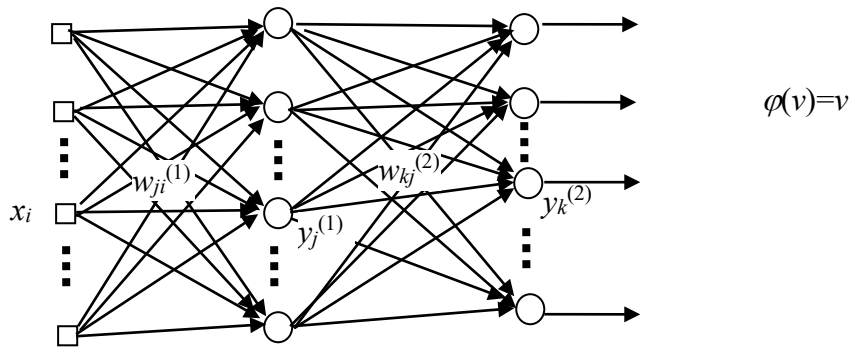


SOLUTION FOR PB5

1.



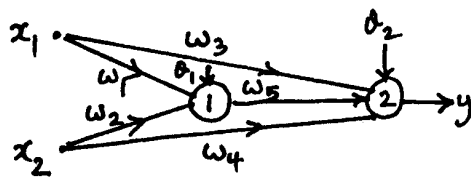
$$y_k^{(2)} = \sum_j w_{kj}^{(2)} y_j^{(1)}$$

$$y_j^{(1)} = \sum_i w_{ji}^{(1)} x_i$$

Therefore,

$$\begin{aligned} y_k^{(2)} &= \sum_j w_{kj}^{(2)} y_j^{(1)} = \sum_j w_{kj}^{(2)} \left(\sum_i w_{ji}^{(1)} x_i \right) \\ &= \sum_j \sum_i w_{kj}^{(2)} w_{ji}^{(1)} x_i \\ &= \sum_i \sum_j w_{kj}^{(2)} w_{ji}^{(1)} x_i \\ &= \sum_i w_{ki} x_i \\ \text{where } w_{ki} &= \sum_j w_{kj}^{(2)} w_{ji}^{(1)} \end{aligned}$$

2.



$\varphi = \text{sigmoid}$ $u = \text{Neuron 1 output}$

$$v_1 = w_1 x_1 + w_2 x_2 - \theta_1 \quad u = \varphi(v_1)$$

$$v_2 = w_3 x_1 + w_4 x_2 + w_5 u - \theta_2, \quad y = \varphi(v_2)$$



$$\frac{\partial e}{\partial y} = \frac{d}{y} - \frac{(1-d)}{(1-y)} ; \quad \frac{\partial e}{\partial v_2} = \frac{\partial e}{\partial y} \cdot \frac{\partial y}{\partial v_2} = \frac{\partial e}{\partial y} \cdot \varphi'(v_2);$$

$$\frac{\partial e}{\partial u} = \frac{\partial e}{\partial v_2} \cdot \frac{\partial v_2}{\partial u} = \frac{\partial e}{\partial v_2} \cdot w_5 ; \quad \frac{\partial e}{\partial v_1} = \frac{\partial e}{\partial u} \cdot \frac{\partial u}{\partial v_1} = \frac{\partial e}{\partial u} \cdot \varphi'(v_1);$$

$$\frac{\partial e}{\partial x_1} = \frac{\partial e}{\partial v_1} \cdot \frac{\partial v_1}{\partial x_1} + \frac{\partial e}{\partial v_2} \cdot \frac{\partial v_2}{\partial x_1} = \frac{\partial e}{\partial v_1} \cdot w_1 + \frac{\partial e}{\partial v_2} \cdot w_3 ;$$

$$\frac{\partial e}{\partial x_2} = \frac{\partial e}{\partial v_1} \cdot \frac{\partial v_1}{\partial x_2} + \frac{\partial e}{\partial v_2} \cdot \frac{\partial v_2}{\partial x_2} = \frac{\partial e}{\partial v_1} \cdot w_2 + \frac{\partial e}{\partial v_2} \cdot w_4$$