

Chapter 6

Our Tune for the Underlying Event

This section focus on our work in order to reproduce a similar tune to CP5 one for the underlying event and minimum bias observables. This is done to test the ability of MCNNTUNES of being one valid tool for the tuning of Monte Carlo generator with real data.

In order to validate MCNNTUNES as a good tool for the tuning we decide to firstly performer a simpler tune with only two free parameters and then try to reproduce CP5 [39] with all the five parameters variation.

6.1 Introduction

We have performed a different tune for the underlying event and minimum bias observables using the same distributions, listed in Chapter 4.3.1 and used in CP5 tune, so we expect to get a similar result from the tune using MCNNTUNES.

Just a quick reminder for the PYTHIA8 settings used in CP5 and in our tune:

- The PDF set used is NNPDF3.1 calculated to the NNLO [55];
- an α_s value equal for all the processes set to 0.118 and running with a NLO evolution.
- The ISR is also ordered according to rapidity.

In the tuning procedure we employed both the MCNNTUNES operation modes described in the previous chapter: PerBin and Inverse models.

6.2 First test: only two parameters variation

The first simplified test we perform is the tuning varying of only two parameters. The parameter chosen are the `MultipartonInteractions:pT0Ref` and `MultipartonInteractions:ecmPow`. These two parameters have been introduced in Section 3.1. The aim of this simplified test is to check the correct operation of MCNNTUNES in fact in a restricted parameters space it is simpler to learn the generator behavior and predict the corrects best values for the parameters.

Table 6.1 shows the parameters space used in this first case. The other parameters are set to the CP5 values (also these are reported in the table as a reminder).

Parameter Name	Value
MultipartonInteractions:pT0Ref [GeV]	[1.0 – 3.0]
MultipartonInteractions:ecmPow	[0.0 – 0.3]
MultipartonInteractions:coreRadius	0.7634
MultipartonInteractions:coreFraction	0.63
ColorReconnection:range	5.176

Table 6.1: Parameters space for the two parameters test. The other parameters are set to the CP5 default values.

Note: during this first part we don't use the two distributions related to the single diffractive and non single diffractive event selection for a bug on the routine of the analyses that have been fixed up before the real tune.

Let now discuss the results obtained for the test with the two models.

6.2.1 Per Bin Model results

The result we obtain for the PerBin model are reported in Table 6.2. The PerBin model estimation of the best parameters is performed by a loss function minimization. The output of the minimizer is reported in Fig. 6.1, the loss function (χ^2/dof) is the orange one, while the best parameter is marked by a solid red line.

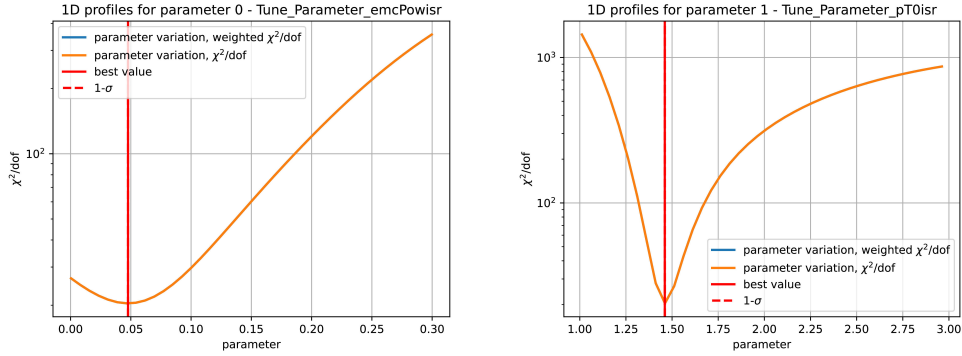


Figure 6.1: The figure shows the output of the minimizer for each parameter. The right one refers to the MPI:ecmPow while the left one to the MPI:pT0Ref. The orange line is the χ^2/DoF as a function of the parameter values, the solid red line indicated the best estimation for the parameters.

The estimated parameters for the tune are also reported in Table 6.2 with a comparison on CP5 boundary for each parameter. To be notice that the errors on the parameter estimated with PerBin model are not reported here because a correct error implementation, as the one described in Section 5.3.2, was not yet implemented in the software at the moment of this test, but here we can see an example of the old error estimation. The old errors estimation process was not working in fact the errors lines (dashed red lines) are overlapped to the line of the parameter estimation in both the figures. The predicted errors were 3 or 4 orders of magnitude smaller then the parameter values.

But as we expected the results we get are similar to the ones obtained from the

CP5 tune. The distributions obtained from the simulation using this parameters are shown below (Section 6.2.3) together with results from Inverse model and CP5.

Parameter	Value	CP5 (down & up)
<code>MultipartonInteractions:pT0Ref</code>	1.46064	1.41 – 1.46
<code>MultipartonInteractions:ecmPow</code>	0.04771	0.03

Table 6.2: Results for the PerBin model in two parameter variation test. The error evaluation was not correctly implemented yet and so the PerBin errors omitted in this table. The upper and lower limit for CP5 are also reported here for a direct comparison between the two tunes.

An important observation is that our model is more sensible to some parameter respect to others.

As an example, in Fig. 6.2 it is clear that our model is more sensible to the parameter `MultipartonInteractions:pT0Ref` (top) respect to `MultipartonInteractions:-ecmPow` (bottom). This is reflected in the output of the minimizer a greater sensibility gives a better defined minimum and vice versa. The top two panels show what happen when the distribution are very sensitive to the variation of the parameter as we can see on the left side the variation of the `pT0Ref` parameter leads to very different scenarios. This is reflected by the minimizer out in a well defined minimum and a smaller error on the parameter determination. A different scenario is displayed on the bottom panels of Fig. 6.2 where the distribution is less sensitive to the variation of the parameter `ecmPow` and so the minimum is less defined and so we are going to have a larger error on the estimation.

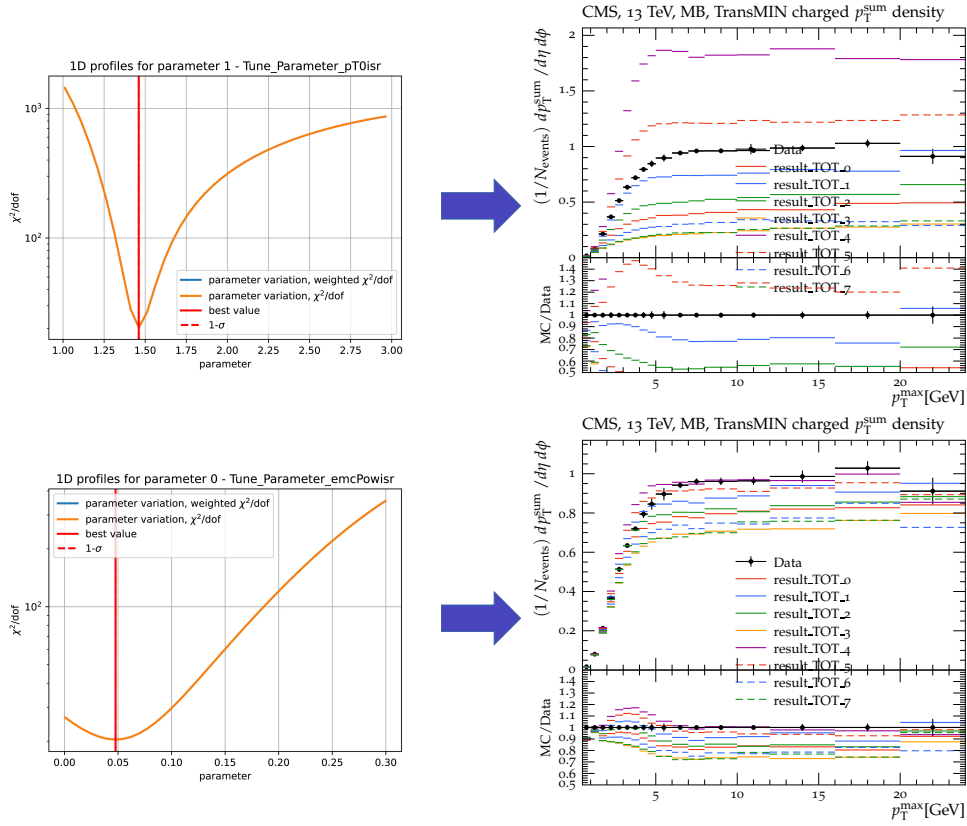


Figure 6.2: the sensibility of the tuned distributions respect to the variation of the parameters in related to the output of the minimizer. The top panels are related to **pT0Ref** while the bottom ones to **emcPow**. The different colored lines in the 2 distributions (on the right) are the simulations with different values for the parameter. The black point are the data.

6.2.2 Inverse Model results

The other operation mode offered by MCNNTUNES is the Inverse model. The results we get from the first test of the Inverse model are described here while the overall distribution are reported in next section together the ones from the PerBin Model. As mentioned before to make this model work properly one have to perform a hyperparameters optimization. our hyperparameter optimization was a scan of the architecture parameters shown in Table 6.3 the number of trials (combinations of these parameters) was 1000. in this case the best model we found is the one reported in Table 6.4.

Hyperparameter	Variation Range
Number of hidden layer	2-5
Units per layer	2-20
Activation function	tanh, relu, sigmoid
Optimizer	sgd, rmsprop, adagrad, adadelata, adam, adamax, nadam
Epochs	250-15000 in discrete steps
Batch size	64-5000 in discrete steps
Number of trials	1000

Table 6.3: Hyperparameter space scanned for the optimization of the NN architecture.

Hyperparameter	Value
Number of hidden layer	4
Units layers	[2, 14, 9, 18]
Activation function	tanh
Optimizer	nadam
Epochs	1000
Batch size	500

Table 6.4: Best hyperparameters model found for the test with 2 parameters variation.

Once the best model is trained the output we get from this model is the distribution of predictions obtained by the resampling phase of the experimental data then fed to the network. The prediction spread for the two parameters test is shown in Fig. 6.3 these are obtained from the re-sampling phase using the multivariate Gaussian distribution described in Eq. 5.11.

The estimated parameter are marked by the solid black line, while the dotted black lines are the error on the parameter. The value we get from the tune are also reported in Table 6.5 together with the CP5 values. In this case the error estimation is correctly implemented and a direct comparison between the value is possible. Looking at the values reported in the table it is clear that the two tune are compatible.

