



Data Structures with C++ : CS189

Lecture 7-2: Binary Search Trees

Recap

- A tree gives us the ability to look up data in log time instead of n
- To find data, it starts with a pointer to the root, and travels left to find smaller data, and right to find larger data
- The basic BST doesn't allow duplicates
- STL does not offer a BST container, but STL's "Set" is mostly the same

Recursive?

- A tree does not automatically mean recursion
- The guiding principle is if an algo needs to fork, it is recursive. Otherwise use a loop.
- There is exactly one path from the top to what you are looking for, so it doesn't fork
- Something that *needs* to touch every node (copy) is recursive because it forks

Different Implementation

```
struct VectorTreeNode {  
    T mData;  
    int mLeftIndex;  
    int mRightIndex;  
};
```

```
class BST {  
    vector  
    <VectorTreeNode>  
    mNodes;  
};
```

- You don't know how STL implements Sets
 - Information Hiding!
- It happens to use a red-black tree last time I looked it up
 - Variations of trees are later.
 - Red-black is "better but slower" and "hella hard"
- Why not a Vector?
 - Vectors can't shrink well
 - That's how Heaps work later on though
- Pointers and indexes both mean "Where can I find the next one?"

Deleting Nodes

Note:

In the next few slides there are mentions of Double Pointers. They were causing too much trouble and they weren't the point, so I replaced them with the Parent pointer.

- Draw a picture of a tree
- Deleting a leaf is easy, but what if there are two children?
- Algorithm is this:
 - No children? Delete it
 - One child? Whomever was pointing at me now points at my child. (Skip me.) Now delete.
 - Two children? Don't delete the node! Find the next highest piece of data, swap data, and delete *their* old node. (Which might have a right child.)
 - "Next highest" = Take one step right and then as many lefts as you can. "The smallest data bigger than us."

Now a Set

```
struct SetNode {  
    T mData;  
    TreeNode *mLeft;  
    TreeNode *mRight;  
    TreeNode *mParent;  
};
```

- One more time, tree is the tech, Set is the ADT
- The only difference is that to make remove easier, the node gets an "up" pointer
 - Breaks scientific definition of tree
- Without being able to go up, we need to have two walkers so we can stitch the tree back together
 - Or *shudder* Double-pointers
- Being able to go up also lets us go left and right
 - This is how Set's iterator can have a Next.

Map

```
struct MapNode {  
    K mKey;  
    V mValue;  
    TreeNode *mLeft;  
    TreeNode *mRight;  
    TreeNode *mParent;  
};
```

```
map<string,int> tAges;  
tAges["Bob"] = 42;
```

- A Map is a Set, but with two pieces of data in each node
- The Key is used as the search term
- The Value is used for the resulting data
 - We saw this usage in the "Use STL" week before
- Remember, maps have two separate template types
 - Only the Key must have $<$ or a Functor.
- Almost every place we had a T, we now have a K
 - The only place V shows up is as return values

Map/Operator Rant

```
map<string, int>ages;  
ages["Bob"] = 4;  
if( ages.find("Bob") !=  
    ages.end() )  
    cout << "Yes";
```

```
if( ages.find("Alice") !=  
    ages.end() )  
    cout << "No";
```

```
int Y = ages["Alice"];  
if( ages.find("Alice") !=  
    ages.end() )  
    cout << "YES!?!";
```

- I personally think Maps are the coolest
- But in order to look like an array, it uses operator [], which returns a reference like other containers' accessors
- But if you access a map with a key that is not there, the key GETS ADDED
 - The getter is NOT CONST?!?!
- No other language does that
 - There is a method called At that does a get but without that horrible horribleness
 - It's not really a bug, it's just how [] works
 - One reason I hate operator overloading
 - $A * B \neq B * A$ is another



End

Anybody who leaves early and doesn't get an A is a silly person