

# Statistics Knowledge Collected.

## for data science level

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- [source for data used](#)

## . Explore the data analysis

- data type structure / unstructure.
- ordinal is one type of ordered factor categorical data.
- data: continuous, discrete, categorical(binary, ordinal.)
- databases are more detailed in their classification of data types [sql learning](#)
- rectangular data -- data frame
- python uses pandas library `DataFrame()`
- index created by default
- R uses `data.frame`
- R does not support user-specified indexes, python does
- non-rec data: time series data, spatial data for mapping and location analytics, knowledge graph(network optimization and recommendation systems)
- we care more about rec data - pred model.

## . Estimation of location

- mean, weighted mean, median, weighted median, trimmed mean, robust [robust](#) not sensitive to extreme values or outliers.
- data science and business refer to estimates for values to draw actual and theoretical as **METRIC**
- Trimmed mean minus the extreme values' counts when doing mean
- weighted  $x \cdot w / \sum w$
- mean is more sensitive to data, but median is less likely to be affected.
- median is not only a robust estimate, trimmed mean, eg 10% top and bottom in real life. -- compromise for median and mean.
- others more robust
- [good sources slides for calculation estimate](#)
- [king of ds](#)

## . Estimate of variability

- Deviations : difference obs - estimate location. = errors = residuals. (残差)
- variance : sum of squared deviations from mean divided by  $n-1$  = mean squared errors.
- standard deviation: square root of variances -- euclidean norm
- MAD: mean abs of dev
- range
- ranks : metrics based on data values from low to high.
- percentile
- interquartile range. = IQR
- $MAD = \frac{\sum |x - \bar{x}|}{n}$
- $var = s^2 = \frac{\sum (x - \bar{x})^2}{n-1}$
- **degree of freedom** usually don't care, cuz  $n$  is large. (cue variable why  $n-1$ ) \_\_\_\_\_ it is on premise that you want make estimate of pop based on samp.
- $n$  --- biased var. (underestimate the var)
- $n - 1$  standard non biased estimate
- In fact: consider constraints in computing estimates,  $n-1$  === one constraint. [choosing  $K$ ]
- **The above are not robust**
- $STD > MAD > MEDIAN AD$
- 后俩基于 constraint scale of factor , 前者基于 norm dist

## . Exploring the data dist.

- boxplot, freq.table, hist, density,

## . Exploring binary and cate. data.

- mode, expected, bar charts, pie
- bar chart similar to hist. -- but x-axis not ordered.
- *expected value = a form of weighted mean in which the weights are prob.*
- cate data usually summarised in proportion
- distinct things, levels of fa, binned num.

## . Correlation

- modelling
- predict and target

- coefficient correlation -- numerical 1 -1
- correlation matrix
- $cc = 0$  means no association
- contingency tables, hexagonal binning, contour plots, violin
- density
- two categorical table

## . data and sampling dist.

-sample, population, n, rs, strata, sample bias.

- data quality matters here
- bias -- statistical bias to measurements of sampling errors systemic and process when collected
- observable or not
- Random selection -- avoid bias
- in stratified sampling
- size matter
- central limit theorem
- standard error =  $se = s / \sqrt{n}$
- standard deviation measures variability of individual data points
- while standard error measures the variability of the sampling metric.
- the larger the sample size the normally it is
- dist. of sample are normally skewed
- error, standardize by dividing sde. 根号下
- z-score of standardizing an individual point
- errors are normally dist. usually while data might not.
- poisson dist. for per time period

## . t dist. estimate of mean

- degree of freedom
- n sample size
- t is similar to z but thicker tails for sampling.
- t used for sample mean, regression parameters and more.

## . binomial dist.

- trial, success,

- $n$  变大的时候 可以被 normal approximate
- $n * p(1-p)$

## . Poisson dist.

- Many processes produce events randomly at a given overall rate.
- $\lambda$ - rate which occurs events
- position frequency distr. given time unit
- exponential dis. **the time or distance from one even to another**
- weibull dist. version of expo rate is allowed to shift over time.

