

Fourier Transform Pairs			Fourier Transform Operations	
$x(t)$	$X(f)$		$x(t)$	$X(f)$
$e^{-at}u(t)$	$\frac{1}{a + j2\pi f}$	$a > 0$	$kx(t)$	$kX(f)$
$e^{at}u(-t)$	$\frac{1}{a - j2\pi f}$	$a > 0$	$x_1(t) + x_2(t)$	$X_1(f) + X_2(f)$
$e^{-a t }$	$\frac{2a}{a^2 + (2\pi f)^2}$	$a > 0$	$x^*(t)$	$X^*(-f)$
$\delta(t)$	1		$X(t)$	$x(-f)$
1	$\delta(f)$		$x(at)$	$\frac{1}{ a }X\left(\frac{f}{a}\right)$
$e^{j2\pi f_0 t}$	$\delta(f - f_0)$		$x(t - t_0)$	$X(f)e^{-j2\pi f t_0}$
$\cos 2\pi f_0 t$	$\frac{1}{2}[\delta(f - f_0) + \delta(f + f_0)]$		$x(t)e^{j2\pi f_0 t}$	$X(f - f_0)$
$\sin 2\pi f_0 t$	$\frac{1}{j2}[\delta(f - f_0) - \delta(f + f_0)]$		$x_1(t) * x_2(t)$	$X_1(f)X_2(f)$
$u(t)$	$\frac{1}{2}\delta(f) + \frac{1}{j2\pi f}$		$x_1(t)x_2(t)$	$X_1(f) * X_2(f)$
$\text{rect}\left(\frac{t}{T}\right) = \begin{cases} 1, &  t  \leq T/2, \\ 0, &  t  > T/2. \end{cases}$	$T \text{sinc}(fT)$		$\frac{d^n x(t)}{dt^n}$	$(j2\pi f)^n X(f)$
$\Lambda\left(\frac{t}{T}\right) = \begin{cases} 1 - \frac{ t }{T}, &  t  \leq T, \\ 0, &  t  > T. \end{cases}$	$T \text{sinc}^2(fT)$		$\int_{-\infty}^t x(u)du$	$\frac{X(f)}{j2\pi f} + \frac{X(0)}{2}\delta(f)$
$\text{sinc}(2Wt) = \frac{\sin(2W\pi t)}{2W\pi t}$	$\frac{1}{2W} \text{rect}\left(\frac{f}{2W}\right)$			
$\sum_{n=-\infty}^{\infty} \delta(t - nT_0)$	$\frac{1}{T_0} \sum_{n=-\infty}^{\infty} \delta(f - nf_0)$	$f_0 = \frac{1}{T_0}$		
Useful Trigonometric Identities				
$\exp(\pm j\theta) = \cos(\theta) \pm j\sin(\theta)$	$\cos(A) + \cos(B) = 2\cos\left(\frac{A+B}{2}\right)\cos\left(\frac{A-B}{2}\right)$			
$\cos(\theta) = \frac{1}{2}[\exp(j\theta) + \exp(-j\theta)]$	$\sin(\theta) = \frac{1}{2j}[\exp(j\theta) - \exp(-j\theta)]$			
$2\cos(A)\cos(B) = \cos(A-B) + \cos(A+B)$	$\cos^2(A) = \frac{1}{2}[1 + \cos(2A)]$			
$2\sin(A)\sin(B) = \cos(A-B) - \cos(A+B)$	$\sin^2(A) = \frac{1}{2}[1 - \cos(2A)]$			
$2\cos(A)\sin(B) = \sin(A+B) - \sin(A-B)$	$\sin(2A) = 2\cos(A)\sin(A)$			
$\cos(A \pm B) = \cos(A)\cos(B) \mp \sin(A)\sin(B)$	$\sin(A \pm B) = \sin(A)\cos(B) \pm \cos(A)\sin(B)$			