

VS

Solution

24 / Oct / 2017

Prj 1

Prj 2

Source

main.c

"build a solution"

✓

Syntax

printf () ✓

scanf ()

VS



scanf_s ()

strcpy (a, b)



strcpy_s ()

if - else if - else

switch

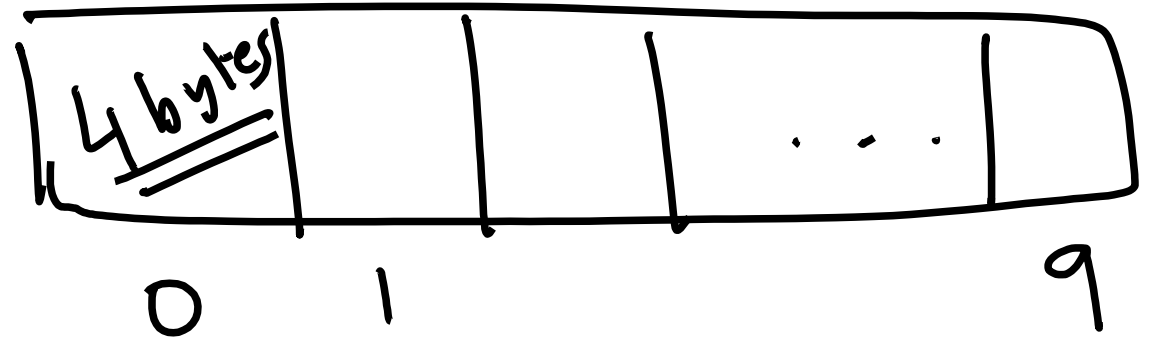
loops — while

do - while

for

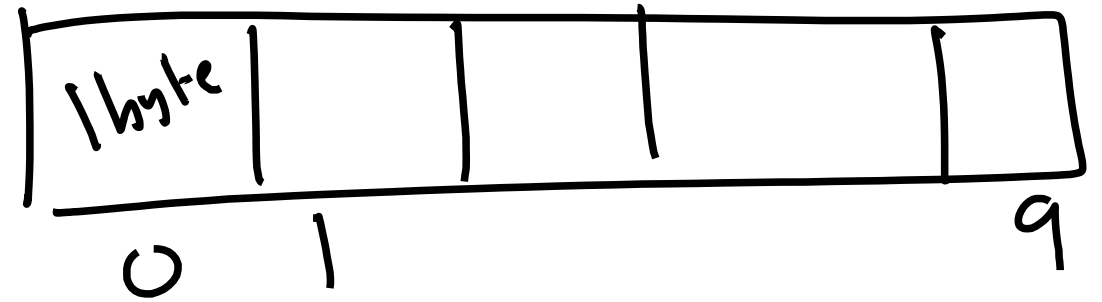
Arrays

`int array[10];`



`float values[10];`

`char name[10];`

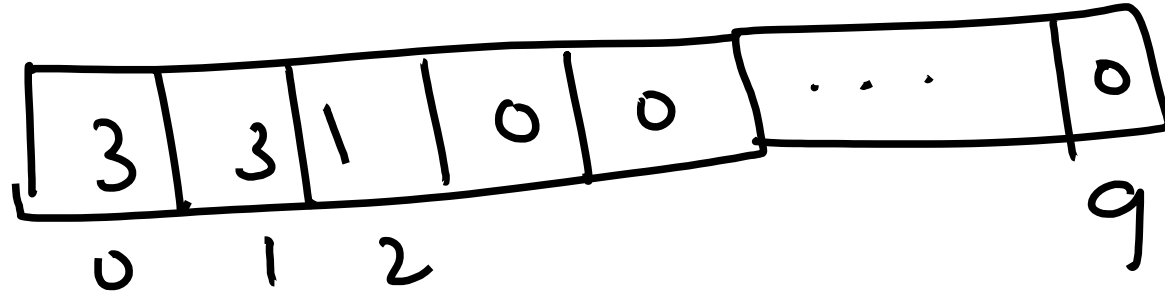


`array[i] = array[i] + 10;`

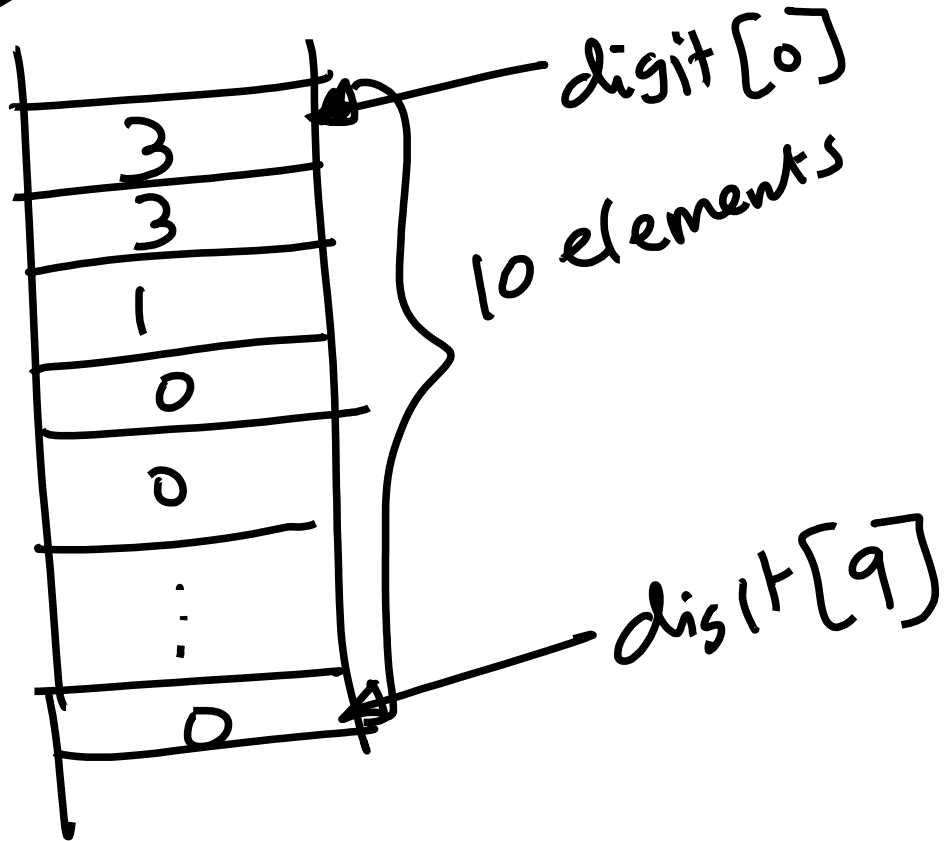
T3-1

(a)

int digits[10] = {3, 3, 1};



RAM



73.2

```
