COG displacement in one
cycle time.
T= L/bodyVel; % Cycle Period
Tt=(1-b)*T;
```

Gait Planner

This code has been adapted from the example code given by Professor Agheli

```
% segment into partitions 6 equal timesteps according to example
time = linspace(0,Tt,6);

xdotmaxf_g=2*(time(6)-time(1))*u/((time(5)-time(2))+(time(4)-
time(3)));

for i = 1:6
xPositions(i,:) = [-L/2;-L/2;-L/4;L/4;L/2;L/2];
zPositions(i,:) = [0;h/2;h;h;h/2;0];
end

xdot = [0;0;xdotmaxf_g;xdotmaxf_g;0;0];
zdot = [0;xdotmaxf_g;0;0;-xdotmaxf_g;0];
alphaH=[-30*pi/180, 30*pi/180, -90*pi/180, 90*pi/180, -150*pi/180,
150*pi/180];

% % xPositions_g = xPositions + L/2;
```

```

xb_g(1,1)=-((1-b)/2)*L-D*cos(alphaH(1)); % frame b is a frame attached
to the hip joint whose
xb_g(2,1)=-((1-b)/2)*L-D*cos(alphaH(2));
xb_g(3,1)=-((1-b)/2)*L;
xb_g(4,1)=-((1-b)/2)*L;
xb_g(5,1)=-((1-b)/2)*L-D*cos(alphaH(5));
xb_g(6,1)=-((1-b)/2)*L-D*cos(alphaH(6));

% x axis is parallel to the x axis of frame g (Gi).
zb_g(1,1)=h;
zb_g(2,1)=h;
zb_g(3,1)=h;
zb_g(4,1)=h;
zb_g(5,1)=h;
zb_g(6,1)=h;

dt=Tt/5;
xdotb_g=bodyVel;
zdotb_g=0;

for i=1:6
    for t=1:5 % 5 is because of time dividing to 5 equal extents.
        xb_g(i,t+1)=xb_g(i,t)+xdotb_g*dt;
        zb_g(i,t+1)=zb_g(i,t)+zdotb_g*dt;
    end
    for t=1:6
        xf_b(i,t)=xPositions(i,t)-xb_g(i,t);
        zf_b(i,t)=zPositions(i,t)-zb_g(i,t);
    end
end
% ****xf_b(t) and zf_b(t) ARE THE SAME FOR ALL LEGS i=1,2,...,6. But
yf_b
% differs as follow. For each leg, yf_b is the same for all t.
yf_b=[D*sin(30*pi/180), -D*sin(30*pi/180), D, -D, D*sin(30*pi/180),
-D*sin(30*pi/180)];

for i=1:6 % this is because of 6 legs
    for j=1:6 % this is because we have divided out T to 6 dt.
        %xf_H(i,j)=RH_b*xf_b(i,j);

        xf_H(i,j)=[cos(alphaH(i)), -
sin(alphaH(i)), 0]*[xf_b(i,j);yf_b(i);zf_b(i,j)];

        yf_H(i,j)=[sin(alphaH(i)), cos(alphaH(i)), 0]*[xf_b(i,j);yf_b(i);zf_b(i,j)];
        zf_H(i,j)=zf_b(i,j);
    end
end
makePosnVelPlot(time,xdot,zdot,xPositions,zPositions,xf_b,zf_b)

```

IK

```

for i=1:6 % for all 6 legs
    for j=1:6 % time discrete

```

```

        Alpha(i,j)=(atan(yf_H(i,j)/xf_H(i,j)));
        l(i,j)=sqrt(yf_H(i,j)^2+xf_H(i,j)^2);
        d(i,j)=sqrt(zf_H(i,j)^2+(l(i,j)-l1)^2);
        Beta(i,j)=acos((l2^2+d(i,j)^2-l3^2)/(2*l2*d(i,j)))-
atan(abs(zf_H(i,j))/(l(i,j)-l1));
        Gamma(i,j)=pi-(acos((l2^2+l3^2-d(i,j)^2)/(2*l2*l3)));
%         Beta(i,j)=Beta(i,j)*180/pi;
%         Gamma(i,j)=pi-Gamma(i,j);
    end
end
A=Alpha*180/pi
B=Beta*180/pi
G=Gamma*180/pi

```

A =