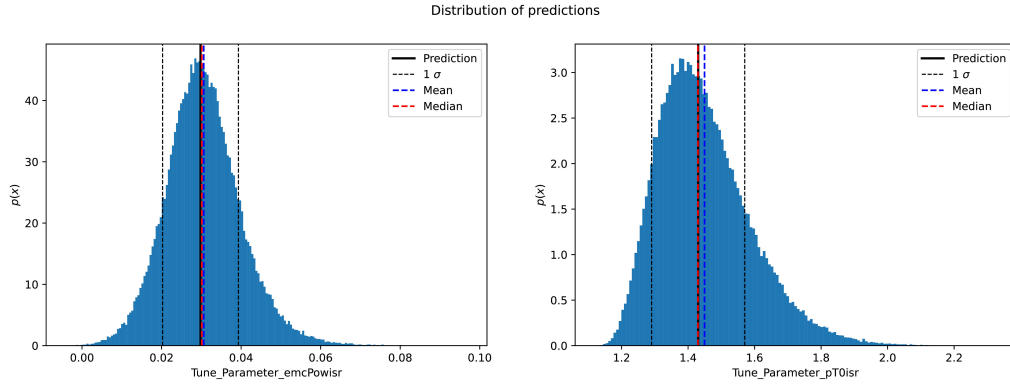


Figure 6.3: The spread of predictions we get as output from the Inverse Model. the right one refers to the `ecmPow` parameter and the left one to `pT0Ref`. The parameters predicted are marked by the solid black line while the error is evaluated using the standard deviation indicated by the dashed black lines.

Parameter	Value	CP5 (down & up)
MultipartonInteractions:pT0Ref	1.43 ± 0.14	$1.41 - 1.46$
MultipartonInteractions:ecmPow	0.0298 ± 0.0095	0.03

Table 6.5: Results for the Inverse model in two parameter variation test. The upper and lower limit for CP5 are also reported here for a direct comparison between the two tunes. The two predicted parameters are compatible to the one in CP5.

6.2.3 Overall results

In this section we are going to show some overall results for the first test with only two free parameters. We are not going to show all the graphs here we list them all in the appendix Appendix A.

From the graphs in Fig. 6.4 is clear that MCNNTUNES gives some good result for the test.

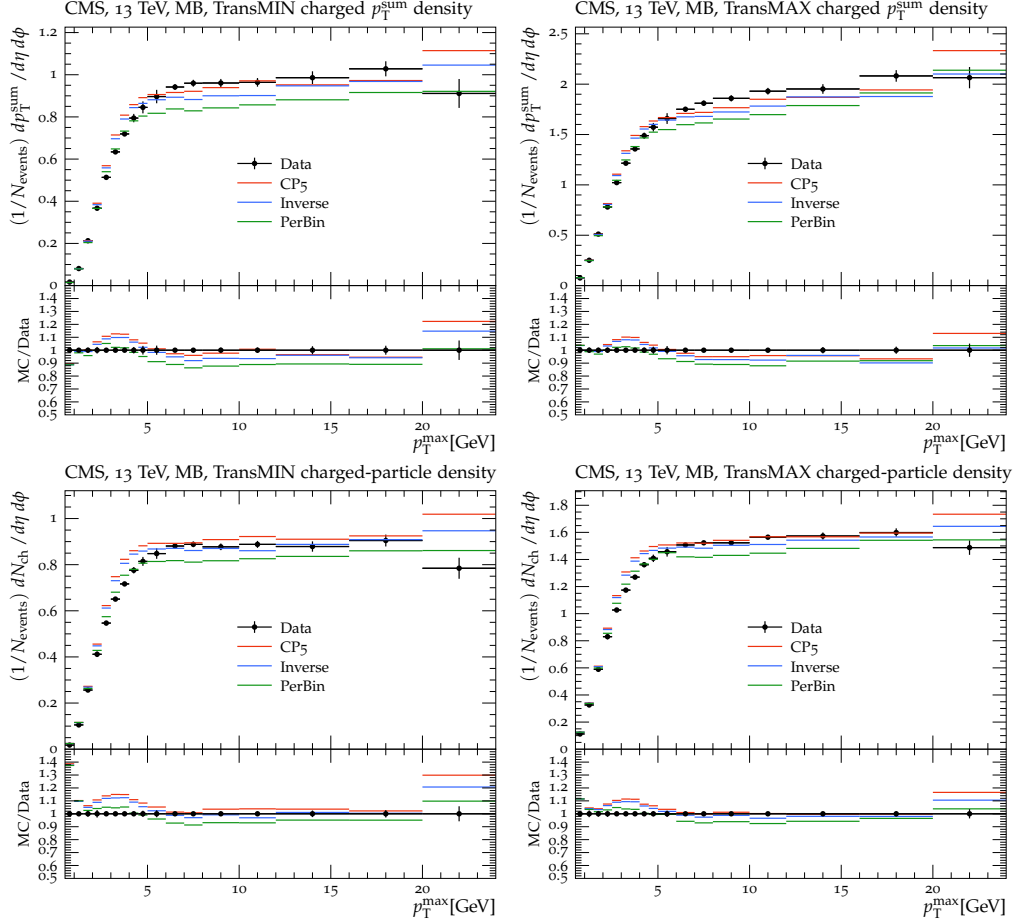


Figure 6.4: Results for the two parameters variation test. Here are reported the distributions from the $\sqrt{s} = 13$ TeV CMS analysis [34] that show the transMAX charged particle density (upper left) and the charged p_T -sum density (upper right); the transMIN charged particle density (lower left) and the charged p_T -sum density (lower right) as a function of the transverse momentum of the leading charged particle. The black points are the experimental data and the black vertical lines the experimental uncertainties. The data are compared to the MC prediction from the result we get using PerBin Model (green line), Inverse Model (blue line) and the existing tune CP5 (red line). The data are well described by all the tunes. Our tune describe very well the low- p_T region ($p_T \lesssim 5$ GeV).

The result we get from PerBin model (green line) and from Inverse model (blue line) are similar to the result obtained from CP5 tune (red line). our tune describe the low region ($p_T \lesssim 5$ GeV) very well this region is very important because is the region with lower error on the experimental data.

Overall, we can consider this test successfully passed from MCNNTUNES, it gives result similar to the standard tool PROFESSOR. This was only a simplified test to

check the correct operation for the tool. So, passed the test we decide to extend our analysis to a complete tune for the underlying event.

6.3 Our tune for the UE in Minimum Bias observations

Given the good results for the test we extend our analysis to the variation of five parameters. The interested parameter are the ones related to the Multi Parton Interaction and to the Color Reconnection. The ranges of variation for these parameters are the same used for CP5 and summarized in Table 6.6.

Parameter Name	Value
<code>MultipartonInteractions:pT0Ref [GeV]</code>	[1.0 – 3.0]
<code>MultipartonInteractions:ecmPow</code>	[0.0 – 0.3]
<code>MultipartonInteractions:coreRadius</code>	[0.1 – 0.95]
<code>MultipartonInteractions:coreFraction</code>	[0.1 – 0.8]
<code>ColorReconnection:range</code>	[1.0 – 9.0]

Table 6.6: The variation ranges for the five parameters that we want to tune. These are the same used in the CP5 tune in [39].

As the parameters space increase we need to increase also the number of samples and then the size of the training set in order to have a sufficient granularity in the sampling of the space. The training set we use for the PerBin model with five parameters variation is composed from approximately 2000 MC runs, instead for the Inverse model we try also larger training set.

6.3.1 Per Bin Model results

The PerBin model is the model that give to us the best results, the parameters estimation we get from the PerBin model loss function minimization is reported in Fig. 6.5. In the figure the five parameters χ^2/DoF functions are reported with a blue line. The predicted value is indicated by the solid red line while the $1 - \sigma$ range with the dotted lines. It is clear that also in this case the most sensible parameter is the `MultipartonInteractions:pT0Ref` (6.5e) the minimum in that case is very well defined and the error small. The parameters in Fig. 6.5c and Fig. 6.5d are also well defined the error is not to big. The not so good defined parameters are the `MultipartonInteractions:coreFraction`, that is in a minimum but with a larger error than the other parameters which is why the distribution under analysis are less sensitive to the variation of this parameter, and the `ColorReconnection:range`. The last one is not actually in a real minimum, in this case also the error evaluation, as a confidence interval is not possible. This indicated a saturation of this parameter, over a certain value all the possible reconnection have already occurred, and so a consequent small sensitivity to this parameter variation.

The value we get for the parameter are reported also in Table 6.7 and compared to the CP5 limits. It is easy to see that all the parameters are compatible with the

