

Assignment 5 pdf:

Description:

In this assignment, I will be creating an application that uses public key encryption to encrypt and decrypt files, using the ss algorithm. The way that public key encryption works are by having four keys two public and two private. The private keys are generated by the user. Let's say I want to send an encrypted file safely to another person. I can use the public key to encrypt the file and only the creator with the private key is able to decrypt the file. Let's say this user wants to send back an encrypted file and make sure it is from them they will encrypt their file using a private key and I will decrypt the file using the public key if it is not nonsense I know it came from the owner of the private key. I will create a keygen program that generates the private keys and public keys that will be used for decryption and encryption. I will create a decryption executable, that takes either a public key or a private key and decrypts a file. Finally, I will create an encryption executable that will encrypt a file using either a private key or a public key.

Files to include:

- `decrypt.c`: This contains the implementation and `main()` function for the decrypt program
- `encrypt.c`: This contains the implementation and `main()` function for the encrypt program.
- `keygen.c`: This contains the implementation and `main()` function for the keygen program.
- `numtheory.c`: This contains the implementations of the number theory functions.
- `numtheory.h`: This specifies the interface for the number theory functions.
- `randstate.c`: This contains the implementation of the random state interface for the SS library and number theory functions.
- `randstate.h`: This specifies the interface for initializing and clearing the random state.
- `ss.c`: This contains the implementation of the SS library
- `ss.h`: This specifies the interface for the SS library

`randstate.c`:

- `void randstate_init(uint64_t seed)`
initializes the global random state named `state` with a Mersenne Twister algorithm, using `seed` as the random seed. You should call `srandom()` using this seed as well. This function will also entail calls to `gmp_randinit_mt()` and to `gmp_randseed_ui()`.
- `void randstate_clear(void)`
Clears and frees all memory used by the initialized global random state named `state`. This should just be a single call to `gmp_randclear()`

`numtheory.c`

- `void pow_mod(mpz_t out, mpz_t base, mpz_t exponent, mpz_t modulus)`

Performs fast modular exponentiation, computing base raised to the exponent power modulo modulus, and storing the computed result in out.

Using the provided algorithm

- `bool is_prime(mpz_t n, uint64_t iters)`
Conducts the Miller-Rabin primality test to indicate whether or not n is prime using iters number of Miller-Rabin iterations. This function is needed when creating the two large primes p and q in SS, verifying if a large integer is a prime. In addition to the `is_prime()` function. Use the algorithm provided
- `void make_prime(mpz_t p, uint64_t bits, uint64_t iters)`
Generates a new prime number stored in p . The generated prime should be at least bits number of bits long. The primality of the generated number should be tested using `is_prime()` using iters number of iterations.
- `void gcd(mpz_t d, mpz_t a, mpz_t b)`
Computes the greatest common divisor of a and b , storing the value of the computed divisor in d . Use algorithm provided
- `void mod_inverse(mpz_t i, mpz_t a, mpz_t n)`
Computes the inverse i of a modulo n . In the event that a modular inverse cannot be found, set i to 0. Note that this pseudocode uses parallel assignments, which C does not support. Thus, you will need to use auxiliary variables to fake the parallel assignments. Use the algorithm provided

ss.c

- `void ss_make_pub(mpz_t p, mpz_t q, mpz_t n, uint64_t nbits, uint64_t iters)`
Creates parts of a new SS public key: two large primes p and q , and n computed as $p * p * q$. Begin by creating primes p and q using `make_prime()`. We first need to decide the number of bits that go to each prime respectively such that $\log_2(n) \geq \text{nbits}$. Let the number of bits for p be a random number in the range $[\text{nbits}/5, (2 \times \text{nbits})/5]$. Recall that $n = p^2 \times q$: the bits from p will be contributed to n twice, the remaining bits will go to q . The number of Miller-Rabin iterations is specified by iters . You should obtain this random number using `random()` and check that $p \nmid q-1$ and $q \nmid p-1$.
- `void ss_write_pub(mpz_t n, char username[], FILE *pbfile)`
Writes a public SS key to pbfile . The format of a public key should be n , then the username, each of which are written with a trailing newline. The value n should be written as a hexstring. See the GMP functions for formatted output for help with writing hexstrings.
- `void ss_read_pub(mpz_t n, char username[], FILE *pbfile)`
Reads a public SS key from pbfile . The format of a public key should be n , then the username, each of which should have been written with a trailing newline. The value n should have been written as a hexstring. See the GMP functions for formatted input for help with reading hexstrings.
- `void ss_make_priv(mpz_t d, mpz_t p, mpz_t q)`
Creates a new SS private key d given primes p and q and the public key n . To compute d , simply compute the inverse of n modulo $\lambda(pq) = \text{lcm}(p-1, q-1)$.
- `void ss_write_priv(mpz_t pq, mpz_t d, FILE *pvfile)`

Writes a private SS key to pvfile. The format of a private key should be pq then d, both of which are written with a trailing newline. Both these values should be written as hexstrings.

