

VS

Solution

24 / Oct / 2017

Prj 1

Prj 2

Source

main.c

"build a solution"

✓

# Syntax

printf ( ) ✓

scanf ( )

VS



scanf\_s ( )

strcpy (a, b)



strcpy\_s ( )

---

if - else if - else

switch

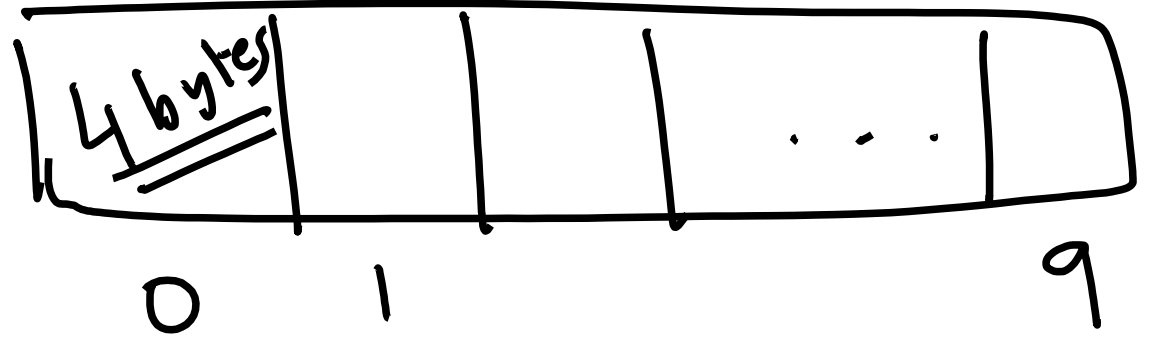
loops — while

do-while

for

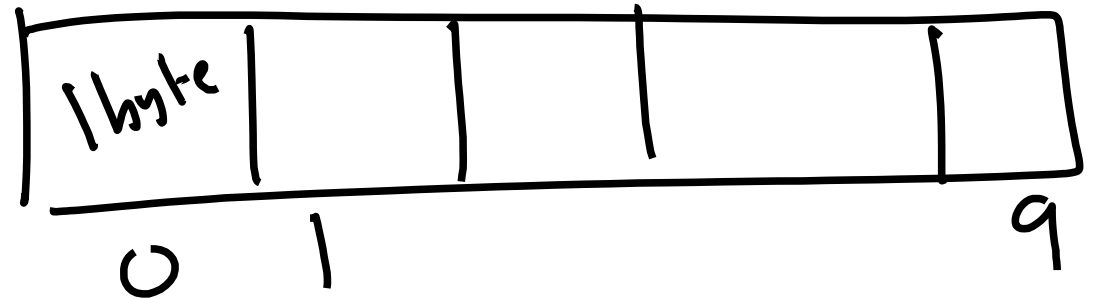
# Arrays

int array[10];



float values[10];

char name[10];

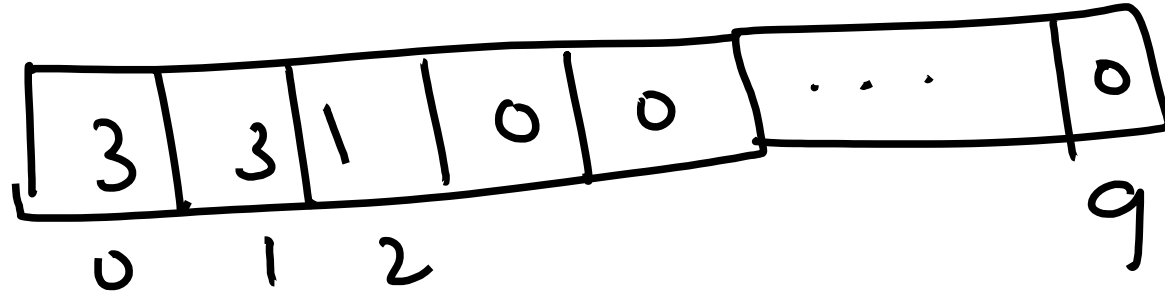


array[~~i~~] = array[i] + 10;