6.3. OUR TUNE FOR THE UE IN MINIMUM BIAS OBSERVATIONS

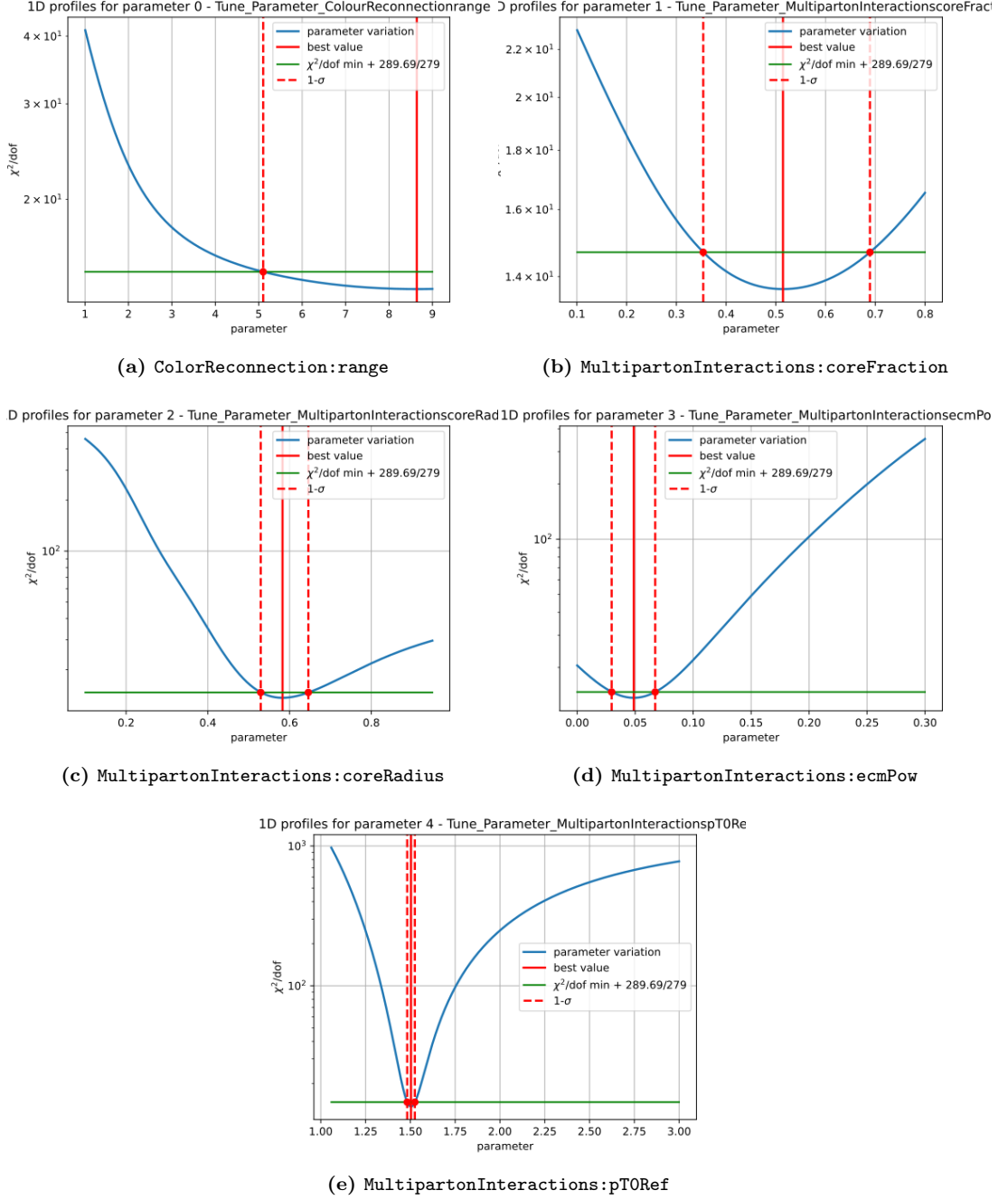


Figure 6.5: The minimizer output for every tuned parameter. The blue line is the χ^2/DoF as a function of the parameter value. The solid vertical line indicate the best estimation for the parameter value while the errors are indicated by the dashed red lines. In the graph (a) it is clear that a saturation in the parameter is reached after a certain value this lead to a small sensitivity to the parameter variation and so a non-well defined minimum. The upper limit in this case cannot be calculated. The other parameters are all in a real minimum and with a concrete error evaluation.

CP5 except for the `ColorReconnection:range`.

The distribution we get are reported in the Section 6.3.3 as we can see in the Fig. 6.13 the PerBin model does not describe very well this distribution for the pseudorapidity of the inelastic production of hadrons. A possible explanation is

Parameter	Value	CP5 (down & up)
MultipartonInteractions:pT0Ref	$1.50^{+0.02}_{-0.02}$	1.41 – 1.46
MultipartonInteractions:ecmPow	$0.049^{+0.018}_{-0.019}$	0.03
MultipartonInteractions:coreFraction	$0.51^{+0.17}_{-0.16}$	0.43 – 0.73
MultipartonInteractions:coreRadius	$0.58^{+0.06}_{-0.05}$	0.67 – 0.69
ColorReconnection:range	$8.6^{-3.5}_{+null}$	4.88 – 4.69

Table 6.7: The results of the tune using PerBin Model. All the values are compatible with the one with the CP5 using a Z test with a significance level of 0.05. But the value predicted for the Color Reconnection have a very large error and is not as similar to the one obtained from CP5. The *null* subscript indicates that the definition of the confidence region exceed the scanned space for the parameters defined for each parameter in Table 6.6.

that the experimental uncertainties on the bins of this distribution are higher than the ones in others and so this distribution be less important in the overall loss function.

So, we decide to perform a second tune using PerBin Model. In the second tune we give to all Fig. 6.13 bins an higher weight using the weightrules implemented in MCNNTUNES, we give a weight of 5 to all bins of this distribution. In this way we are giving a greater importance to this distribution and so we are going to describe those data better.

The output of the minimization step is reported in Fig. 6.6. The value we get from the weighted tune are also reported in Table 6.8. The values we get are compatible also in this case with CP5 except for the MultipartonInteractions:coreRadius that is higher than the one predict from CP5.

But if we look at the overall result in Section 6.3.3 the PerBin Model with different weights give a result more similar to CP5 in almost all the distributions.

Parameter	PerBin	PerBin + Re-weight	CP5 (down & up)
MPI:pT0Ref	$1.50^{+0.02}_{-0.02}$	$1.42^{+0.01}_{-0.01}$	1.41 – 1.46
MPI:ecmPow	$0.049^{+0.018}_{-0.019}$	$0.0342^{+0.014}_{-0.014}$	0.03
MPI:coreFraction	$0.51^{+0.17}_{-0.16}$	$0.34^{+0.14}_{-0.17}$	0.43 – 0.73
MPI:coreRadius	$0.58^{+0.06}_{-0.05}$	$0.9^{+null}_{-0.1}$	0.67 – 0.69
CR:range	$8.6^{-3.5}_{+null}$	$5.6^{+1.0}_{-0.9}$	4.88 – 4.69

Table 6.8: The results of the tune using PerBin model + re-weight are compared to the ones with PerBin model and CP5. except for the coreRadius parameter, all the predicted values are compatible with the one with the CP5 using a Z test with a significance level of 0.05. The PerBin + re-weight gives results more similar to the one obtained from CP5 this is also clear watching to the overall resulting distribution. The *null* subscript indicates that the definition of the confidence region exceed the scanned space for the parameters defined for each parameter in Table 6.6

6.3. OUR TUNE FOR THE UE IN MINIMUM BIAS OBSERVATIONS

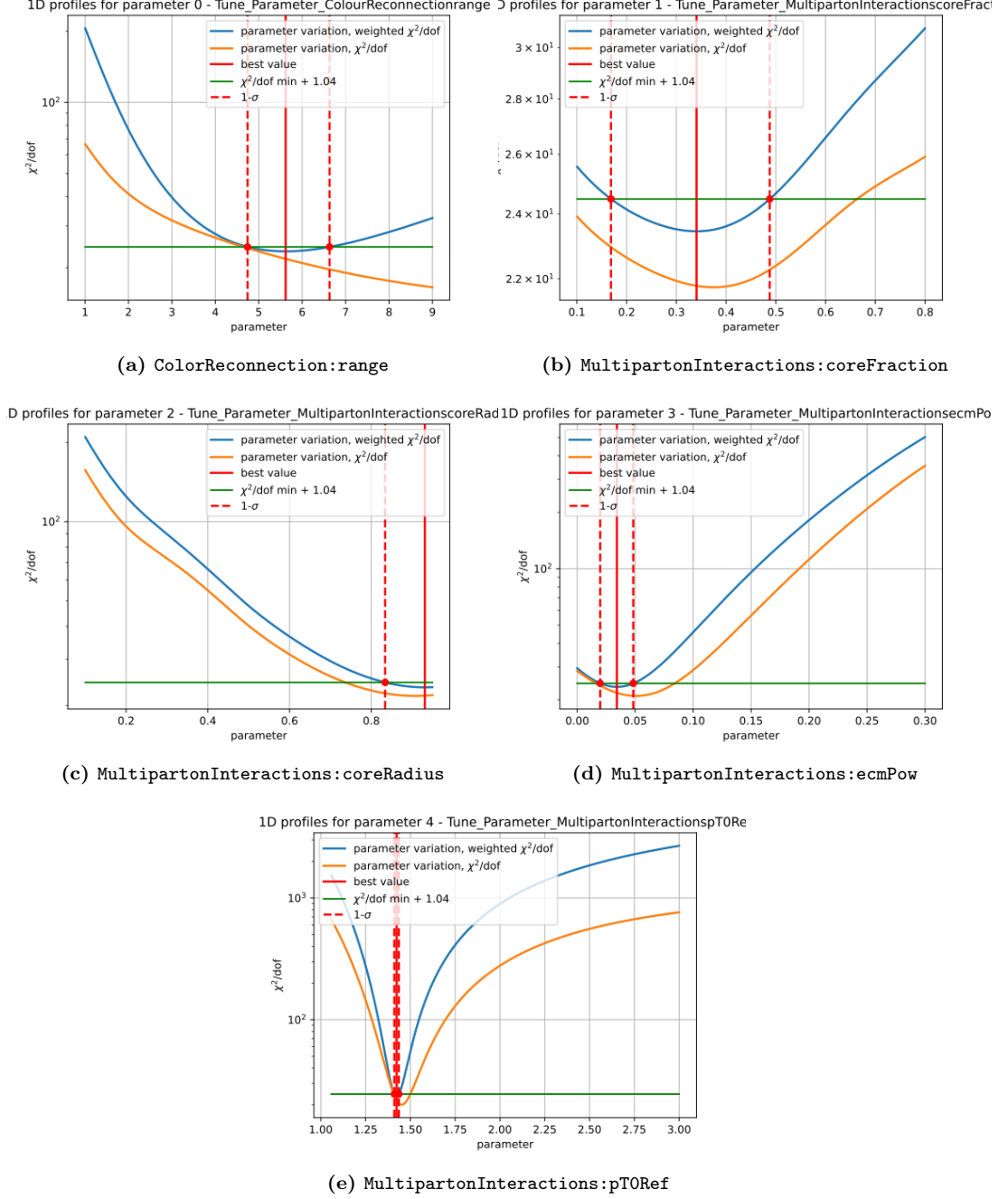


Figure 6.6: The minimizer output for every tuned parameter using PerBin model with the re-weight. The blue line is the χ^2/DoF as a function of the parameter value before the re-weight while the orange line indicate the same function but applying the re-weight. The solid vertical line indicate the best estimation for the parameter value while the errors are indicated by the dashed red lines. The parameter in figure (c) is predicted near the upper limit of the variation range.

6.3.2 Inverse Model results

On the other hand if the PerBin model gives to us very good result, we cannot tell the same for the Inverse Model. In this case the Inverse Model gives very bad results. Also after the hyperparameters optimization, using the scan space described in Table 6.3, the model fails.

The distributions of predictions are reported for each parameter in Fig. 6.7 and the actual parameters in Table 6.9 as we can see the predicted values are in most of the cases out of the variation ranges set for the sampling and (also to the maximum possible value in PYTHIA8). Some other parameter are determined with a very large distribution and so very large errors.