```

    23.7940    41.6312    17.0142    -8.4491   -12.2928    -9.8961
   -23.7940   -41.6312   -17.0142     8.4491    12.2928     9.8961
    26.5651    34.9920    21.8014   -21.8014   -34.9920   -26.5651
   -26.5651   -34.9920   -21.8014    21.8014    34.9920    26.5651
     9.8961    12.2928     8.4491   -17.0142   -41.6312   -23.7940
    -9.8961   -12.2928    -8.4491    17.0142    41.6312    23.7940

```

B =

1.0e+02 *

Columns 1 through 4

```

   -0.0536 + 0.0000i    0.8423 + 0.0000i    1.8000 - 0.9661i    0.9930 +
0.0000i
   -0.0536 + 0.0000i    0.8423 + 0.0000i    1.8000 - 0.9661i    0.9930 +
0.0000i
   -0.0051 + 0.0000i    0.5642 + 0.0000i    1.4069 + 0.0000i    1.4069 +
0.0000i
   -0.0051 + 0.0000i    0.5642 + 0.0000i    1.4069 + 0.0000i    1.4069 +
0.0000i
   -0.0810 + 0.0000i    0.3582 + 0.0000i    0.9930 + 0.0000i    1.8000 -
0.9661i
   -0.0810 + 0.0000i    0.3582 + 0.0000i    0.9930 + 0.0000i    1.8000 -
0.9661i

```

Columns 5 through 6

```

   0.3582 + 0.0000i   -0.0810 + 0.0000i
   0.3582 + 0.0000i   -0.0810 + 0.0000i
   0.5642 + 0.0000i   -0.0051 + 0.0000i
   0.5642 + 0.0000i   -0.0051 + 0.0000i
   0.8423 + 0.0000i   -0.0536 + 0.0000i
   0.8423 + 0.0000i   -0.0536 + 0.0000i

```

G =

1.0e+02 *

Columns 1 through 4

1.0222 + 0.0000i	1.7014 + 0.0000i	1.8000 - 0.3470i	1.2887 + 0.0000i
1.0222 + 0.0000i	1.7014 + 0.0000i	1.8000 - 0.3470i	1.2887 + 0.0000i
0.8407 + 0.0000i	1.2284 + 0.0000i	1.5916 + 0.0000i	1.5916 + 0.0000i
0.8407 + 0.0000i	1.2284 + 0.0000i	1.5916 + 0.0000i	1.5916 + 0.0000i
0.6026 + 0.0000i	0.8825 + 0.0000i	1.2887 + 0.0000i	1.8000 - 0.3470i
0.6026 + 0.0000i	0.8825 + 0.0000i	1.2887 + 0.0000i	1.8000 - 0.3470i

Columns 5 through 6

0.8825 + 0.0000i	0.6026 + 0.0000i
0.8825 + 0.0000i	0.6026 + 0.0000i
1.2284 + 0.0000i	0.8407 + 0.0000i
1.2284 + 0.0000i	0.8407 + 0.0000i
1.7014 + 0.0000i	1.0222 + 0.0000i
1.7014 + 0.0000i	1.0222 + 0.0000i

```
ydotf_b=0;
for t=1:6
    xdotf_b(t)=xdot(t)-xdotb_g;
    zdotf_b(t)=zdot(t)-zdotb_g;
end
for i=1:6
    for j=1:6
        xdotf_H(i,j)=[cos(alphaH(i)), -
sin(alphaH(i)), 0]*[xdotf_b(j);ydotf_b;zdotf_b(j)];

        ydotf_H(i,j)=[sin(alphaH(i)), cos(alphaH(i)), 0]*[xdotf_b(j);ydotf_b;zdotf_b(j)];
        zdotf_H(i,j)=zdotf_b(j);
    end
end
for j=1:6 % time
    for i=1:6 % leg numnber
        theta1=Alpha(i,j);
        theta2=Beta(i,j);
        theta3=Gamma(i,j);
        J(1,1)=-(-sin(theta1)*sin(theta2)*cos(theta3)-
sin(theta1)*cos(theta2)*sin(theta3))*l3-sin(theta1)*l2*cos(theta2)-
l1*sin(theta1);
        J(1,2)=-(-
cos(theta1)*sin(theta2)*sin(theta3)+cos(theta1)*cos(theta2)*cos(theta3))*l3-
cos(theta1)*l2*sin(theta2);
```