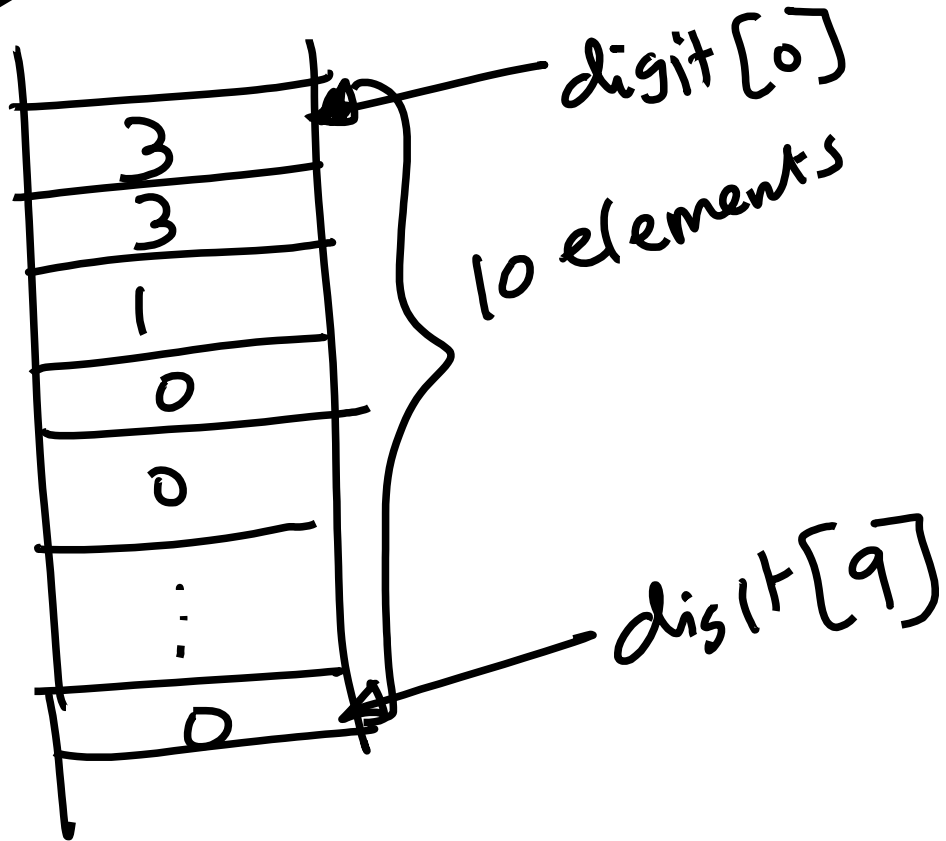
T3-1

(a)

int digits[10] = {3, 3, 1};



RAM



73.2

```
float data[100], d[100], avg;
```

```
for (i=0; i<100; i++) {  
    avg = avg + data[i];  
}
```

avg = avg / 100; /\* avg / strlen? try this! \*/

```
for (i=0; i<100; i++) {  
    d[i] = data[i] - avg;
```

float array[10][10];

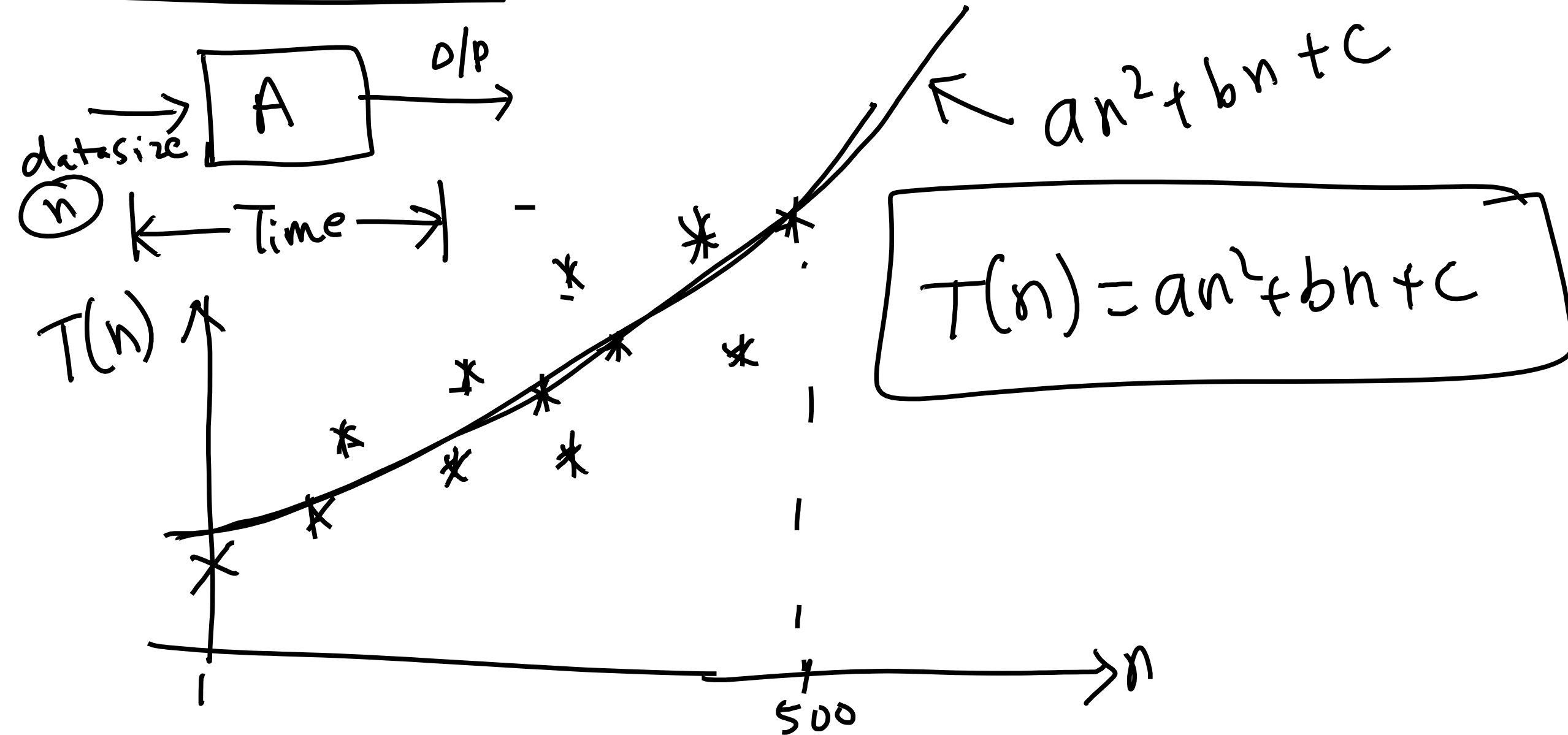
↓      ↓  
row    col

$$\begin{bmatrix} (0,0) & (0,1) & \dots & (0,9) \\ (1,0) & & & (1,9) \\ \vdots & & & \\ (9,0) & (9,1) & \dots & (9,9) \end{bmatrix}$$

array[3][4] = {1, 2, 3, 4, ..., 12};

array 
$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$$

# Time Complexity



$$T(n) = an^2 + bn + c$$

$n$	$\frac{T(n)}{n}$
1	$(a, b, c)$
5	$(a5^2, b5)$
$\vdots$	
500	$(500^2, 500)$
$\vdots$	
1 mil	$1\text{mil}^2, 1\text{mil}$

$\rightarrow n^2$  term dominates

$$n^3 + n^2 + n + k$$

Big  $O(\cdot)$

Order of complexity is  $\underline{\underline{n^2}}$   $O(n^2)$ .

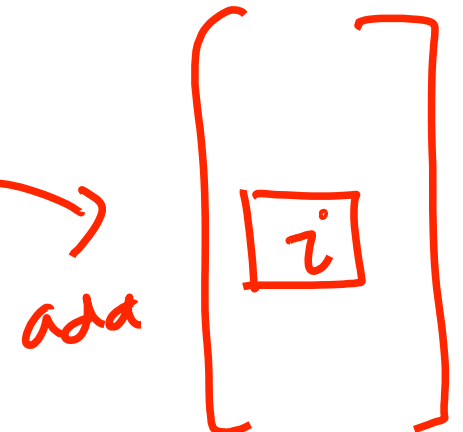
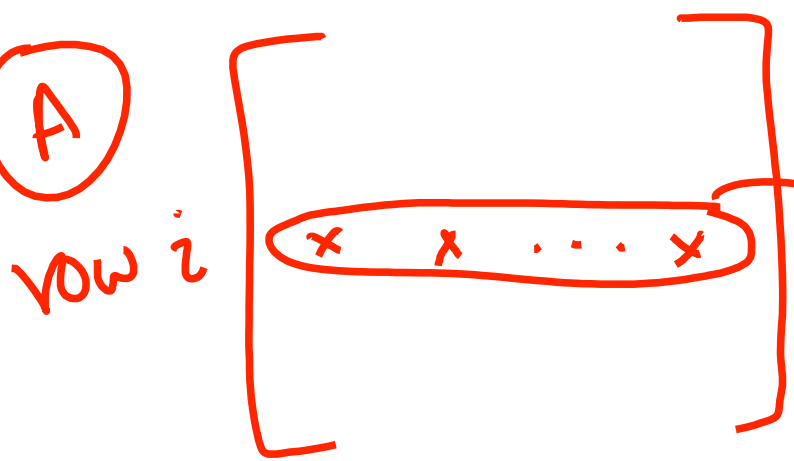


$\rightarrow$  for ( $i=0$ ;  $i < \underset{n}{100}$ ;  $i++$ ) {  
     for ( $j=0$ ;  $j < \underset{n}{100}$ ;  $j++$ ) {  $O(n^2)$ .  
          $a[i][j] = a[i][j] + 1;$   
     }  
   }

$\rightarrow$  }  
 $i - 100$

for a fixed  $i$   $j$  runs  $100 \times$   
 & that  $i$  runs  $100 \times$   
 $100 \times 100 = 10000$

(A)



$$b[i] = \sum_{j=0}^{N-1} a[i][j]$$

Time Complexity?  
 $O(N^2)$

```
for (i=0; i < N; i++) {  
    sum = 0;  
    for (j=0; j < N; j++)  
        sum = a[i][j] + sum;  
    b[i] = sum;  
}
```

$$b[i] = b[i] + a[i][j];$$

(B)  $\begin{bmatrix} A \\ N \times N \end{bmatrix} \begin{bmatrix} B \\ N \times N \end{bmatrix}$

$$\begin{bmatrix} (i,0) \\ \hline \end{bmatrix} \begin{bmatrix} (i,0) \\ \hline \end{bmatrix} = \begin{bmatrix} (i,0) \\ \hline \end{bmatrix}$$

$$a[i][0] + b[i][0] \Rightarrow c[i][0]$$

```
for (i=0; i<N; i++) {
```

Time Complexity ?

```
    for (j=0; j<N; j++) {
```

$O(N^2)$

```
        c[i][j] = a[i][i] + b[i][j];
```

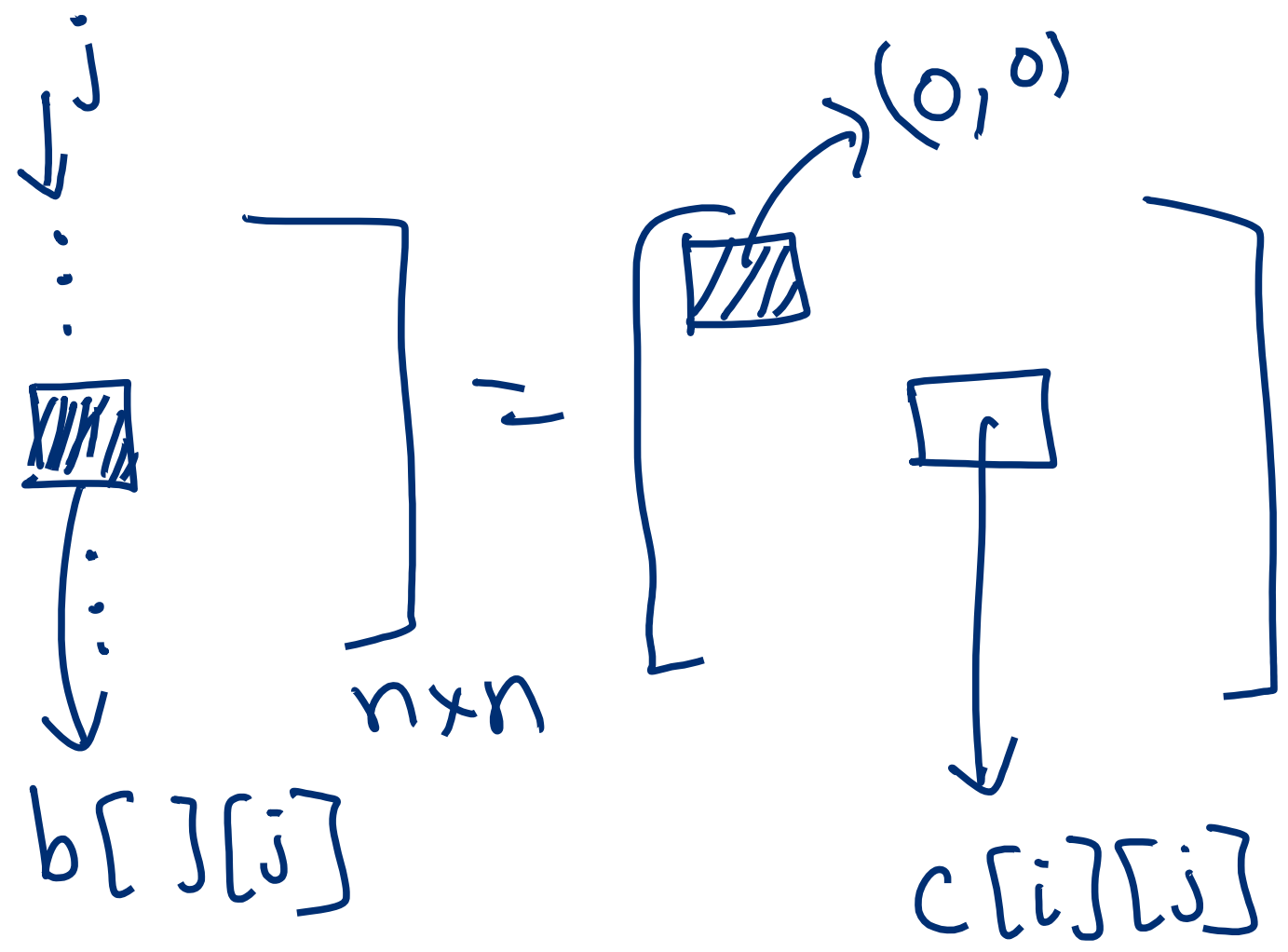
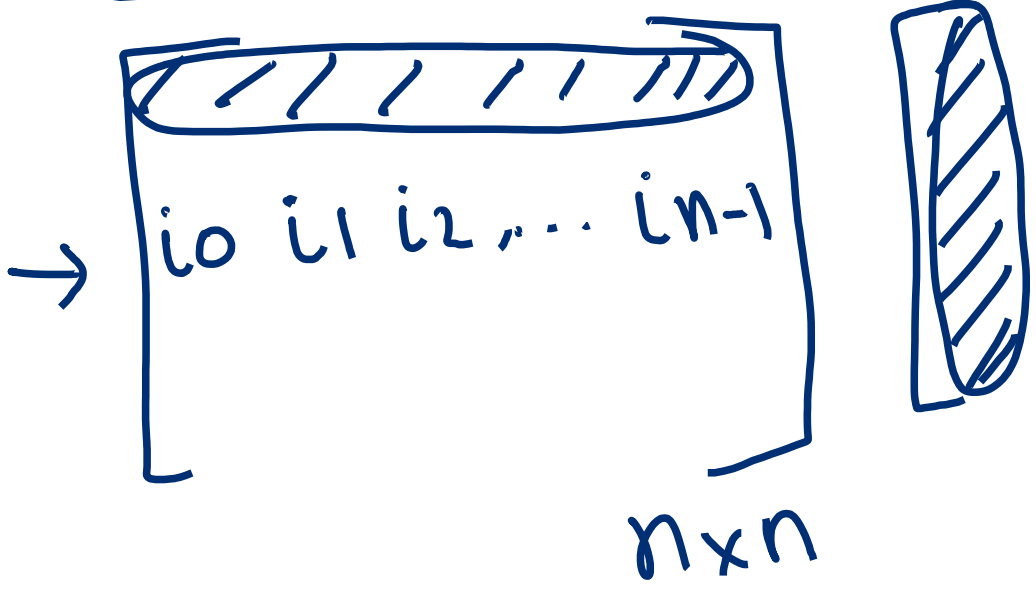
```
    }
```

```
}
```

```
int a[20][20], b[20][20],  
    c[20][20];
```

(C)

mat. mult-



$$a_{i0} b_{0j} + a_{i1} b_{1j}$$

$$+ a_{i2} \cdot b_{2j} + \dots$$

$$+ a_{ik} \cdot b_{kj} + \dots + a_{i,n-1} \cdot b_{n-1,j} = C_{ij}$$

$$\begin{bmatrix} a_{i0} \\ \vdots \end{bmatrix} \begin{bmatrix} \odot \\ \vdots \end{bmatrix}$$

$$C_{ij} = \sum_{k=0}^{n-1} a_{ik} \cdot b_{kj}$$

$$i = 0, 1, \dots, n-1$$

$$j = 0, 1, \dots, n-1$$

```

for (i=0; i<N; i++) {    /* row */
    for (j=0; j<N; j++) { /* col */
        for (k=0; k<N; k++) {
            c[i][j] = c[i][j] +
                a[i][k] * b[k][j];
        }
    }
}

```

Time complexity =  $O(N^3)$

# Space Complexity

integer size

(A)  $\underline{\underline{4}}n^2 + \underline{\underline{4}}n = \underline{\underline{4}}(n^2 + n) \rightarrow \underline{\underline{O(n^2)}}$

(B)  $n^2 + n^2 + n^2 = 3n^2 \rightarrow 4 \times 3n^2 = \underline{\underline{12n^2}}$

(C)  $n^2 + n^2 + n^2 = 3n^2 \rightarrow \underline{\underline{12n^2}}$



$$\textcircled{d} \quad \underset{N \times N}{A} \times \underset{N \times N}{A} = \underline{\underline{A^2 = B}}$$

$$\boxed{A^3} ?$$

$$\underbrace{A \times A \times A}_{\downarrow} \quad \downarrow$$

$$\underbrace{\cancel{B} \times A}_{C}$$

Time Complexity = ?