float data[100], d[100], avg;
```

```
for (i=0; i<100; i++) {  
    avg = avg + data[i];  
}
```

avg = avg / 100; /* avg / strlen? try this! */

```
for (i=0; i<100; i++) {  
    d[i] = data[i] - avg;
```

float array[10][10];

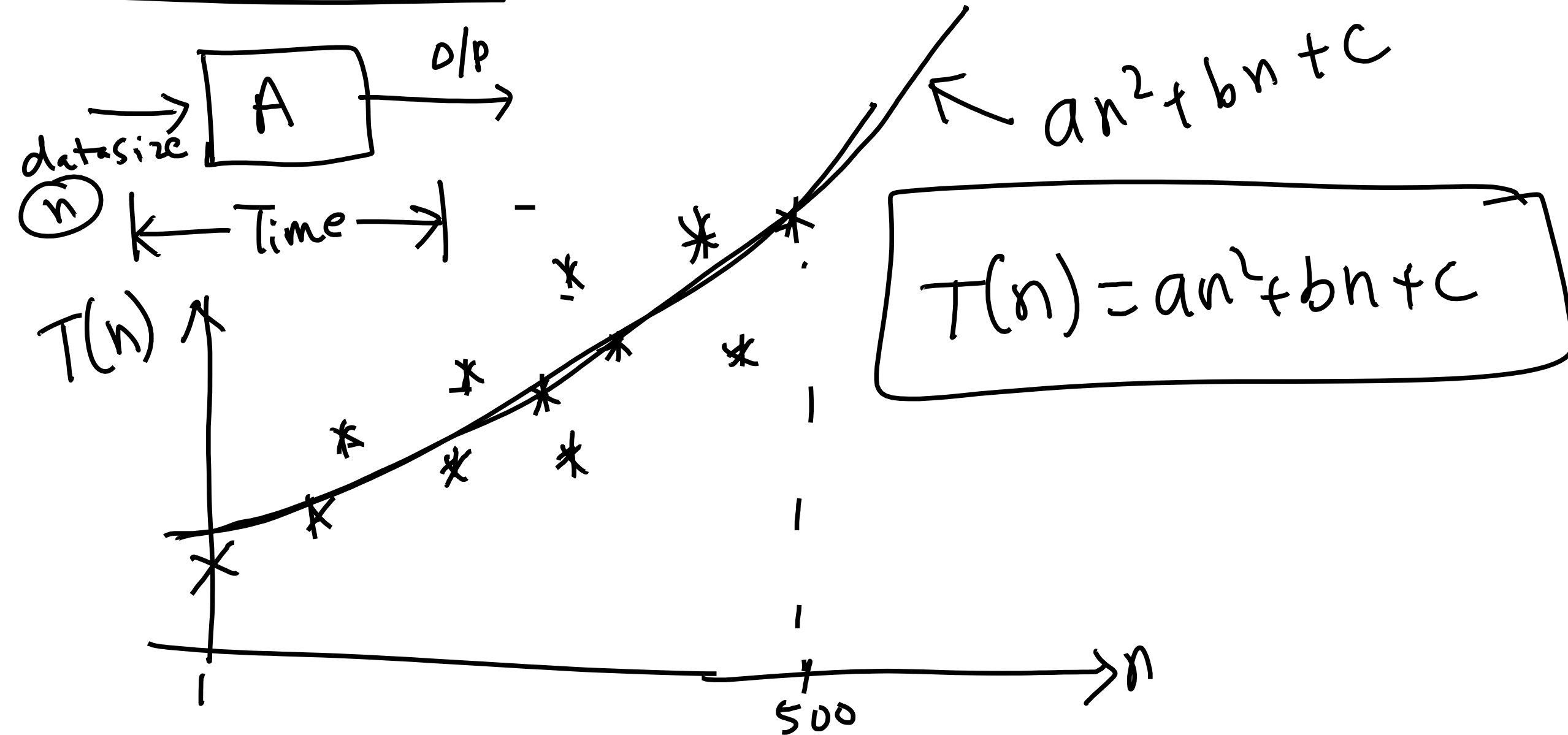
↓ ↓
row col

$\begin{bmatrix} (0,0) & (0,1) & \dots & (0,9) \\ (1,0) & & & (1,9) \\ \vdots & & & \\ (9,0) & (9,1) & \dots & (9,9) \end{bmatrix}$

array[3][4] = {1, 2, 3, 4, ..., 12};

array $\begin{bmatrix} 1 & 2 & 3 & 4 \\ 5 & 6 & 7 & 8 \\ 9 & 10 & 11 & 12 \end{bmatrix}$