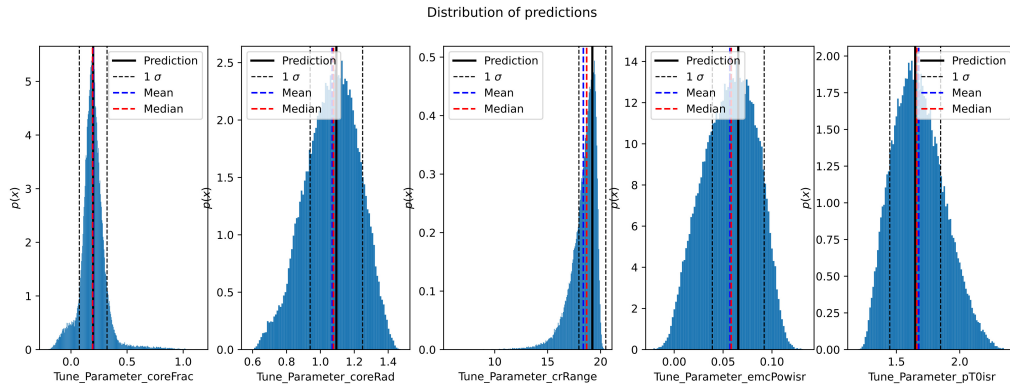


Figure 6.7: The spread of prediction obtained from the Inverse model. It is clear that also after the hyperparameters optimization the inverse model is not working properly. The distribution have long tails out of the limits for the variation, the central one referred to the Color Reconnection is predicted completely out of the boundaries.

Parameter	Value	CP5 (down & up)
MultipartonInteractions:pT0Ref	1.65 ± 0.20	$1.41 - 1.46$
MultipartonInteractions:ecmPow	0.066 ± 0.026	0.03
MultipartonInteractions:coreFraction	0.20 ± 0.12	$0.43 - 0.73$
MultipartonInteractions:coreRadius	1.1 ± 0.2	$0.67 - 0.69$
ColorReconnection:range	19.2 ± 1.3	$4.88 - 4.69$

Table 6.9: The predicted values using Inverse model are showed here, the model is not working in this case the predicted values for the core radius and for the color reconnection are out of the boundary while other parameter are predicted with a quite large error.

We can see from Fig. 6.8 the tune we get from the Inverse Model (blue line), as was expected, cannot describe the observables distributions. The tune misses all the experimental data points approximately by a 50% of the value. So we have to exclude this model for this tune. Maybe the failure is related to the higher number of parameters respect to the first test, that leads to a more complex generator response and so a more difficult model to learn and invert.

In MCNN TUNES presentation paper [48] is reported that the Inverse model can fail when in the training set is not given a sufficient number of MC simulations with parameters values near to the actual real ones. So, trying to make this model

work, we decide to introduce a Gaussian bias in the sampling phase instead of a uniform distributed sampling. Our Gaussian sampling was peaked on the parameters predicted by the PerBin Model, but also this procedure does not leads to some consistent results.

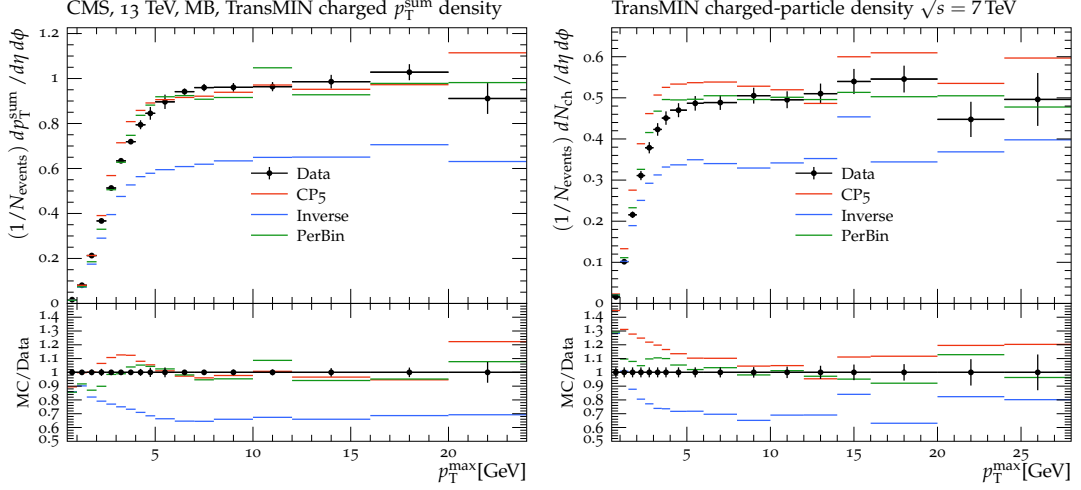


Figure 6.8: An example of the fact that the Inverse model (blue line) is not working: the bins are filled to only the 50% of the expected value in almost all the bins. On the left is shown the transMIN charged particle transverse momentum sum density for the CMS analysis at $\sqrt{s} = 13$ TeV [34] and on the right the transMIN charged particle density from the CMS analysis [44] in both case as a function of the leading object transverse momentum.

6.3.3 Overall results

Overall, what we have are two tunes performed with the PerBin Model that are quite good tunes. In this section all the fitted distributions are shown and the two tunes are compared to the distribution obtained with the CP5 default values. The PerBin Model describe very well the data in particular in all the low- p_T regions where the experimental uncertainties are smaller and so more important in the χ^2 evaluation.

The first distributions showed in Fig. 6.9 are referred to the charged particle multiplicity and the charged particle scalar p_T sum in the two transverse regions (TransMAX and TransMIN) as a function of the leading object transverse momentum. The black points are the experimental data taken from the CMS experiment at the center of mass energy of 13 TeV. They are compared to the CP5 tune, red line, and the two tunes we have gotten from the PerBin Model and PerBin Model plus the re-weights, respectively blue and green lines. It is easy to see that all the three tunes are describing the distribution very well, in particular our tunes in the low- p_T regions ($p_T < 5$ GeV) are describing the distribution also better than CP5 in most of the cases.

Instead, in Fig. 6.10 are reported the same distribution but at $\sqrt{s} = 7$ TeV also in this case our tunes are good in describing the distributions, they seem to be also better than CP5.

Also the data at the center-of-mass energy of 1.96 TeV are well described. These data had been collected by the CDF experiment in proton-antiproton collisions.

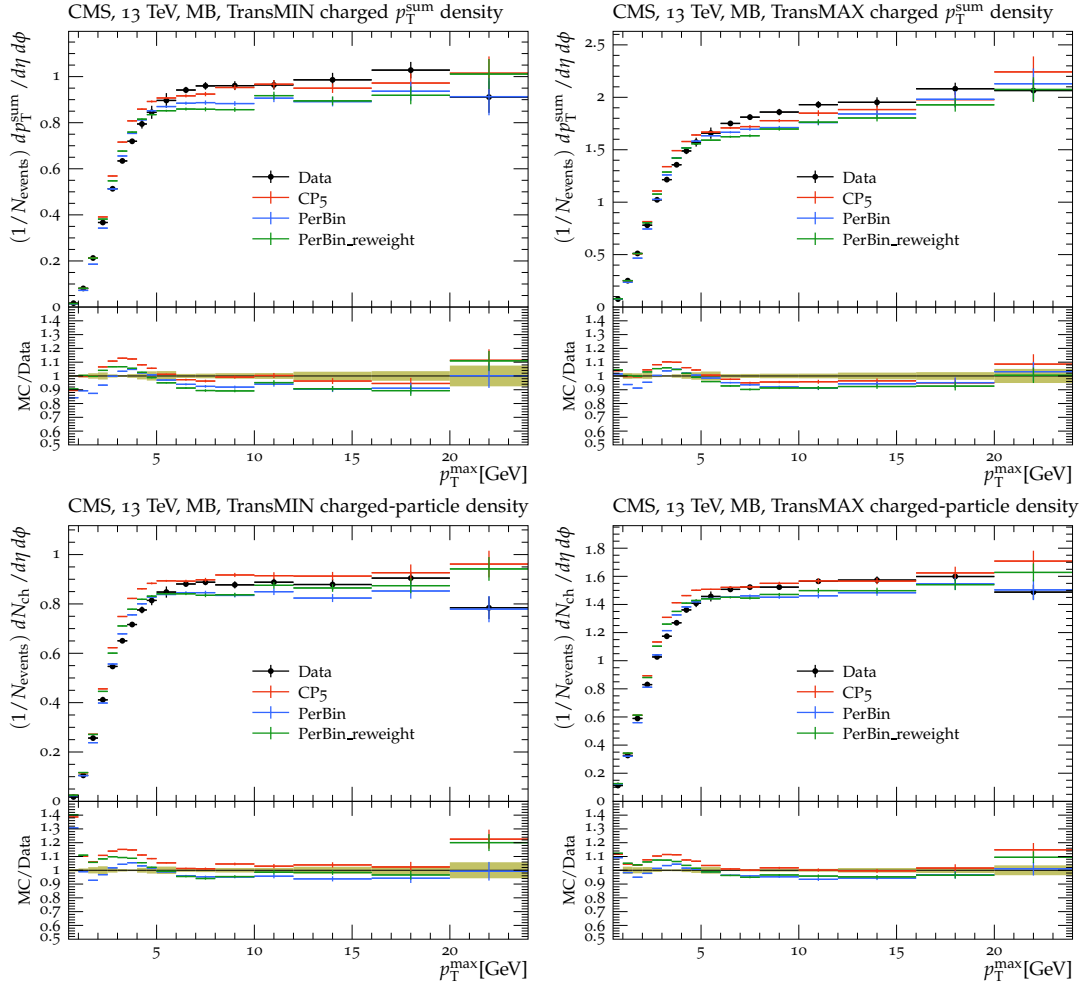


Figure 6.9: In this figure the data from the $\sqrt{s} = 13$ TeV CMS analysis [34] that show the transMAX charged particle density (upper left) and the charged p_T -sum density (upper right); the transMIN charged particle density (lower left) and the charged p_T -sum density (lower right) as a function of the transverse momentum of the leading charged particle. The CP5 tune is compared to our tune using the PerBin Model. Our tune (red line) seems good as the CP5 (blue line) in describing the data. The first bins are the most important they have a smaller experimental error than the higher p_T data. Also the PerBin model with re-weight (green line) seems really good in the description of the data. Also the ratio between MC and data points is reported and the green band represent the experimental uncertainties, while the vertical colored lines on the MC points are the statistical uncertainties.

Fig. 6.12 and Fig. 6.13 represent the pseudorapidity distribution for diffractive events and for inelastic charged hadrons production. The left distribution of Fig. 6.12 and the distribution in Fig. 6.13 are not well described by the PerBin Model (blue line) but are better described by the PerBin Model plus the re-weights for these bins. So also in this case we have a good result from MCNTUNES tool.

A numerical evaluation on the overall difference between MC and experimental points can be evaluated for all the three tunes using the χ^2/DoF definition:

$$\chi^2 = \sum_i \frac{(\text{MC}_i - \text{exp}_i)^2}{\sigma_i^2} . \quad (6.1)$$

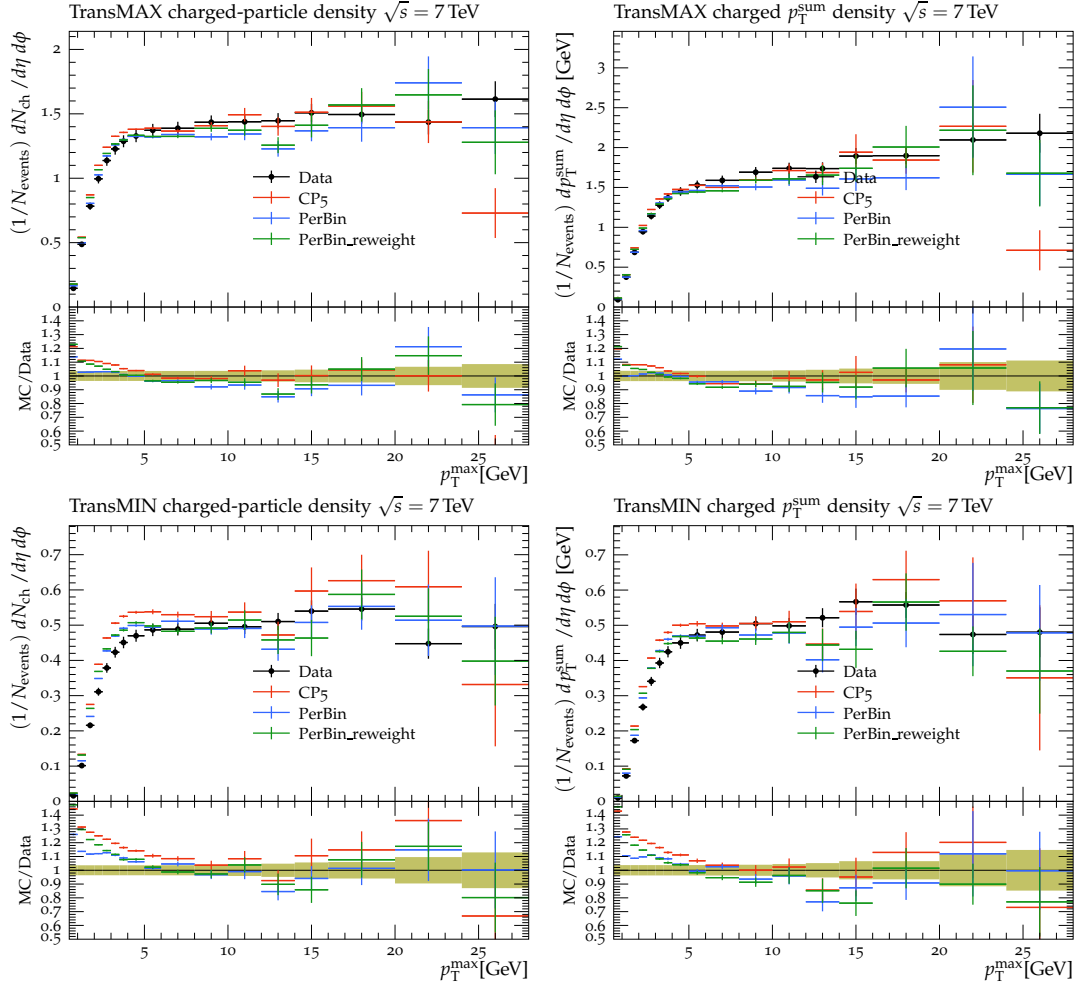


Figure 6.10: Here the data at $\sqrt{s} = 7$ TeV from the CMS analysis [44] for the transMAX charged particle density (upper left) and the charged p_T -sum (upper left); the transMIN charged particle density (lower left) and the charged $p-T$ -sum are displayed as a function of the leading object transverse momentum. The three tunes describe the data (black point) very well. The low $p-T$ regions are described better from our tune respect to the CP5 tune. As was expected the result from the PerBin model with the re-weights (green line) are more similar to the CP5 result. Also the ratio between MC and experimental points is reported and the green band represent the experimental uncertainties, while the vertical colored lines on the MC points are the statistical uncertainties.

The results we get are reported in Table 6.10. From this is clear that from this eval-

Tune	χ^2/DoF
CP5:	23.9
PerBin:	13.7
PerBin + re-weights:	19.4

Table 6.10: χ^2 evaluation for the three tunes.

uation the better tune overall is the PerBin model tune. In fact, the PerBin Model describes very well the distributions were the experimental uncertainties are smaller but don't describe very well the last distributions in the left panel of Fig. 6.12 and

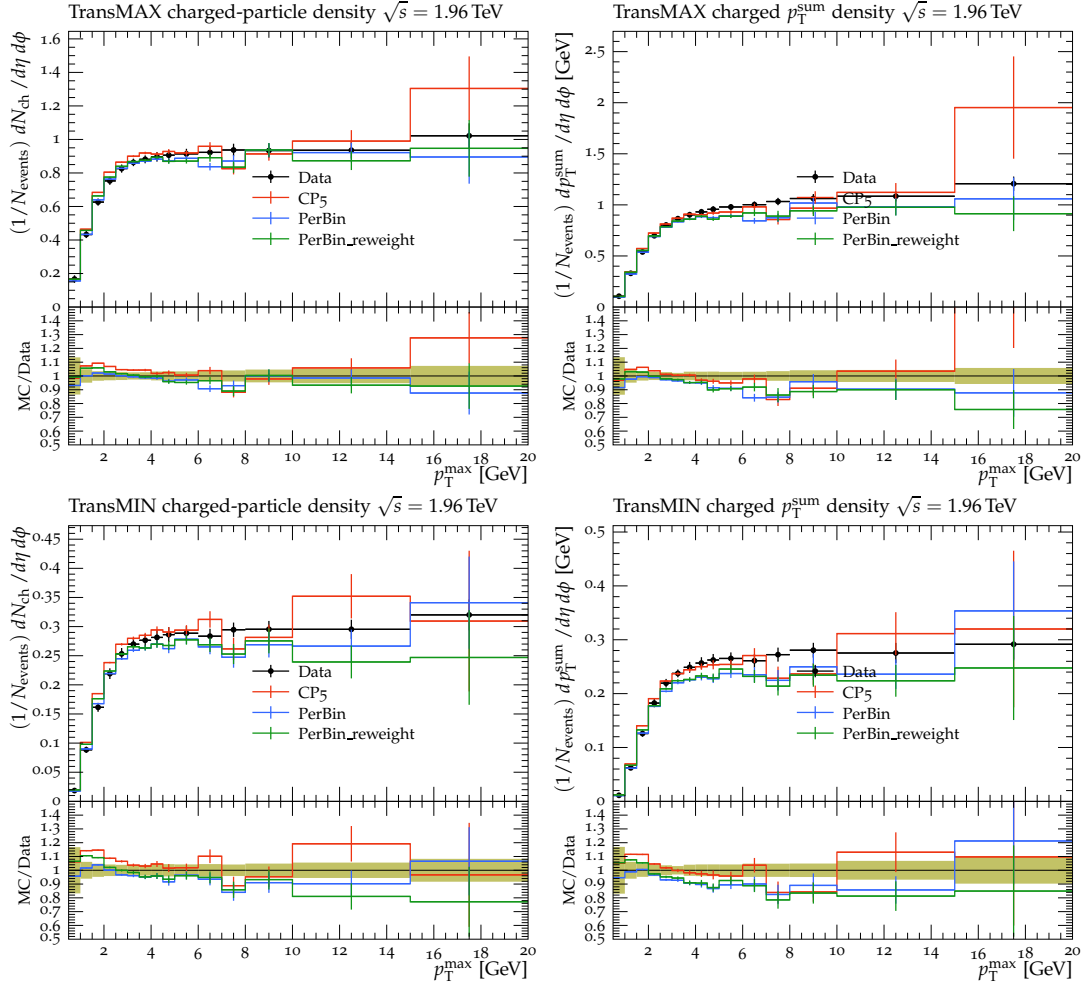


Figure 6.11: The transMAX charged particle density (upper left) and the charged p_T -sum (upper left); the transMIN charged particle density (lower left) and the charged p_T -sum from the CDF analysis at $\sqrt{s} = 1.96$ TeV in proton-antiproton collisions [43]. The data are described very well from the CP5, PerBin, PerBin + re-weights tunes. Also the ratio between MC and experimental points is reported and the green band represent the experimental uncertainties, while the vertical colored lines on the MC points are the statistical uncertainties.

Fig. 6.13. A very good result is also the one obtained from the PerBin Model with the different weights for the bins in the distribution in Fig. 6.13. This tune in the idea of having a more general tune that describe better all the distributions can be considered as a better tune. In general the χ^2 evaluated is less in both our tunes respect to the CP5 one.

Given these results we can conclude that MCNNTUNES is valid tool for the tune of the parameters in high energy physics generators. We obtained two valid tunes for the underlying event and minimum bias observations in proton-proton collisions. The activity observed in the two transverse regions and the pseudorapidity distributions for different events selections are well described after the tune of the parameters that control the multi parton interactions and the color reconnection in PYTHIA8. The output we got from the minimizer in Fig. 6.5 tell to us that the most important parameter for the description of this distributions is the threshold value p_{T0}^{ref} , all the distributions have a large sensitivity on the variation of this parameter and this is

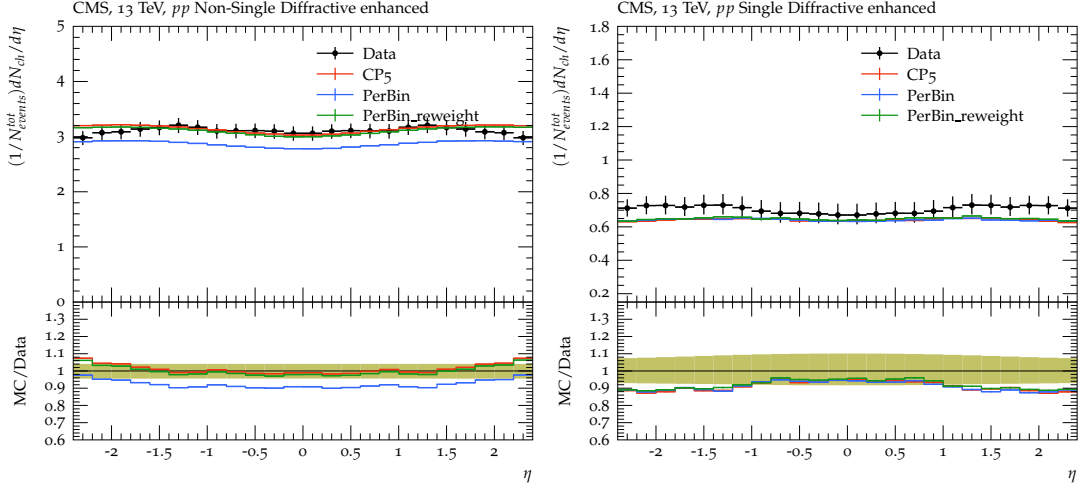


Figure 6.12: Here are reported the pseudorapidity distributions ($p_T > 0.5$ GeV, $|\eta| < 2.4$) for charged particle multiplicity in single diffractive (right) and non-single diffractive (left) events selection. The black points are the data from the CMS analysis at $\sqrt{s} = 13$ TeV [45]. The data from the NSD events are not so well described from the PerBin model (blue line) but with the re-weights we can describe these data points better. Instead, for the SD events we get a result equal to the one of CP5. Also the ratio between MC and data points is reported and the green band represents the experimental uncertainties, while the vertical colored lines on the MC points are the statistical uncertainties, in these distributions the statistical uncertainties are very small due to the high number of events in each bin.