$$A \times A \rightarrow B$$

$$B \times A \rightarrow C$$

$$\textcircled{N^3}$$

$$\textcircled{N^3}$$

---


$$2N^3$$

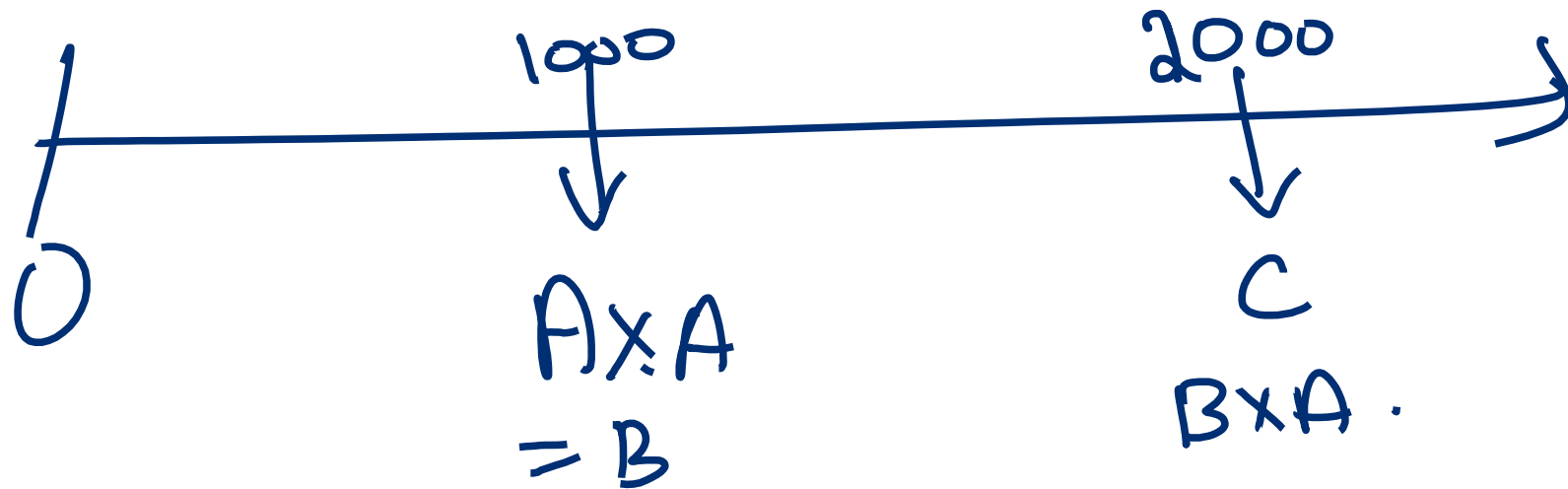

---

$$N=10 \quad t=1\text{msec}$$

$$\boxed{A^2} = O(N^3) \quad 10 \times 10 \times 10 = 1000 \times 1 = 1000 \text{ Msec}$$

↓  
B

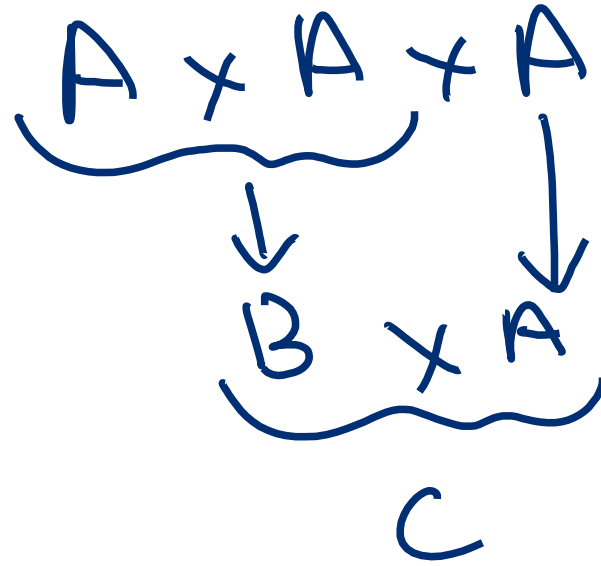
$$B \times A = O(N^3) = 1000 \text{ msec}$$



# Space Complexity

A, B, C

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ n^2 & n^2 & n^2 \end{array} = 3n^2$$



int →  $4 \times 3n^2 = 12n^2$  bytes

When the algo terminates mem. used =  $2n^2$   
=  $8n^2$  bytes