Time Complexity



$$T(n) = an^2 + bn + c$$

n	$\frac{T(n)}{n}$
1	(a, b, c)
5	$(a5^2, b5)$
\vdots	
500	$(500^2, 500)$
\vdots	
1 mil	$1\text{mil}^2, 1\text{mil}$

$\rightarrow n^2$ term dominates

$$n^3 + n^2 + n + k$$

Big $O(\cdot)$

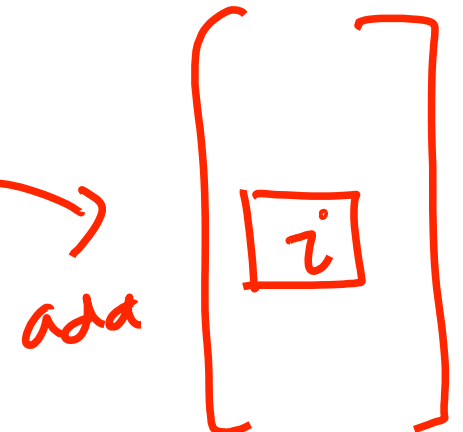
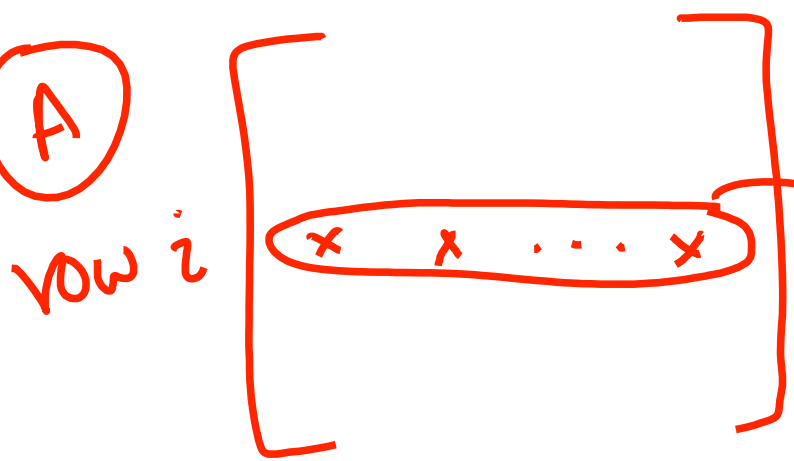
Order of complexity is $\underline{\underline{n^2}}$ $O(n^2)$.

\rightarrow for ($i=0$; $i < \underset{n}{100}$; $i++$) {
 for ($j=0$; $j < \underset{n}{100}$; $j++$) { $O(n^2)$.
 $a[i][j] = a[i][j] + 1;$
 }
 }

\rightarrow }
 $i - 100$

for a fixed i j runs $100 \times$
 & that i runs $100 \times$
 $100 \times 100 = 10000$

(A)



$$b[i] = \sum_{j=0}^{N-1} a[i][j]$$

Time Complexity?
 $O(N^2)$

```

$$\begin{aligned} & \text{for } (i=0; i < N; i++) \{ \\ & \quad \text{sum} = 0; \\ & \quad \text{for } (j=0; j < N; j++) \\ & \quad \quad \text{sum} = a[i][j] + \text{sum}; \\ & \quad b[i] = \text{sum}; \end{aligned}$$

```

$b[i] = b[i] + a[i][j];$

③
$$\begin{bmatrix} A \\ N \times N \end{bmatrix} + \begin{bmatrix} B \\ N \times N \end{bmatrix}$$

$$\begin{bmatrix} \boxed{\text{(i,o)}} \\ \text{[]} \end{bmatrix} + \begin{bmatrix} \boxed{\text{(i,o)}} \\ \text{[]} \end{bmatrix} = \begin{bmatrix} \boxed{\text{(i,o)}} \\ \text{[]} \end{bmatrix}$$

$$a[i][o] + b[i][o] \Rightarrow c[i][o]$$

for (i=0; i<N; i++) { /*row*/ Time Complexity ?

for (j=0; j<N; j++) { /*col*/ $O(N^2)$.