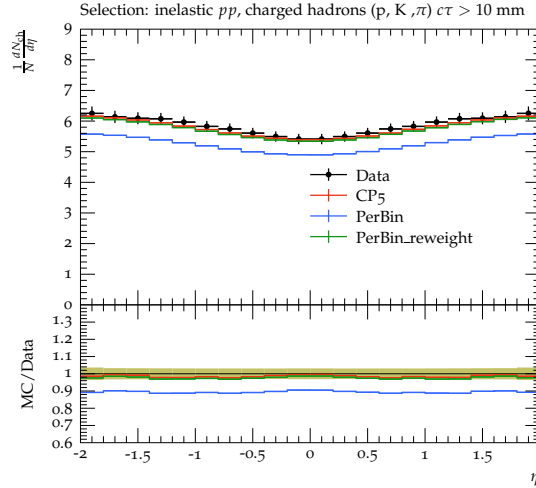


Figure 6.13: In this figure is shown the last distribution we use for the tune from the CMS analysis at $\sqrt{s} = 13$ TeV [42]. The pseudorapidity distribution ($|\eta| < 2$) for the charged hadron density in an inelastic proton-proton scattering selection. Also here the PerBin model (blue line) gives a different result from the CP5 and the PerBin + re-weights tunes. Also the ratio between MC and data points is reported and the green band represents the experimental uncertainties, while the vertical colored lines on the MC points are the statistical uncertainties, in this distribution the statistical uncertainties are very small due to the high number of events in each bin.

related to the well defined minimum we got.

On the other hand the small dependence on the variation of the `ColorReconnection:range` parameter over a certain threshold indicates a saturation, in fact over some

value almost all the possible color reconnection have taken place and so the model is less sensitive to this parameter.

The Inverse model instead in this case don't give us a good result but maybe further tests can take to some good results. Maybe increasing even more the training set size but with careful, MCNNTUNES does not present any control on the NNs typical over-fitting problem. Even if the Inverse Model don't give us a complete tune for the underlying events it perform very well in the first test. So, we cannot exclude it as a valid tool.

Now, that the tool is validated we are going to extend the tune procedure to some new distribution and parameter. In the next chapter we focus on the tune of the *Primordial k_T* and Space Shower in order to improve the description of the data collected in Z boson production events.

Appendix A

Test with two free parameters for the Underlying Events

Here are reported all the distributions obtained by the test on two parameters:

- `MultipartonInteractions:pT0Ref`
- `MultipartonInteractions:ecmPow`

We compare the results we get from PerBin Model and from Inverse Model with the CP5 ones.

The value we get are also reported in the Table [A.1](#). The PerBin Model errors are not reported because there was not a proper errors estimation correctly implemented yet for this model.

Parameter	PerBin	Inverse	CP5 (down & up)
<code>MPI:pT0Ref</code>	1.46064	1.43 ± 0.14	1.41 – 1.46
<code>MPI:ecmPow</code>	0.04771	0.0298 ± 0.0095	0.03

Table A.1: Result PerBin model and Inverse Model in two parameter variation test. The value are compared to the upper and lower limit for CP5.

APPENDIX A. TEST WITH TWO FREE PARAMETERS FOR THE UNDERLYING EVENTS

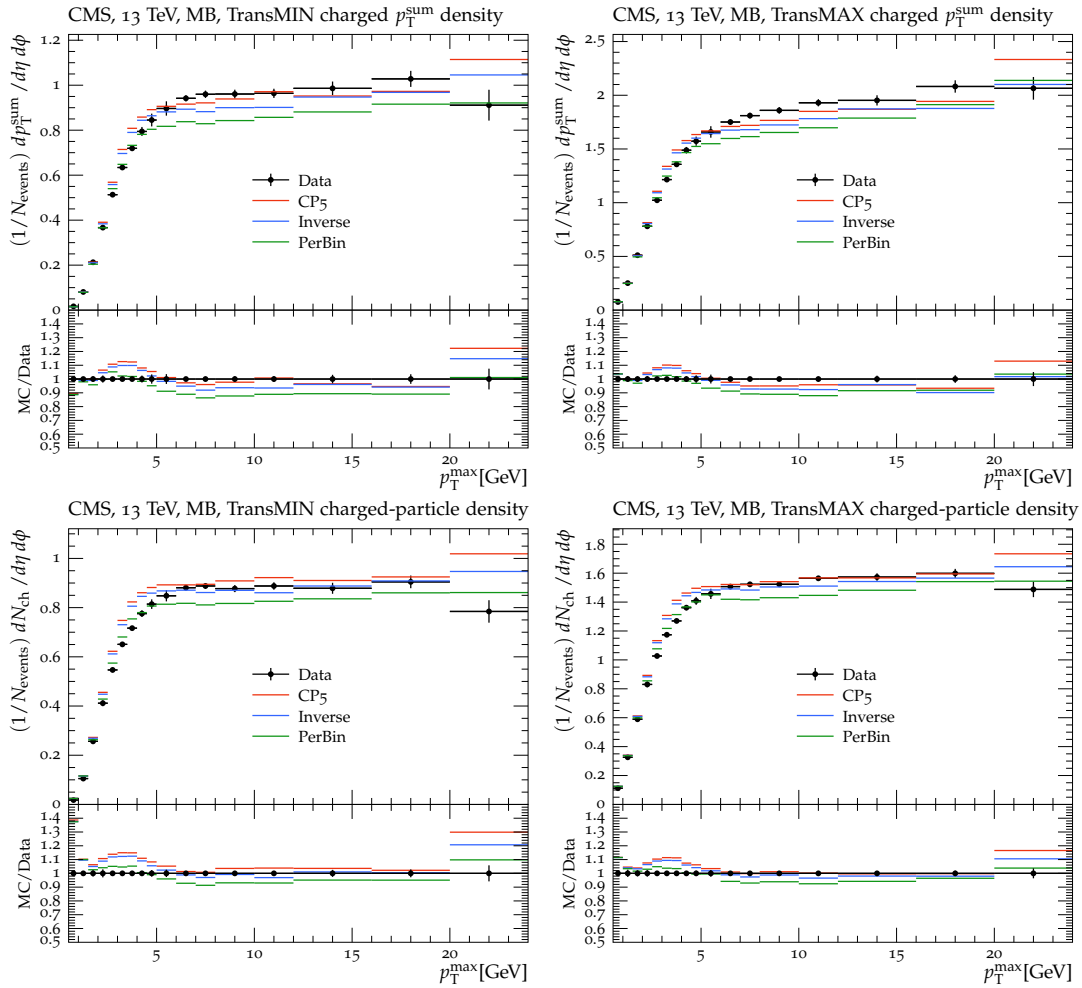


Figure A.1: In this figure the data from the $\sqrt{s} = 13$ TeV CMS analysis [34] that show the transMAX charged particle density (upper left) and the charged p_T -sum density (upper right); the transMIN charged particle density (lower left) and the charged p_T -sum density (lower right) as a function of the transverse momentum of the leading charged particle. The CP5 tune is compared to our test tune using the PerBin Model and Inverse Model.

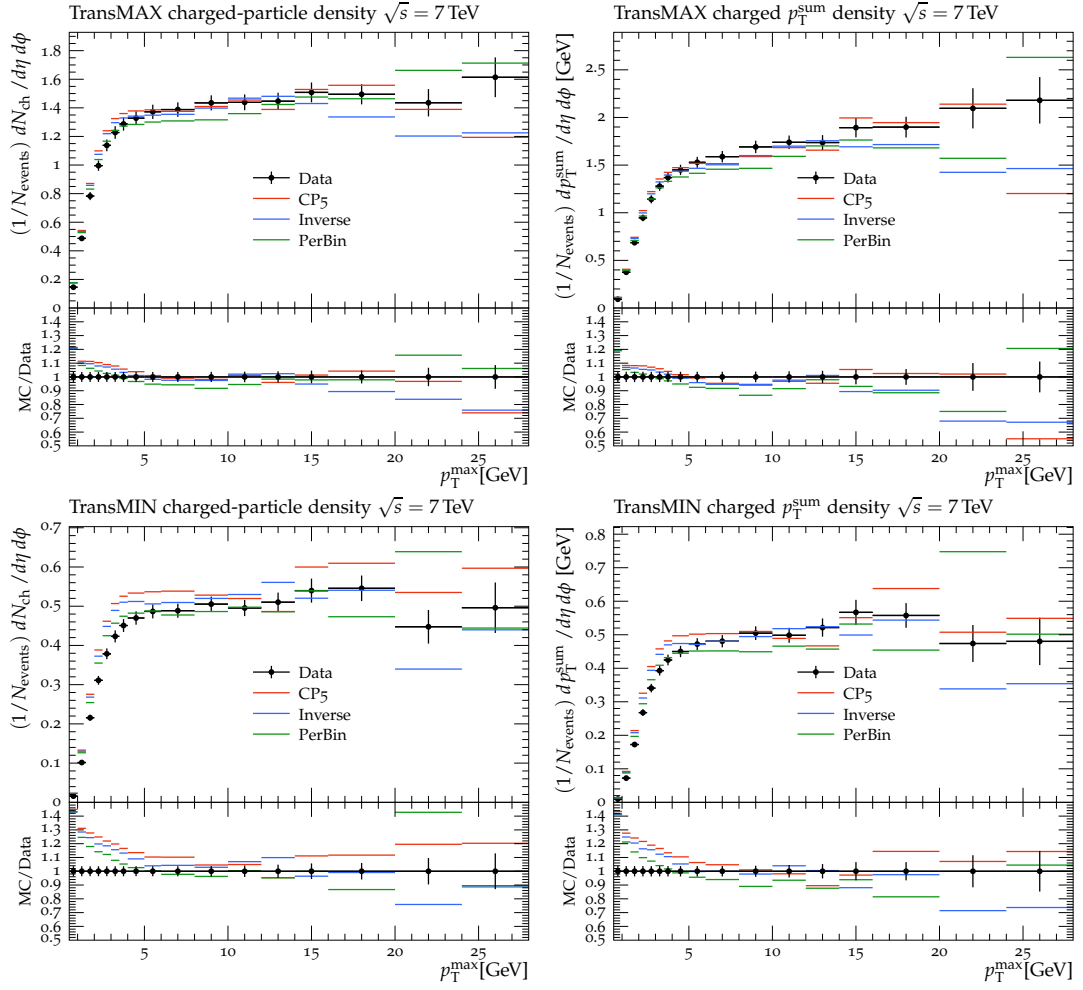


Figure A.2: Here the data at $\sqrt{s} = 7$ TeV from the CMS analysis [44] for the transMAX charged particle density (upper left) and the charged p_T -sum (upper left); the transMIN charged particle density (lower left) and the charged $p-T$ -sum are displayed as a function of the transverse momentum of the leading object.

