ECE597ML-697ML Homework 3

Last Updated: February 28, 2023

Instructions

Due Tuesday 3/7 at 4pm. Complete all exercises and problems below.

How to submit

You will edit the following files included with the homework in the directory hw3-files:

- logistic_regression.ipynb
- logistic_regression.py
- sms_classify.py

The directory includes these additional files with data, code, or documentation that you will not need to edit:

- util.py
- book-data.csv
- sms.txt
- sms_readme.txt

Complete the requested code in these files, then follow these steps:

- 1. written solutions. Create a single high-quality pdf with your solutions to the exercises and extra credit, if applicable. The solutions can be typed or written and scanned but the resulting pdf must be high quality and easily readable. Upload the pdf to Gradescope.
- 2. **code listing**. When you are done editing and ready to submit your code listing, in the hw3-files directory create a new file called hw3-code.pdf with a listing of all of your code and results. Open the pdf to make sure it is correct and includes all of your code and plots. You can run this multiple times if you update your code.
- 3. Submit a single zip file containing source code solutions and listing to Moodle. Make sure your code is complete and files are included in the directory. Also include any auxiliary data or code files you created that are needed to run your code.

Rename your code directory from hw3-files to hw3-<your last name> and zip it:

```
$ mv hw3-files hw3-parente
```

\$ zip -r hw3-parente.zip hw3-parente

Submit the single zip file to Moodle.

Problems

Let $g(z) = \frac{1}{1 + e^{-z}}$ be the logistic function.

Problem 1 (5 points). Show that $\frac{d}{dz}g(z) = g(z)(1 - g(z))$.

Problem 2 (5 points). Show that 1 - g(z) = g(-z).

Problem 3 (5 points). Consider the log loss function for logistic regression simplified so there is only one training example:

$$J(\boldsymbol{\theta}) = -y \log h_{\boldsymbol{\theta}}(\mathbf{x}) - (1 - y) \log(1 - h_{\boldsymbol{\theta}}(\mathbf{x})), \qquad h_{\boldsymbol{\theta}}(\mathbf{x}) = g(\boldsymbol{\theta}^T \mathbf{x}) = \frac{1}{1 + e^{-\boldsymbol{\theta}^T \mathbf{x}}}$$

Show that the partial derivative with respect to θ_j is:

$$\frac{\partial}{\partial \theta_i} J(\boldsymbol{\theta}) = (h_{\boldsymbol{\theta}}(\mathbf{x}) - y) x_j$$

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Problem 4 (10 points). Logistic regression for book classification. In this problem, you will implement logistic regression for book classification. Open the jupyter notebook logistic_regression.ipynb and follow the instructions to complete the problem.

Problem 5 (10 points). SMS spam classification. In this problem you will use your implementation of logistic regression to create a spam classifier for SMS messages. Open the jupyter notebook sms_classify.ipynb and follow the instructions to complete the problem.

Problem 6 (5 points). Mandatory for ECE597ML - SMS spam classification When looking at the vocabulary and at the mistakes the algorithm in sms_classify.ipynb makes, suggest a couple of ways the algorithm can be modified to improve the classification accuracy.