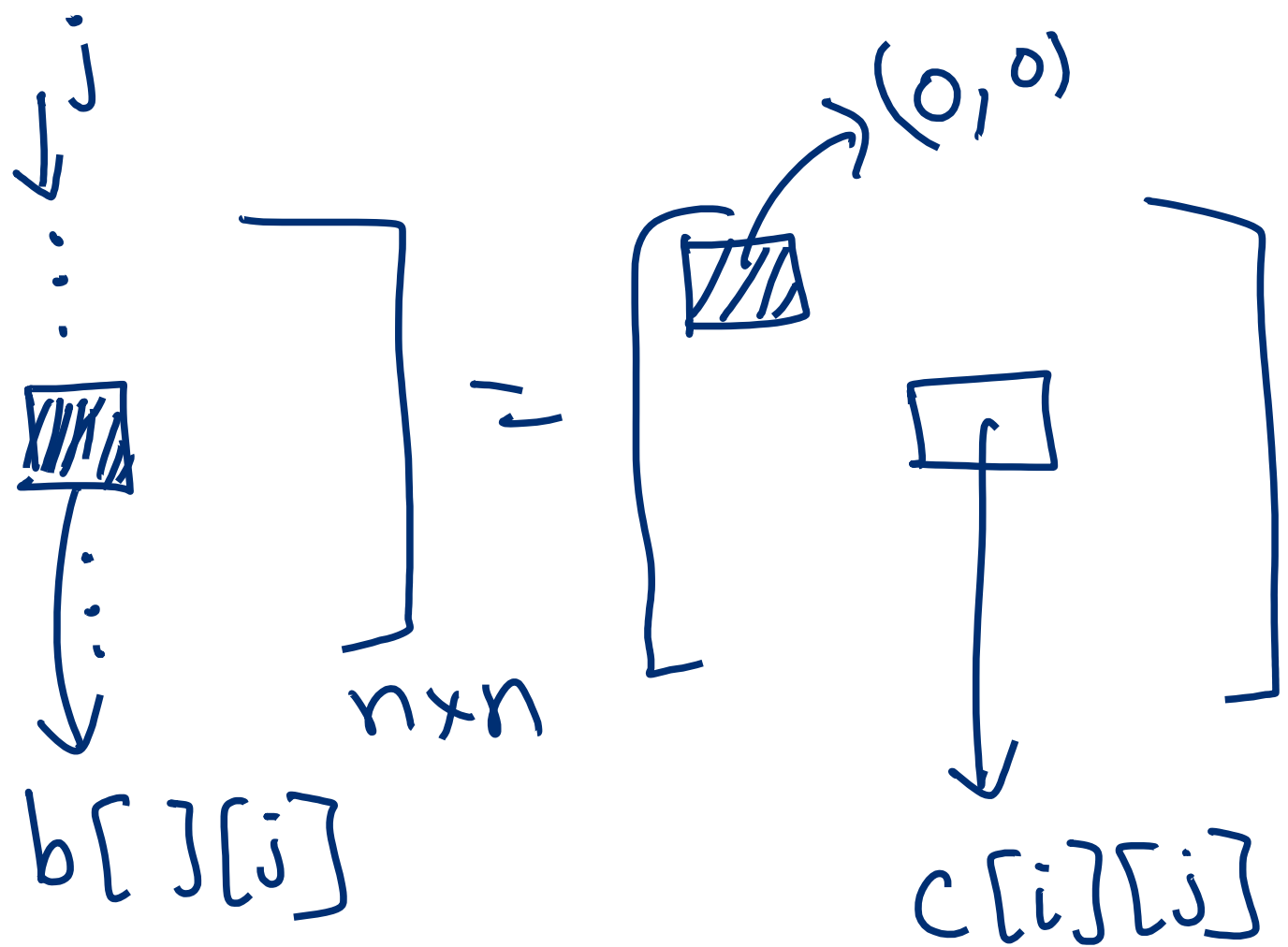
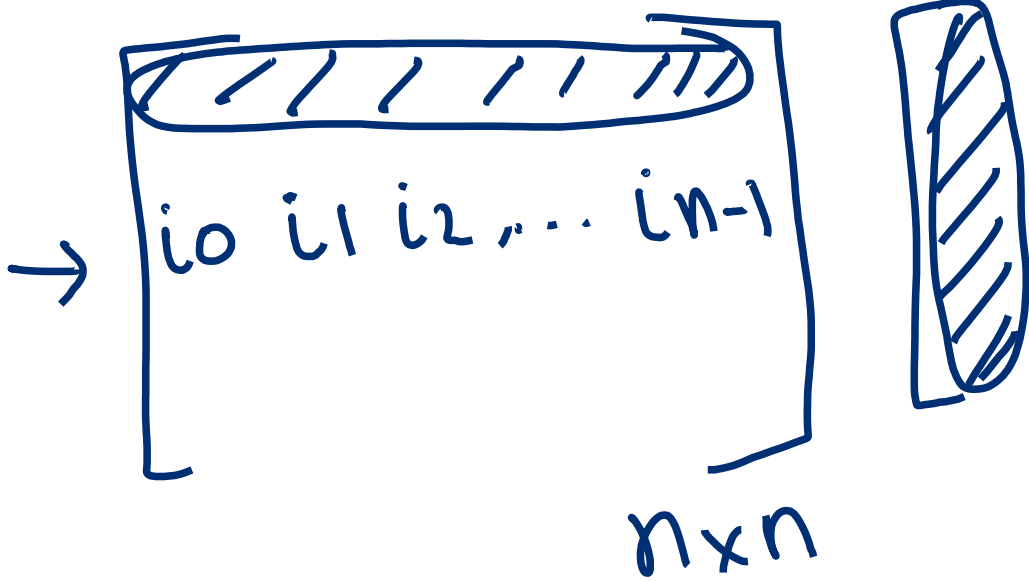
c[i][j] = a[i][i] + b[i][j];

}

int a[20][20], b[20][20],
c[20][20];

(C)

mat. mult-



$$a_{i0} b_{0j} + a_{i1} b_{1j}$$

$$+ a_{i2} \cdot b_{2j} + \dots$$

$$+ a_{ik} \cdot b_{kj} + \dots + a_{i,n-1} \cdot b_{n-1,j} = C_{ij}$$

$$\begin{bmatrix} a_{i0} \\ \vdots \end{bmatrix} \begin{bmatrix} \odot \\ \vdots \end{bmatrix}$$

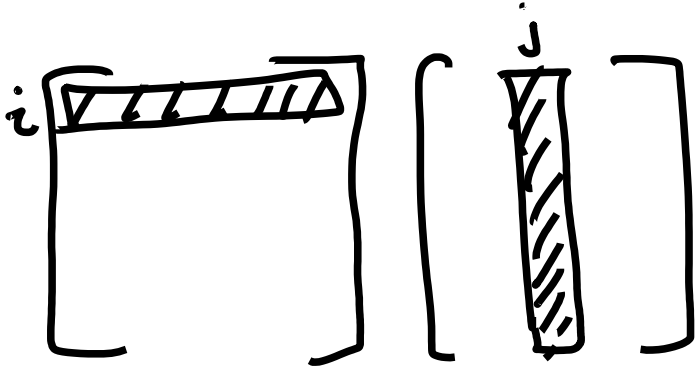
$$C_{ij} = \sum_{k=0}^{n-1} a_{ik} \cdot b_{kj}$$

$$i = 0, 1, \dots, n-1$$

$$j = 0, 1, \dots, n-1$$

for (i=0; i < N; i++) { /* row */

for (j=0; j < N; j++) { /* col */



for (k=0; k < N; k++) {

$$C[i][j] = C[i][j] + a[i][k] * b[k][j];$$

}

}

}

Time complexity = $O(N^3)$

Space Complexity

integer size

(A) $\underline{\underline{4}}n^2 + \underline{\underline{4}}n = \underline{\underline{4}}(n^2 + n) \rightarrow \underline{\underline{O(n^2)}}$

(B) $n^2 + n^2 + n^2 = 3n^2 \rightarrow 4 \times 3n^2 = \underline{\underline{12n^2}}$

(C) $n^2 + n^2 + n^2 = 3n^2 \rightarrow \underline{\underline{12n^2}}$

$$\textcircled{d} \quad \underset{N \times N}{A} \times \underset{N \times N}{A} = \underline{\underline{A^2 = B}}$$

$$\boxed{A^3} ?$$

$$\underbrace{A \times A \times A}_{\downarrow} \quad \downarrow$$

$$\underbrace{\cancel{B} \times A}_{C}$$

Time Complexity = ?.

$$A \times A \rightarrow B$$

$$B \times A \rightarrow C$$

$$\textcircled{N^3}$$

$$\textcircled{N^3}$$

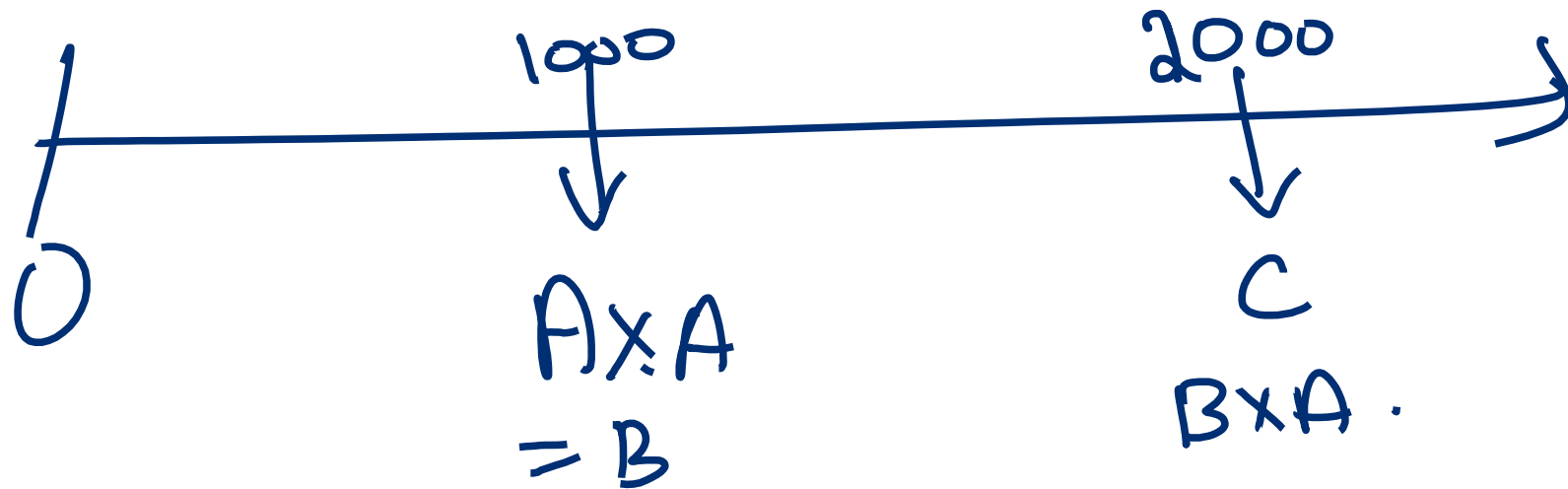
$$2N^3$$

$$N=10 \quad t=1\text{msec}$$

$$\boxed{A^2} = O(N^3) \quad 10 \times 10 \times 10 = 1000 \times 1 = 1000 \text{ Msec}$$

↓
B

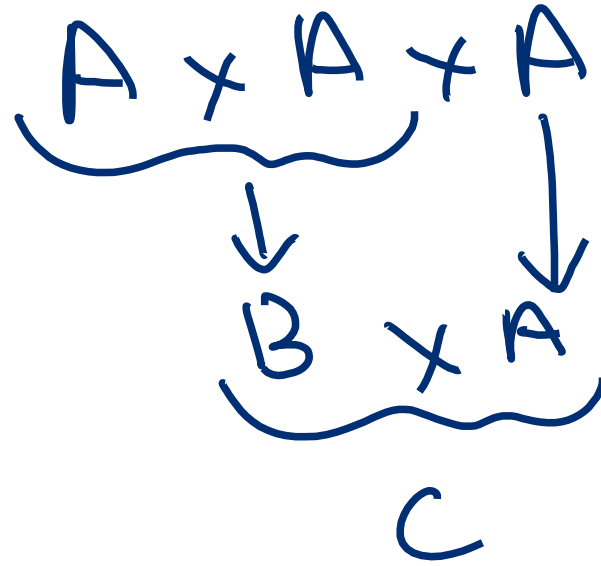
$$B \times A = O(N^3) = 1000 \text{ msec}$$



Space Complexity

A, B, C

$$\begin{array}{ccc} \downarrow & \downarrow & \downarrow \\ n^2 & n^2 & n^2 \end{array} = 3n^2$$



int → $4 \times 3n^2 = 12n^2$ bytes

When the algo terminates mem. used = $2n^2$
= $8n^2$ bytes

```

for (i = 0 to N 10) {
    for (j = 0 to i) {
        x = i + j;
    }
}

```

$$1 + 2 + 3 + \dots + N - 1 + N = \frac{N(N+1)}{2}$$

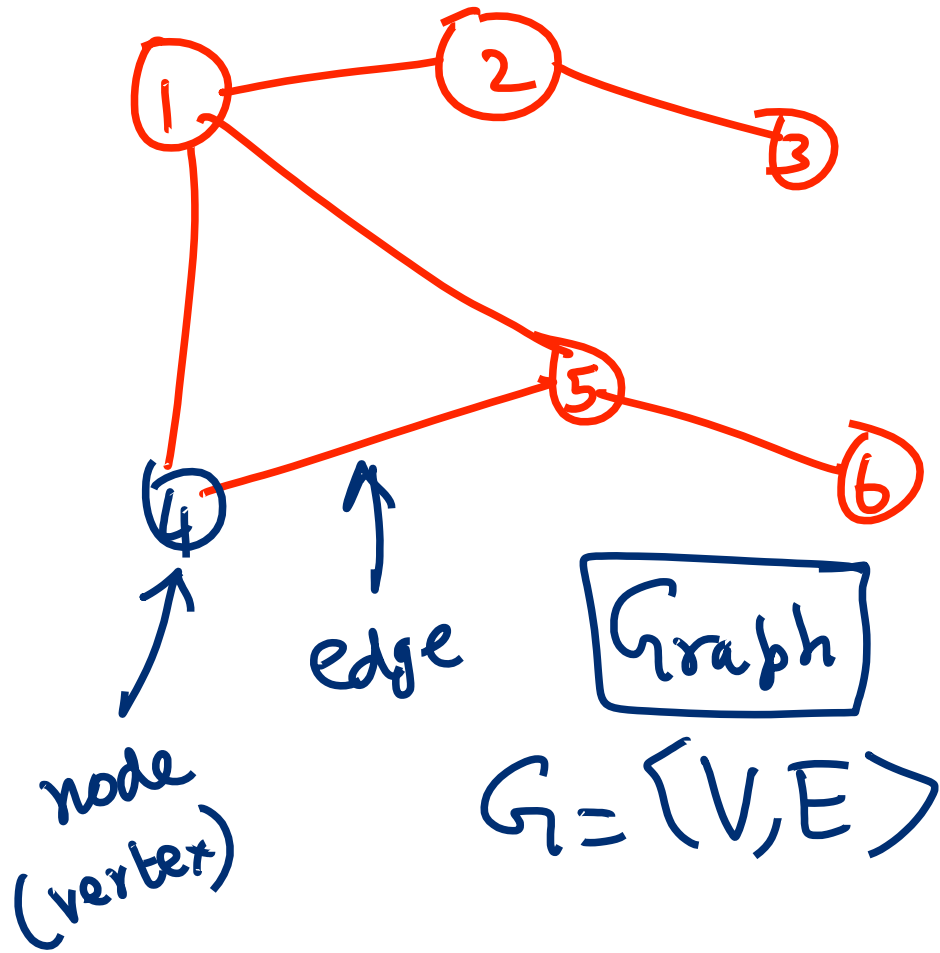
$$\underline{\underline{O(N^2)}}$$

26/oct/2017

Time complexity

i	j (# of times j runs)
0	①
1	②
2	③
⋮	
5	6
⋮	
10	⑪

$$T = (1 + 2 + 3 + \dots + 11)$$

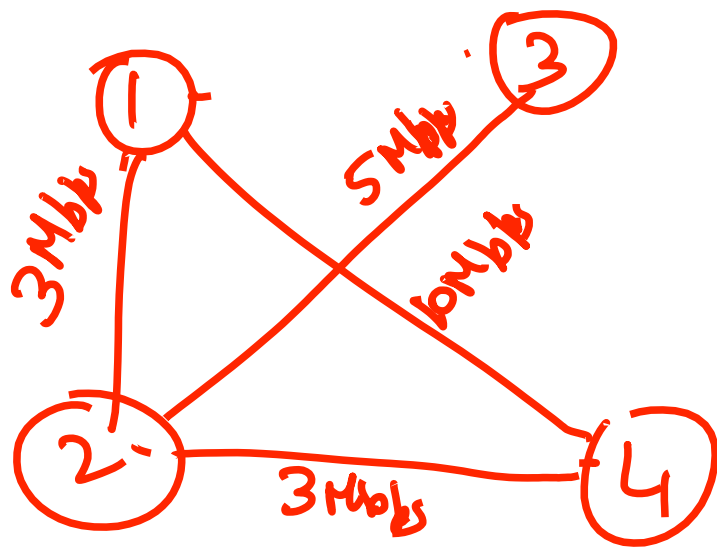


→

	1	2	3	4	5	6
1	0	1	0	1	1	0
2	1	0	1	0	0	0
3	0	1	0	0	0	0
4	1	0	0	0	1	0
5	1	0	0	1	0	1
6	0	0	0	0	1	0

adjacency matrix

1	0	1	0	1
2	1	0	1	1
3	0	1	0	0
4	1	1	0	0

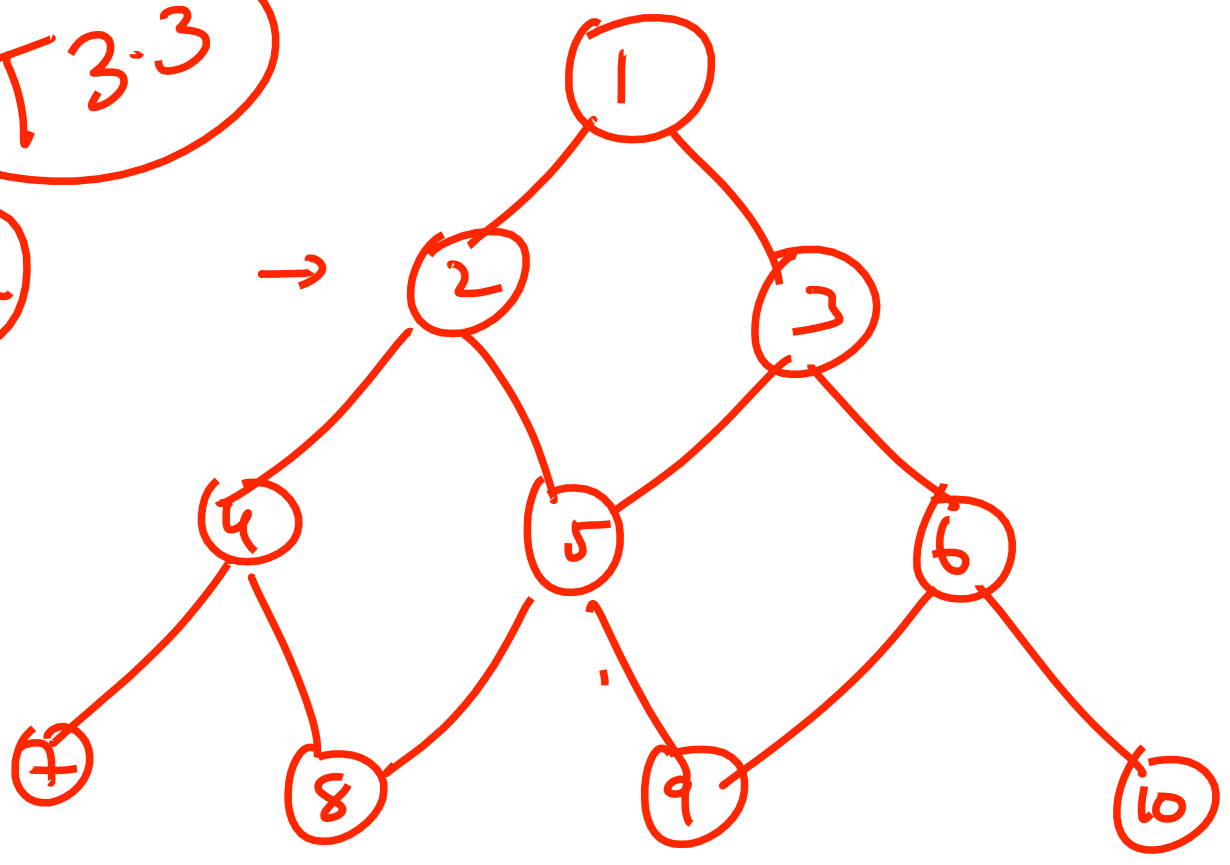


1	0	² 3	0	10
	3	0	5	3
	0	5	0	0
	10	3	0	0

270

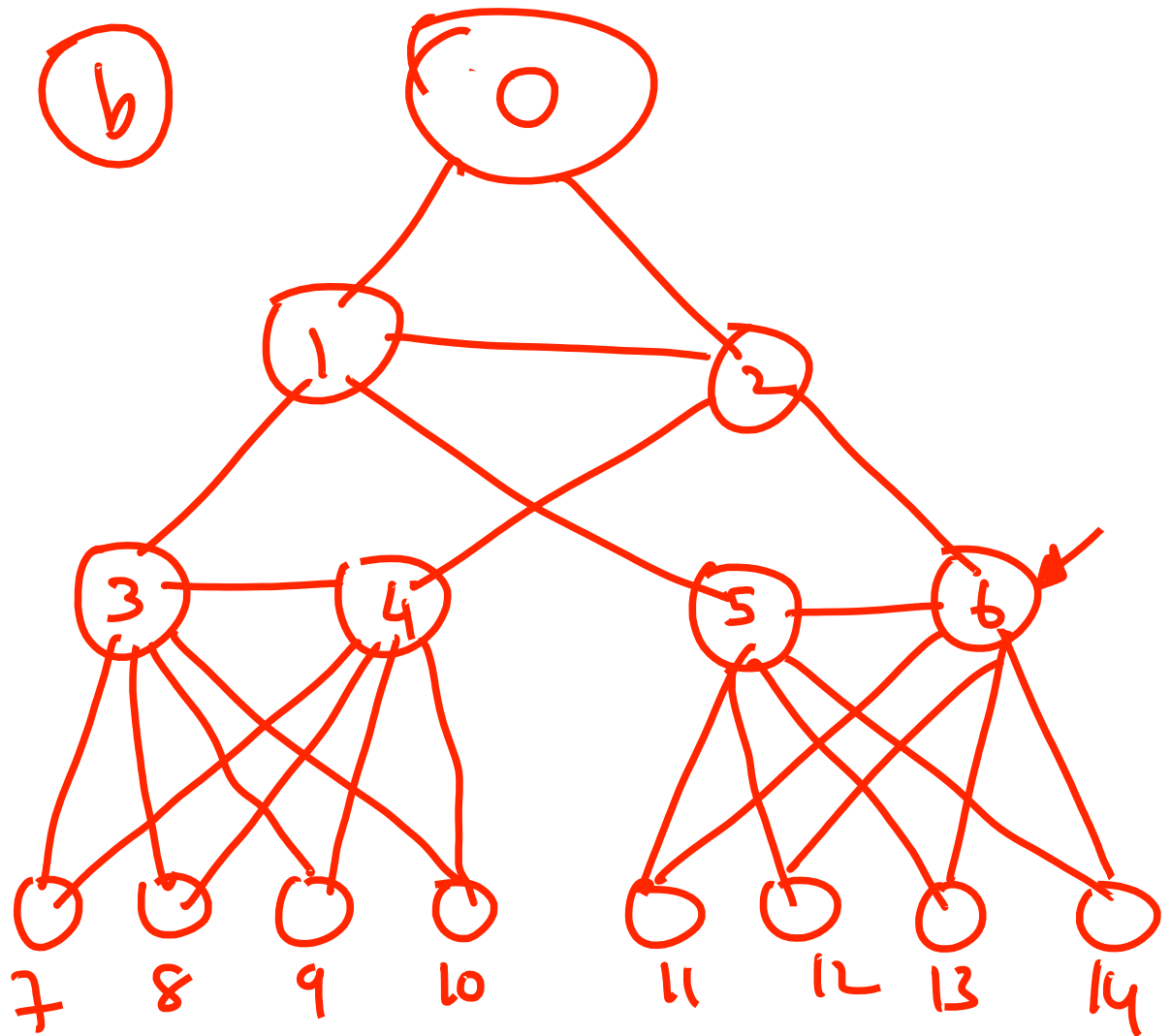
$T_{3,3}$

(a)



	1	2	3	4	5	6	7
1	0	1	1	0	0
2	1	0	0	1	1	0	...
3	1	0	0	0	1	1	0
4	0	1	0	0			1
...							
...							
...							

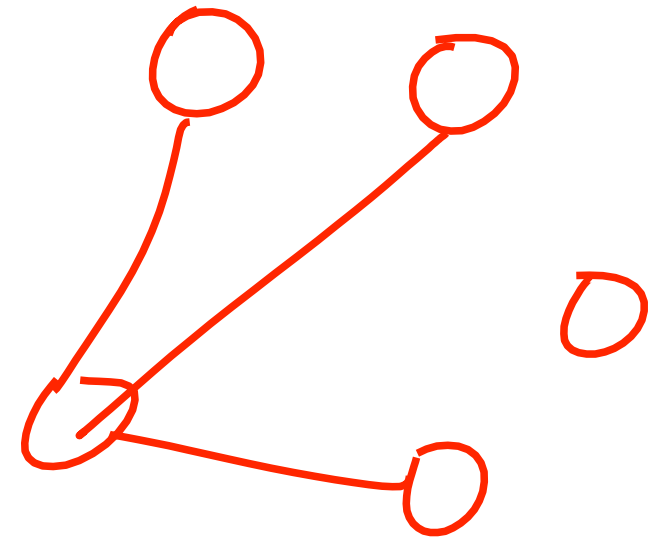
b



(3,4)

	1	2	3	4	5
1	0	(3)	0	2	0
2	(3)	0	0	(2)	(2)
3	0	0	0	2	0
4	2	(2)	2	0	0
5	0	(2)	0	0	0

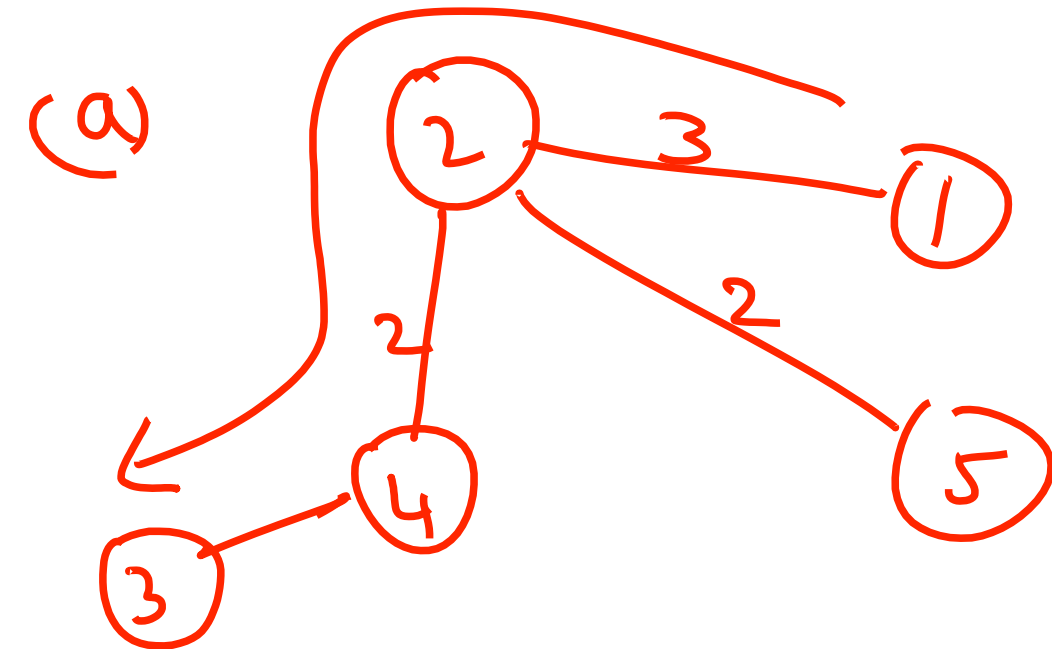
(b) ① → 2, 4
 ② → 1, 4, 5
 ⋮



(c).

(d) degree of a node

② — 3 links incident on node 2



deg of node :

①	3
2	5 ←
3	6 ←
4	1
6	5
7	3

diameter of a graph

maximum delay in that net/w.

Worst case delay in the network.

URoP