APPENDIX A. TEST WITH TWO FREE PARAMETERS FOR THE UNDERLYING EVENTS

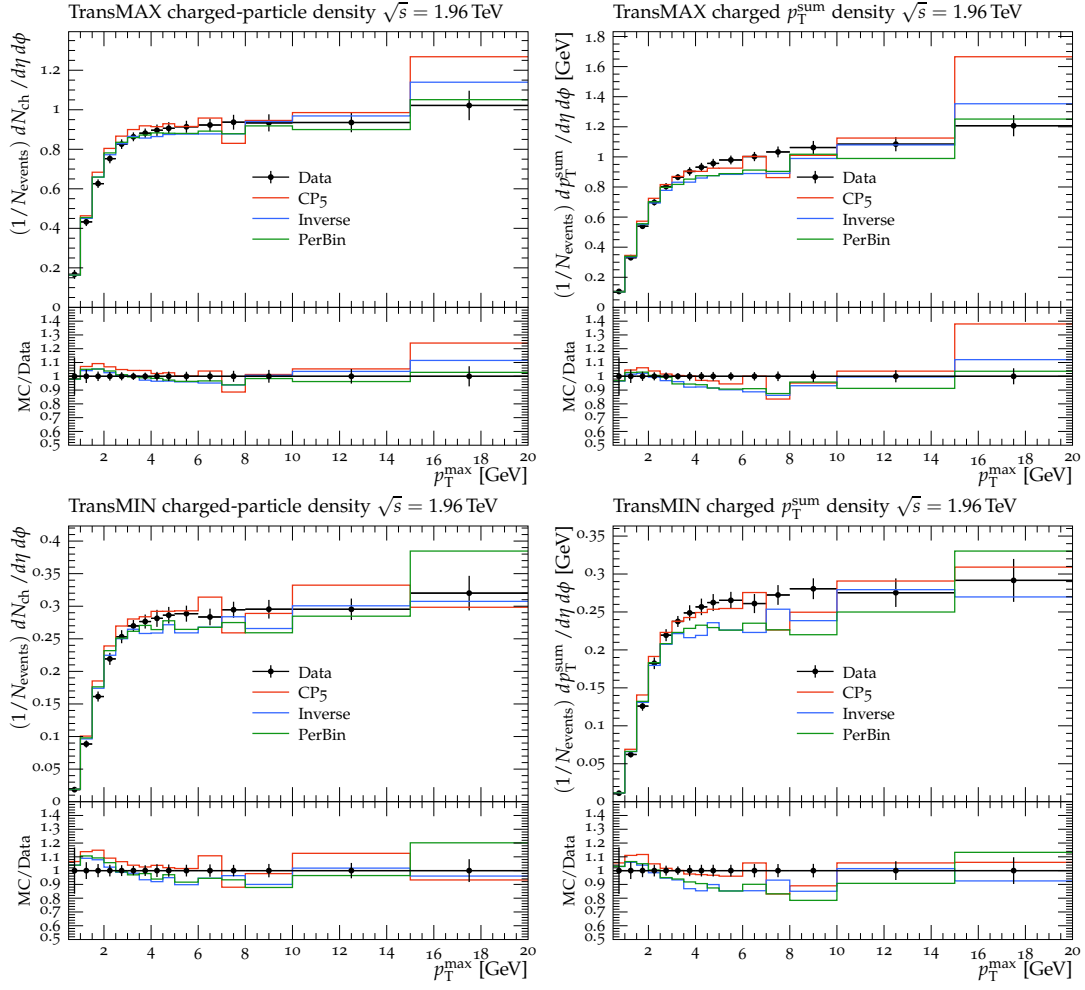


Figure A.3: The transMAX charged particle density (upper left) and the charged p_T -sum (upper left); the transMIN charged particle density (lower left) and the charged $p - T$ -sum from the CDF analysis at $\sqrt{s} = 1.96$ TeV in proton-antiproton collisions [43].

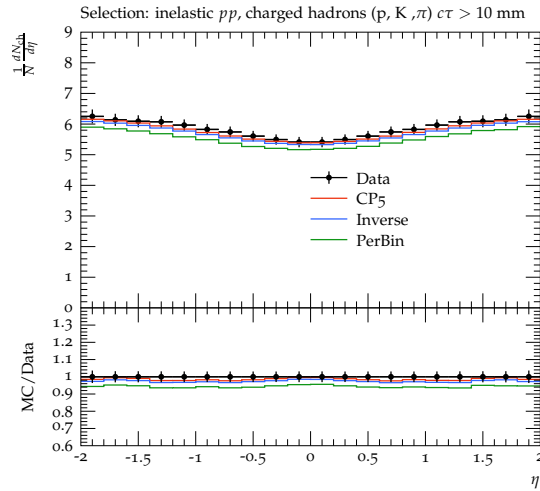


Figure A.4: In this figure is shown the last distribution we use for the tune from the CMS analysis at $\sqrt{s} = 13$ TeV [42]. The pseudorapidity distribution ($|\eta| < 2$) for the charged hadron density in an inelastic proton-proton scattering selection.

Bibliography

- [1] Steven Weinberg. A model of leptons, Nov 1967. URL <https://link.aps.org/doi/10.1103/PhysRevLett.19.1264>.
- [2] Giovanna Francesca Cottin Buracchio. Phenomenology of new physics beyond the Standard Model: signals of Supersymmetry with displaced vertices and an extended Higgs sector at colliders, Aug 2017. URL <https://cds.cern.ch/record/2276806>. Presented 09 Jun 2017.
- [3] H. Abramowicz et al. Combination of measurements of inclusive deep inelastic $e^\pm p$ scattering cross sections and QCD analysis of HERA data. *Eur. Phys. J. C*, 75(12):580, 2015. doi: 10.1140/epjc/s10052-015-3710-4.
- [4] R. P. Feynman. The behavior of hadron collisions at extreme energies. *Conf. Proc. C*, 690905:237–258, 1969.
- [5] P.A. Zyla et al. Review of Particle Physics. *PTEP*, 2020(8):083C01, 2020. doi: 10.1093/ptep/ptaa104. and 2021 update.
- [6] J. D. Bjorken. Asymptotic Sum Rules at Infinite Momentum. *Phys. Rev.*, 179: 1547–1553, 1969. doi: 10.1103/PhysRev.179.1547.
- [7] Sidney D Drell and Tung-Mow Yan. Partons and their applications at high energies, 1971. ISSN 0003-4916. URL <https://www.sciencedirect.com/science/article/pii/0003491671900716>.
- [8] J M Campbell, J W Huston, and W J Stirling. Hard interactions of quarks and gluons: a primer for lhc physics, Dec 2006. ISSN 1361-6633. URL <http://dx.doi.org/10.1088/0034-4885/70/1/R02>.
- [9] L N Lipatov. The parton model and perturbation theory, 1975. URL <http://cds.cern.ch/record/400357>.
- [10] Vladimir Naumovich Gribov and L N Lipatov. Deep inelastic ep scattering in perturbation theory, 1972. URL <https://cds.cern.ch/record/427157>.
- [11] G. Altarelli and G. Parisi. Asymptotic freedom in parton language, 1977. ISSN 0550-3213. URL <https://www.sciencedirect.com/science/article/pii/0550321377903844>.
- [12] Yuri L. Dokshitzer. Calculation of the Structure Functions for Deep Inelastic Scattering and $e^+ e^-$ Annihilation by Perturbation Theory in Quantum Chromodynamics., 1977.

- [13] W.J. Stirling. private communication. URL <http://www.hep.ph.ic.ac.uk/~wstirling/plots/plots.html>.
- [14] F. Bloch and A. Nordsieck. Note on the radiation field of the electron, Jul 1937. URL <https://link.aps.org/doi/10.1103/PhysRev.52.54>.
- [15] Toichiro Kinoshita. Mass singularities of feynman amplitudes, 1962. URL <https://doi.org/10.1063/1.1724268>.
- [16] T. D. Lee and M. Nauenberg. Degenerate systems and mass singularities, Mar 1964. URL <https://link.aps.org/doi/10.1103/PhysRev.133.B1549>.
- [17] A. Kulesza, G. Sterman, and W. Vogelsang. Electroweak vector boson production in joint resummation, 2002. URL <https://arxiv.org/abs/hep-ph/0207148>.
- [18] Torbjörn Sjöstrand, Stefan Ask, Jesper R. Christiansen, Richard Corke, Nishita Desai, Philip Ilten, Stephen Mrenna, Stefan Prestel, Christine O. Rasmussen, and Peter Z. Skands. An introduction to pythia 8.2, Jun 2015. ISSN 0010-4655. URL <http://dx.doi.org/10.1016/j.cpc.2015.01.024>.
- [19] Manuel Bähr, Stefan Gieseke, Martyn A. Gigg, David Grellscheid, Keith Hamilton, Oluseyi Latunde-Dada, Simon Plätzer, Peter Richardson, Michael H. Seymour, Alexander Sherstnev, and Bryan R. Webber. Herwig++ physics and manual, Nov 2008. ISSN 1434-6052. URL <http://dx.doi.org/10.1140/epjc/s10052-008-0798-9>.
- [20] T Gleisberg, S Hoeche, F Krauss, A Schaelicke, S Schumann, and J Winter. Sherpa 1. , a proof-of-concept version, Feb 2004. ISSN 1029-8479. URL <http://dx.doi.org/10.1088/1126-6708/2004/02/056>.
- [21] E. Boos, M. Dobbs, W. Giele, I. Hinchliffe, J. Huston, V. Ilyin, J. Kanzaki, K. Kato, Y. Kurihara, L. Lonnblad, M. Mangano, S. Mrenna, F. Paige, E. Richter-Was, M. Seymour, T. Sjostrand, B. Webber, and D. Zeppenfeld. Generic user process interface for event generators, 2001.
- [22] Stefano Catani, Frank Krauss, Bryan R Webber, and Ralf Kuhn. Qcd matrix elements + parton showers. *Journal of High Energy Physics*, 2001(11):063–063, Nov 2001. ISSN 1029-8479. doi: 10.1088/1126-6708/2001/11/063. URL <http://dx.doi.org/10.1088/1126-6708/2001/11/063>.
- [23] Stefano Frixione and Bryan R Webber. Matching nlo qcd computations and parton shower simulations. *Journal of High Energy Physics*, 2002(06):029–029, Jun 2002. ISSN 1029-8479. doi: 10.1088/1126-6708/2002/06/029. URL <http://dx.doi.org/10.1088/1126-6708/2002/06/029>.
- [24] Stefano Frixione, Paolo Nason, and Bryan R Webber. Matching nlo qcd and parton showers in heavy flavour production. *Journal of High Energy Physics*, 2003(08):007–007, Aug 2003. ISSN 1029-8479. doi: 10.1088/1126-6708/2003/08/007. URL <http://dx.doi.org/10.1088/1126-6708/2003/08/007>.