- `void ss_read_priv(mpz_t pq, mpz_t d, FILE *pvfile)`
Reads a private SS key from pvfile. The format of a private key should be pq then d, both of which should have been written with a trailing newline. Both these values should have been written as hexstrings
- `void ss_encrypt(mpz_t c, mpz_t m, mpz_t n)`
Performs SS encryption, computing the ciphertext c by encrypting message m using the public key n. Remember, encryption with SS is defined as $E(m) = c = mn \pmod n$.
- `void ss_encrypt_file(FILE *infile, FILE *outfile, mpz_t n)`
Encrypts the contents of infile, writing the encrypted contents to outfile. The data in infile should be in encrypted in blocks. Why not encrypt the entire file? Because of n. We are working modulo n, which means that the value of the block of data we are encrypting must be strictly less than n. We have two additional restrictions on the values of the blocks we encrypt:
 1. The value of a block cannot be 0: $E(0) \equiv 0 \equiv 0 \pmod n$.
 2. The value of a block cannot be 1. $E(1) \equiv 1 \equiv 1 \pmod n$.
A solution to these additional restrictions is to simply prepend a single byte to the front of the block we want to encrypt. The value of the prepended byte will be 0xFF. This solution is not unlike the padding schemes such as PKCS and OAEP used in modern constructions of RSA. To encrypt a file, follow these steps:
 1. Calculate the block size k. This should be $k = b(\log_2(pn) - 1) / 8$.
 2. Dynamically allocate an array that can hold k bytes. This array should be of type `(uint8_t *)` and will serve as the block.
 3. Set the zeroth byte of the block to 0xFF. This effectively prepends the workaround byte that we need.
 4. While there are still unprocessed bytes in infile: (a) Read at most k-1 bytes in from infile, and let j be the number of bytes actually read. Place the read bytes into the allocated block starting from index 1 so as to not overwrite the 0xFF. (b) Using `mpz_import()`, convert the read bytes, including the prepended 0xFF into an `mpz_t m`. You will want to set the order parameter of `mpz_import()` to 1 for most significant word first, 1 for the endian parameter, and 0 for the nails parameter. (c) Encrypt m with `ss_encrypt()`, then write the encrypted number to outfile as a hexstring followed by a trailing newline.
- `void ss_decrypt(mpz_t m, mpz_t c, mpz_t d, mpz_t pq)`
Performs SS decryption, computing message m by decrypting ciphertext c using private key d and public modulus n. Remember, decryption with SS is defined as $D(c) = m = c d \pmod{pq}$.
- `void ss_decrypt_file(FILE *infile, FILE *outfile, mpz_t pq, mpz_t d)`

Decrypts the contents of infile, writing the decrypted contents to outfile. The data in infile should be decrypted in blocks to mirror how `ss_encrypt_file()` encrypts in blocks. To decrypt a file, follow these steps:

1. Dynamically allocate an array that can hold $k = b(\log_2(pq) - 1)/8c$ bytes. This array should be of type `(uint8_t *)` and will serve as the block. • We need to ensure that our buffer is able to hold at least the number of bits that were used during the encryption process. In this context we don't know the value of n , but we can overestimate the number of bits in p using pq .

2 Iterating over the lines in infile:

(a) Scan in a hexstring, saving the hexstring as a `mpz_t c`. Remember, each block is written as a hexstring with a trailing newline when encrypting a file.

(b) First decrypt c back into its original value m . Then using `mpz_export()`, convert m back into bytes, storing them in the allocated block. Let j be the number of bytes actually converted. You will want to set the order parameter of `mpz_export()` to 1 for most significant word first, 1 for the endian parameter, and 0 for the nails parameter.

(c) Write out $j-1$ bytes starting from index 1 of the block to outfile. This is because index 0 must be prepended `0xFF`. Do not output the `0xFF`.

keygen.c

- Parse command-line options using `getopt()` and handle them accordingly
- Open the public and private key files using `fopen()`. Print a helpful error and exit the program in the event of failure
- Using `fchmod()` and `fileno()`, make sure that the private key file permissions are set to `0600`, indicating read and write permissions for the user, and no permissions for anyone else
- Initialize the random state using `randstate_init()`, using the set seed
- Make the public and private keys using `ss_make_pub()` and `ss_make_priv()`, respectively
- Get the current user's name as a string. You will want to use `getenv()`
- Write the computed public and private key to their respective files.
- If verbose output is enabled print the following, each with a trailing newline, in order: (a) username (b) the first large prime p (c) the second large prime q (d) the public key n (e) the private exponent d (f) the private modulus pq
- All of the `mpz_t` values should be printed with information about the number of bits that constitute them, along with their respective values in decimal. See the reference key generator program for an example.
- Close the public and private key files, clear the random state with `randstate_clear()`, and clear any `mpz_t` variables you may have used.

encrypt.c

- Parse command-line options using `getopt()` and handle them accordingly.
- Open the public key file using `fopen()`. Print a helpful error and exit the program in the event of failure
- Read the public key from the opened public key file.

- If verbose output is enabled print the following, each with a trailing newline, in order: (a) username (b) the public key n All of the mpz_t values should be printed with information about the number of bits that constitute them, along with their respective values in decimal. See the reference encryptor program for an example
- Encrypt the file using ss_encrypt_file()
- Close the public key file and clear any mpz_t variables you have used.

decrypt.c

- Parse command-line options using getopt() and handle them accordingly
- Open the private key file using fopen(). Print a helpful error and exit the program in the event of failure
- Read the private key from the opened private key file
- If verbose output is enabled print the following, each with a trailing newline, in order: (a) the private modulus pq (b) the private key d Both these values should be printed with information about the number of bits that constitute them, along with their respective values in decimal. See the reference decryptor program for an example
- Decrypt the file using ss_decrypt_file()
- Close the private key file and clear any mpz_t variables you have used.