

Suppose a company offers three different delivery methods for their products: standard delivery, express delivery, and same-day delivery

60% of customers choose standard delivery, 30% choose express delivery, and 10% choose same-day delivery

The delivery success rates are 95% for standard delivery, 90% for express delivery, and 85% for same-day delivery

If a customer's delivery fails, what is the probability that they chose express delivery?

$$P(A) = 60\%, P(B) = 30\%, P(C) = 10\%$$

$$P(\text{Suc} | A) = 0.95, P(\text{Suc} | B) = 0.9, P(\text{Suc} | C) = 0.85$$

$$P(B | \text{Fail}) = ?$$

Jawab:

$$P(B | \text{Fail}) = P(\text{Fail} | B) * P(B) / P(\text{Fail})$$

$$P(\text{Suc}) = P(\text{Suc} | A) * P(A) + P(\text{Suc} | B) * P(B) + P(\text{Suc} | C) * P(C)$$

$$P(\text{Suc}) = 0.95 * 0.6 + 0.9 * 0.3 + 0.85 * 0.1 = 0.925$$

$$P(\text{Fail}) = 0.075$$

$$P(B | \text{Fail}) = P(\text{Fail} | B) * P(B) / P(\text{Fail})$$

$$\mathbf{P(B | Fail) = 0.1 * 0.3 / 0.075 = 0.4}$$

If a medical test is 95% accurate in detecting a disease and 1% of the population has the disease

Calculate the probability of having the disease given a positive test result!

$$P(\text{Pos} | D) = 0.95$$

$$P(\text{Neg} | \text{noD}) = 0.05$$

$$P(D) = 0.01$$

$$P(\text{noD}) = 0.99$$

Jawab:

$$P(D | \text{Pos}) = P(\text{Pos} | D) * P(D) / P(\text{Pos}) = 0.95 * 0.01 / P(\text{Pos})$$

$$P(\text{Pos}) = P(\text{Pos} | D) * P(D) + P(\text{Neg} | \text{noD}) * P(\text{noD}) = 0.95 * 0.01 + 0.05 * 0.99 = 0.059$$

$$\mathbf{P(D | Pos) = 0.95 * 0.01 / 0.059 = 0.161}$$