

Fourier Transform Pairs		Fourier Transform Operations	
$x(t)$	$X(f)$	$x(t)$	$X(f)$
$e^{-at}u(t)$	$\frac{1}{a+j2\pi f}$	$a > 0$	$kx(t)$
$e^{at}u(-t)$	$\frac{1}{a-j2\pi f}$	$a > 0$	$x_1(t)+x_2(t)$
$e^{-a t }$	$\frac{2a}{a^2+(2\pi f)^2}$	$a > 0$	$X^*(t)$
$\delta(t)$	1		$X(t)$
1	$\delta(f)$		$x(-f)$
$e^{j2\pi f_0 t}$	$\delta(f-f_0)$		$x(at)$
$\cos 2\pi f_0 t$	$\frac{1}{2}[\delta(f-f_0)+\delta(f+f_0)]$		$\frac{1}{ a }X\left(\frac{f}{a}\right)$
$\sin 2\pi f_0 t$	$\frac{1}{j2}[\delta(f-f_0)-\delta(f+f_0)]$		$x(t-t_0)$
$u(t)$	$\frac{1}{2}\delta(f)+\frac{1}{j2\pi f}$		$X(f)e^{-j2\pi f t_0}$
$\text{rect}\left(\frac{t}{T}\right) = \begin{cases} 1, & t \leq T/2, \\ 0, & t > T/2. \end{cases}$	$T \text{sinc}(fT)$		$x(t)e^{j2\pi f_0 t}$
$\Lambda\left(\frac{t}{T}\right) = \begin{cases} 1 - \frac{ t }{T}, & t \leq T, \\ 0, & t > T. \end{cases}$	$T \text{sinc}^2(fT)$		$X(f-f_0)$
$\text{sinc}(2Wt) = \frac{\sin(2W\pi t)}{2W\pi t}$	$\frac{1}{2W} \text{rect}\left(\frac{f}{2W}\right)$		$x_1(t)*x_2(t)$
$\sum_{n=-\infty}^{\infty} \delta(t-nT_0)$	$\frac{1}{T_0} \sum_{n=-\infty}^{\infty} \delta(f-nf_0)$	$f_0 = \frac{1}{T_0}$	$X_1(f)*X_2(f)$
Useful Trigonometric Identities			
$\exp(\pm j\theta) = \cos(\theta) \pm j \sin(\theta)$		$\cos(A) + \cos(B) = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$	
$\cos(\theta) = \frac{1}{2} [\exp(j\theta) + \exp(-j\theta)]$		$\sin(\theta) = \frac{1}{2j} [\exp(j\theta) - \exp(-j\theta)]$	
$2 \cos(A) \cos(B) = \cos(A-B) + \cos(A+B)$		$\cos^2(A) = \frac{1}{2} [1 + \cos(2A)]$	
$2 \sin(A) \sin(B) = \cos(A-B) - \cos(A+B)$		$\sin^2(A) = \frac{1}{2} [1 - \cos(2A)]$	
$2 \cos(A) \sin(B) = \sin(A+B) - \sin(A-B)$		$\sin(2A) = 2 \cos(A) \sin(A)$	
$\cos(A \pm B) = \cos(A)\cos(B) \mp \sin(A)\sin(B)$		$\sin(A \pm B) = \sin(A)\cos(B) \pm \cos(A)\sin(B)$	