-
- [25] Stefano Frixione and Bryan R. Webber. The mc@nlo 3.1 event generator, 2005.
- [26] Rikkert Frederix and Stefano Frixione. Merging meets matching in MC@NLO. *JHEP*, 12:061, 2012. doi: 10.1007/JHEP12(2012)061.
- [27] Victor S. Fadin. BFKL resummation. *Nucl. Phys. A*, 666:155–164, 2000. doi: 10.1016/S0375-9474(00)00022-1.
- [28] I. I. Balitsky and L. N. Lipatov. The Pomeranchuk Singularity in Quantum Chromodynamics. *Sov. J. Nucl. Phys.*, 28:822–829, 1978.
- [29] Richard D. Ball, Valerio Bertone, Stefano Carrazza, Luigi Del Debbio, Stefano Forte, Patrick Groth-Merrild, Alberto Guffanti, Nathan P. Hartland, Zahari Kassabov, José I. Latorre, Emanuele R. Nocera, Juan Rojo, Luca Rottoli, Emma Slade, and Maria Ubiali. Parton distributions from high-precision collider data. *The European Physical Journal C*, 77(10), Oct 2017. ISSN 1434-6052. doi: 10.1140/epjc/s10052-017-5199-5. URL <http://dx.doi.org/10.1140/epjc/s10052-017-5199-5>.
- [30] FRANK SIEGERT. Monte-carlo event generation for the lhc, 2010. URL <http://theses.dur.ac.uk/484/>.
- [31] B. Andersson, G. Gustafson, G. Ingelman, and T. Sjöstrand. Parton fragmentation and string dynamics. *Physics Reports*, 97(2):31–145, 1983. ISSN 0370-1573. doi: [https://doi.org/10.1016/0370-1573\(83\)90080-7](https://doi.org/10.1016/0370-1573(83)90080-7). URL <https://www.sciencedirect.com/science/article/pii/0370157383900807>.
- [32] Torbjorn Sjostrand. Jet Fragmentation of Nearby Partons. *Nucl. Phys. B*, 248: 469–502, 1984. doi: 10.1016/0550-3213(84)90607-2.
- [33] Tai Sakuma and Thomas McCauley. Detector and Event Visualization with SketchUp at the CMS Experiment. *J. Phys. Conf. Ser.*, 513:022032, 2014. doi: 10.1088/1742-6596/513/2/022032.
- [34] Underlying Event Measurements with Leading Particles and Jets in pp collisions at $\sqrt{s} = 13$ TeV. Technical report, CERN, Geneva, 2015. URL <https://cds.cern.ch/record/2104473>.
- [35] Serguei Chatrchyan et al. Measurement of the underlying event in the Drell-Yan process in proton-proton collisions at $\sqrt{s} = 7$ TeV. *Eur. Phys. J. C*, 72: 2080, 2012. doi: 10.1140/epjc/s10052-012-2080-4.
- [36] A. M. Sirunyan et al. Measurement of the underlying event activity in inclusive Z boson production in proton-proton collisions at $\sqrt{s} = 13$ TeV. *JHEP*, 07:032, 2018. doi: 10.1007/JHEP07(2018)032.
- [37] Albert M. Sirunyan et al. Study of the underlying event in top quark pair production in pp collisions at 13 TeV. *Eur. Phys. J. C*, 79(2):123, 2019. doi: 10.1140/epjc/s10052-019-6620-z.
- [38] Florian Bechtel. *The underlying event in proton-proton collisions*. PhD thesis, Hamburg U., 2009.

- [39] Albert M Sirunyan et al. Extraction and validation of a new set of CMS PYTHIA8 tunes from underlying-event measurements. *Eur. Phys. J. C*, 80(1):4, 2020. doi: 10.1140/epjc/s10052-019-7499-4.
- [40] A. Banfi, S. Redford, M. Vesterinen, P. Waller, and T. R. Wyatt. Optimisation of variables for studying dilepton transverse momentum distributions at hadron colliders. *Eur. Phys. J. C*, 71:1600, 2011. doi: 10.1140/epjc/s10052-011-1600-y.
- [41] Albert M Sirunyan et al. Measurements of differential Z boson production cross sections in proton-proton collisions at $\sqrt{s} = 13$ TeV. *JHEP*, 12:061, 2019. doi: 10.1007/JHEP12(2019)061.
- [42] Vardan Khachatryan et al. Pseudorapidity distribution of charged hadrons in proton-proton collisions at $\sqrt{s} = 13$ TeV. *Phys. Lett. B*, 751:143–163, 2015. doi: 10.1016/j.physletb.2015.10.004.
- [43] Timo Antero Aaltonen et al. Study of the energy dependence of the underlying event in proton-antiproton collisions. *Phys. Rev. D*, 92(9):092009, 2015. doi: 10.1103/PhysRevD.92.092009.
- [44] Measurement of the Underlying Event Activity at the LHC at 7 TeV and Comparison with 0.9 TeV. Technical report, CERN, Geneva, 2012. URL <http://cds.cern.ch/record/1478982>.
- [45] Albert M. Sirunyan et al. Measurement of charged particle spectra in minimum-bias events from proton–proton collisions at $\sqrt{s} = 13$ TeV. *Eur. Phys. J. C*, 78(9):697, 2018. doi: 10.1140/epjc/s10052-018-6144-y.
- [46] Andy Buckley, Hendrik Hoeth, Heiko Lacker, Holger Schulz, and Jan Eike von Seggern. Systematic event generator tuning for the LHC. *Eur. Phys. J. C*, 65: 331–357, 2010. doi: 10.1140/epjc/s10052-009-1196-7.
- [47] Stefano Carrazza and Marco Lazzarin. N3pdf/mcnntunes: mcnntunes 0.1.0, October 2020. URL <https://doi.org/10.5281/zenodo.4071125>.
- [48] Marco Lazzarin, Simone Alioli, and Stefano Carrazza. MCNNTUNES: Tuning Shower Monte Carlo generators with machine learning. *Comput. Phys. Commun.*, 263:107908, 2021. doi: 10.1016/j.cpc.2021.107908.
- [49] Martín Abadi, Ashish Agarwal, Paul Barham, Eugene Brevdo, Zhifeng Chen, Craig Citro, Greg S. Corrado, Andy Davis, Jeffrey Dean, Matthieu Devin, Sanjay Ghemawat, Ian Goodfellow, Andrew Harp, Geoffrey Irving, Michael Isard, Yangqing Jia, Rafal Jozefowicz, Lukasz Kaiser, Manjunath Kudlur, Josh Levenberg, Dandelion Mané, Rajat Monga, Sherry Moore, Derek Murray, Chris Olah, Mike Schuster, Jonathon Shlens, Benoit Steiner, Ilya Sutskever, Kunal Talwar, Paul Tucker, Vincent Vanhoucke, Vijay Vasudevan, Fernanda Viégas, Oriol Vinyals, Pete Warden, Martin Wattenberg, Martin Wicke, Yuan Yu, and Xiaoqiang Zheng. TensorFlow: Large-scale machine learning on heterogeneous systems, 2015. URL <https://www.tensorflow.org/>. Software available from tensorflow.org.

- [50] F. Rosenblatt. The perceptron: A probabilistic model for information storage and organization in the brain. 1958. URL <https://doi.org/10.1037/h0042519>.
- [51] Kurt Hornik. Approximation capabilities of multilayer feedforward networks. *Neural Networks*, 4(2):251–257, 1991. ISSN 0893-6080. doi: [https://doi.org/10.1016/0893-6080\(91\)90009-T](https://doi.org/10.1016/0893-6080(91)90009-T). URL <https://www.sciencedirect.com/science/article/pii/089360809190009T>.
- [52] Moshe Leshno, Vladimir Ya. Lin, Allan Pinkus, and Shimon Schocken. Multilayer feedforward networks with a nonpolynomial activation function can approximate any function. *Neural Networks*, 6(6):861–867, 1993. ISSN 0893-6080. doi: [https://doi.org/10.1016/S0893-6080\(05\)80131-5](https://doi.org/10.1016/S0893-6080(05)80131-5). URL <https://www.sciencedirect.com/science/article/pii/S0893608005801315>.
- [53] Nikolaus Hansen. The CMA evolution strategy: A tutorial. *CoRR*, abs/1604.00772, 2016. URL <http://arxiv.org/abs/1604.00772>.
- [54] G. Cowan. *Statistical data analysis*. Oxford University Press, USA, 1998.
- [55] Richard D. Ball et al. Parton distributions from high-precision collider data. *Eur. Phys. J. C*, 77(10):663, 2017. doi: 10.1140/epjc/s10052-017-5199-5.
- [56] Peter Skands, Stefano Carrazza, and Juan Rojo. Tuning PYTHIA 8.1: the Monash 2013 Tune. *Eur. Phys. J. C*, 74(8):3024, 2014. doi: 10.1140/epjc/s10052-014-3024-y.
- [57] Albert M Sirunyan et al. Measurement of differential cross sections for Z boson production in association with jets in proton-proton collisions at $\sqrt{s} = 13$ TeV. *Eur. Phys. J. C*, 78(11):965, 2018. doi: 10.1140/epjc/s10052-018-6373-0.