## . statistical experiments and siinificace testing.

- pm uses alot
- interfece
- limited sample to larger population
- formualte the hyphthesis ---- design experince ---- collet data ---- inference and conclusion
- typical hp : a treatment is better than control

## . ab testing

- treatment
- traetment group
- control group
- randamization
- susbjects
- test statistics
- eg: seed germination for product, profit, produces more clickm, web ads conversisions
- bliing study / double blind

## . hypo

- why hupothesis ? 1. mis understadnd a random evens as a pattern thing. 2. failure to anticipate extreme
- mean difference is more extreme or not.

## . resampling

- resampling helps with ml algorithm.
- **\*\*two types: bootstrap(with replacement) / permutation(random test) \*\***

**- permutation : combine results from different groups; shuffle and randomly draw with NO replacement of same size as group A; repeat that with size equals to group B *with remaining data*; C,D,E, if any; calculate the stats and constitutes one permutation iteration; repeat R times to form a permutation dist. if the observed difference lies outside most of the permutation distribution, then we conclude that chance is not responsible.**

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## **. statsig and p-value**

- P-value: the prob. of obtaining results as unusual or extreme
- alpha unusual
- type 1 reject when  $H_0$  true
- type 2 accept when  $H_0$  falls
- **pvalue** is the prob. that the result is due to chance.
- It is the prob. given a chance model, results as extreme as the observed results could occur.
- $pvalue < \alpha$  leads to reject null hypothesis.
- t test
- overfitting - fitting to the noise

## **. anova**

- pairwise
- F statistics
- SS sum of square
- based on the ratio of variance by group means
- $ms(treatment) / me(error)$  gives f statistics
- For illustration, suppose that you wish to test the hypothesis that  $p$  coefficients are zero, and thus these variables can be omitted from the model, and you also have  $k$  coefficients in

## . CHi-squ !!!

- CHIsquare stat == measure of extend to whcih some observed data departs from expectation
- df
- pearson residual =  $\text{obs} - \text{exp} / \text{root of exp}$
- $(r-1)(c-1)$
- shuttle resampling test
- chi-squire!!! more as a filter to determine effectr or feature is wortht of further consideration than as a formal test of signiicance.
- **feature selection** in machine larning
- chi which assumption of independence.

## . power and sample

- effect size
- power
- sigifican level

## . reg.

- fitted values -- estimate y head
- resi -- difference obs - fitted.=== errors
- $y_i = b_0 + b_1x + e_i$
- $y_i\text{head} = b_0\text{head} + b_1\text{heardx}$
- rss residual sum
- regr ---- predict / explain
- r-suqare == the proportion of variance explained by model
- $t = b / \text{se error of coefficient}$
- higher t, lowewr pvalue means significant
- minimize AIC BIC from bayesian
- weighted reg 1 inverser-variance weight
- RMSE / Rsuqare 最重要俩指标
- stanadarlized error of coefficent can be used to measure the reliabitlity of the variable contributin to a model.
- factor used: dummy 0-1
- factors needed to be converted to numeric in use.
- confounding variable

- cooked distance -- lever+ residual size

## . classi

- naive bayesian 查查
- bay for numdeic needs :1 bind and conver to cate, 2 prob. model  $p(x|y=i)$
- discriminat analysi : LDA taelss measure of importanace and 好计算
- lda believes the covariance matrix same for groups e covariance matrix:
- **LOGIST TIC** 查查

## . evalue model

- accuracy
- confusion matrix 看图
- sebsitivity = percent of 1s cirreckt classfie
- bagging resample records
- rf bag+ resample variables
- boosting requires more care and tune.: give weights to the record with large residual
- regularization : add penalty term besed on number of parameters in model to avoid overffting

## ◦ Unsupervised learning

- principal component: lienar combination of the predictor vaeibels 查查
- <http://support.minitab.com/en-us/minitab/17/topic-library/modeling-statistics/multivariate/principal-components-and-factor-analysis/what-is-pca/>
- loading : weights that trasnform the predictors into the compoonents

## ