

1. Truth table for A, B, C:

A	B	C	$!(A + !B) \times C$	$!( (A \times B) + (C \times B) )$	Output
0	0	0	0	1	1
0	0	1	0	1	1
0	1	0	0	1	1
0	1	1	1	0	1
1	0	0	0	1	1
1	0	1	0	1	1
1	1	0	0	0	0
1	1	1	0	0	0

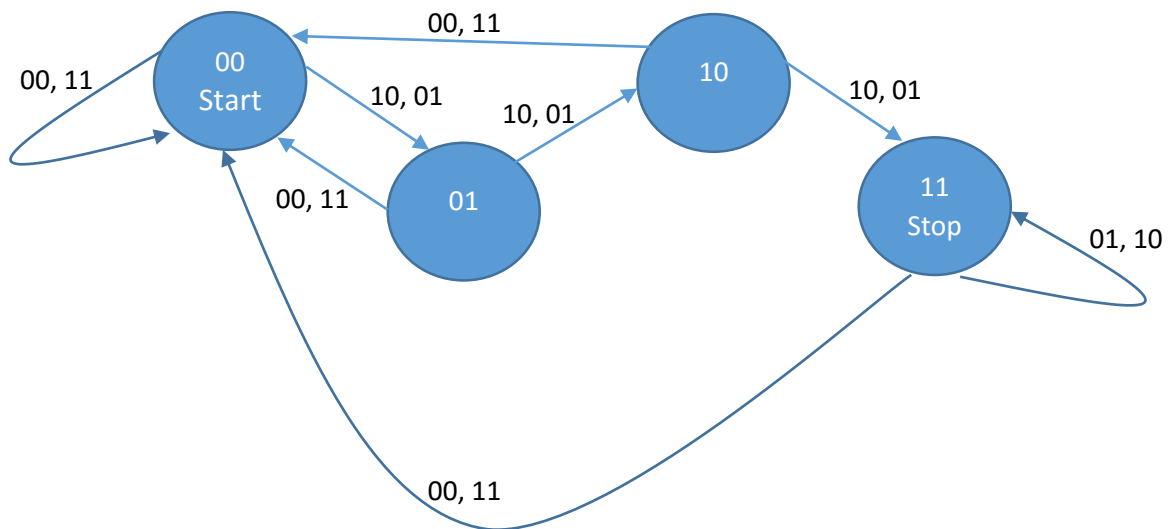
2. Output 1

$$\begin{aligned}
 & (!A \times B \times !C) + (!A \times B \times C) + (A \times !B \times !C) + (A \times !B \times C) + (A \times B \times !C) \\
 &= [ (!A \times B \times !C) + (!A \times B \times C) ] + [ (A \times !B \times !C) + (A \times !B \times C) ] + (A \times B \times !C) \\
 &= (!A \times B) + (A \times !B) + (A \times B \times !C)
 \end{aligned}$$

Output 2

$$\begin{aligned}
 & (!A \times !B \times !C) + (!A \times B \times !C) + (A \times !B \times !C) + (A \times B \times C) \\
 &= [ (!A \times !B \times !C) + (!A \times B \times !C) ] + (A \times !B \times !C) + (A \times B \times C) \\
 &= (!A \times !C) + (A \times !B \times !C) + (A \times B \times C)
 \end{aligned}$$

3. Part a:



**State 00:** start state. **State 01:** last cycle had different input bits. **State 10:** last 2 cycles had different input bits. **State 11:** last 3 cycles had different input bits.

**Output:** 1 if at state 11, 0 otherwise.

Part b:

Truth table

Current state					Next state	
Q1	Q0	Output	Input 1	Input 2	D1	D0
0	0	0	0	0	0	0
0	0	0	0	1	0	1
0	0	0	1	0	0	1
0	0	0	1	1	0	0
0	1	0	0	0	0	0
0	1	0	0	1	1	0
0	1	0	1	0	1	0
0	1	0	1	1	0	0
1	0	0	0	0	0	0
1	0	0	0	1	1	1
1	0	0	1	0	1	1
1	0	0	1	1	0	0
1	1	1	0	0	0	0
1	1	1	0	1	1	1
1	1	1	1	0	1	1
1	1	1	1	1	0	0

Output =  $Q1 \times Q0$

$D1 = (!Q1 \times Q0 \times !In1 \times In2) + (!Q1 \times Q0 \times In1 \times !In2) + (Q1 \times !Q0 \times !In1 \times In2) + (Q1 \times !Q0 \times In1 \times !In2) + (Q1 \times Q0 \times !In1 \times In2) + (Q1 \times Q0 \times In1 \times !In2)$

$D0 = (!Q1 \times !Q0 \times !In1 \times In2) + (!Q1 \times !Q0 \times In1 \times !In2) + (Q1 \times !Q0 \times !In1 \times In2) + (Q1 \times !Q0 \times In1 \times !In2) + (Q1 \times Q0 \times !In1 \times In2) + (Q1 \times Q0 \times In1 \times !In2)$