```

        J(1,3)=(cos(theta1)*sin(theta2)*sin(theta3)-
cos(theta1)*cos(theta2)*cos(theta3))*l3;
        J(2,1)=-
(cos(theta1)*cos(theta2)*sin(theta3)+cos(theta1)*sin(theta2)*cos(theta3))*l3+cos(t
        J(2,2)=-(-
sin(theta1)*sin(theta2)*sin(theta3)+sin(theta1)*cos(theta2)*cos(theta3))*l3-
sin(theta1)*l2*sin(theta2);
        J(2,3)=-(-
sin(theta1)*sin(theta2)*sin(theta3)+sin(theta1)*cos(theta2)*cos(theta3))*l3;
        J(3,1)=0;
        J(3,2)=-(-cos(theta2)*sin(theta3)-sin(theta2)*cos(theta3))*l3-
l2*cos(theta2);
        J(3,3)=-(-cos(theta2)*sin(theta3)-sin(theta2)*cos(theta3))*l3;

        Thetadot(i,j,:)=inv(J)*[xdotf_H(i,j);ydotf_H(i,j);zdotf_H(i,j)];
    end
end

```

Thetadot

Thetadot(:,:,1) =

Columns 1 through 4

```

-4.1373 + 0.0000i    0.7226 + 0.0000i    0.1274 + 0.5691i   -1.5236 +
0.0000i
 4.1373 + 0.0000i   -0.7226 + 0.0000i   -0.1274 - 0.5691i    1.5236 +
0.0000i
-4.6175 + 0.0000i    1.4535 + 0.0000i   -4.7590 + 0.0000i   -4.7590 +
0.0000i
 4.6175 + 0.0000i   -1.4535 + 0.0000i    4.7590 + 0.0000i    4.7590 +
0.0000i
 65.3319 + 0.0000i   -2.4751 + 0.0000i   -1.5236 + 0.0000i    0.1274 +
0.5691i
-65.3319 + 0.0000i    2.4751 + 0.0000i    1.5236 + 0.0000i   -0.1274 -
0.5691i

```

Columns 5 through 6

```

-2.4751 + 0.0000i   65.3319 + 0.0000i
 2.4751 + 0.0000i  -65.3319 + 0.0000i
 1.4535 + 0.0000i   -4.6175 + 0.0000i
-1.4535 + 0.0000i    4.6175 + 0.0000i
 0.7226 + 0.0000i   -4.1373 + 0.0000i
-0.7226 + 0.0000i    4.1373 + 0.0000i

```

Thetadot(:,:,2) =

1.0e+02 *

Columns 1 through 4

```

-0.0554 + 0.0000i -0.0212 + 0.0000i  0.0000 - 0.2246i -0.0884 +
0.0000i
-0.0554 + 0.0000i -0.0212 + 0.0000i  0.0000 - 0.2246i -0.0884 +
0.0000i
-0.0860 + 0.0000i -0.1841 + 0.0000i  0.0276 + 0.0000i -0.0276 +
0.0000i
-0.0860 + 0.0000i -0.1841 + 0.0000i  0.0276 + 0.0000i -0.0276 +
0.0000i
-0.0299 + 0.0000i  1.3203 + 0.0000i  0.0884 + 0.0000i  0.0000 +
0.2246i
-0.0299 + 0.0000i  1.3203 + 0.0000i  0.0884 + 0.0000i  0.0000 +
0.2246i

```

Columns 5 through 6

```

-1.3203 + 0.0000i  0.0299 + 0.0000i
-1.3203 + 0.0000i  0.0299 + 0.0000i
 0.1841 + 0.0000i  0.0860 + 0.0000i
 0.1841 + 0.0000i  0.0860 + 0.0000i
 0.0212 + 0.0000i  0.0554 + 0.0000i
 0.0212 + 0.0000i  0.0554 + 0.0000i

```

Thetadot(:, :, 3) =

Columns 1 through 4

```

 2.7626 + 0.0000i -2.9630 + 0.0000i -6.4038 +22.4590i  7.8769 +
0.0000i
 2.7626 + 0.0000i -2.9630 + 0.0000i -6.4038 +22.4590i  7.8769 +
0.0000i
 4.2729 + 0.0000i 11.3147 + 0.0000i -1.5273 + 0.0000i  1.5273 +
0.0000i
 4.2729 + 0.0000i 11.3147 + 0.0000i -1.5273 + 0.0000i  1.5273 +
0.0000i
 1.1160 + 0.0000i -61.3695 + 0.0000i -7.8769 + 0.0000i  6.4038
-22.4590i
 1.1160 + 0.0000i -61.3695 + 0.0000i -7.8769 + 0.0000i  6.4038
-22.4590i

```

Columns 5 through 6

```

61.3695 + 0.0000i -1.1160 + 0.0000i
61.3695 + 0.0000i -1.1160 + 0.0000i
-11.3147 + 0.0000i -4.2729 + 0.0000i
-11.3147 + 0.0000i -4.2729 + 0.0000i
 2.9630 + 0.0000i -2.7626 + 0.0000i
 2.9630 + 0.0000i -2.7626 + 0.0000i

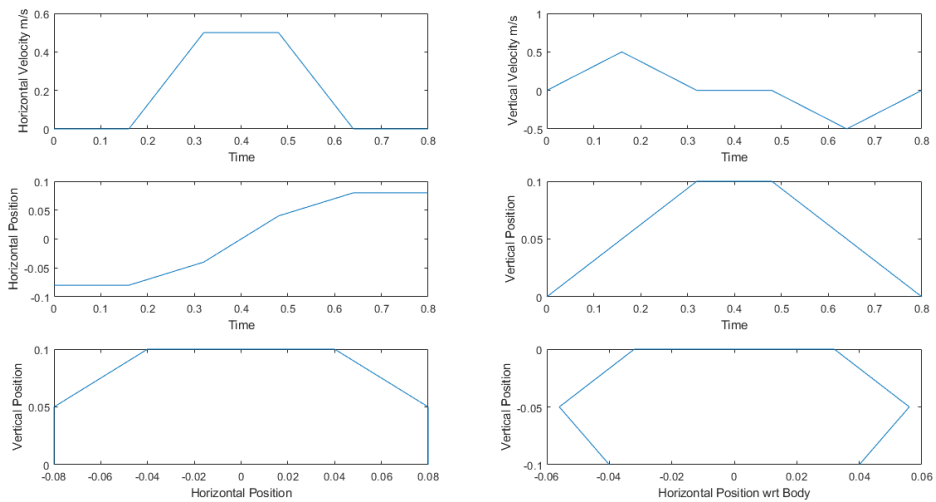
```

end

```
function makePosnVelPlot(t,xdoteval,zdoteval,xeval,zeval,xbody,zbody)
```

Plotting

```
figure('units','normalized','outerposition',[0 0 1 1])
hold on
subplot(3,2,1)
plot(t,xdoteval)
ylabel('Horizontal Velocity m/s')
xlabel('Time')
subplot(3,2,2)
plot(t,zdoteval)
ylabel('Vertical Velocity m/s')
xlabel('Time')
subplot(3,2,3)
plot(t,xeval(4,:))
ylabel('Horizontal Position')
xlabel('Time')
subplot(3,2,4)
plot(t,zeval(4,:))
ylabel('Vertical Position')
xlabel('Time')
subplot(3,2,5)
plot(xeval(4,:),zeval(4,:))
ylabel('Vertical Position')
xlabel('Horizontal Position')
subplot(3,2,6)
plot(xbody(4,:),zbody(4,:))
ylabel('Vertical Position')
xlabel('Horizontal Position wrt Body')
hold off;
```



```
end
```

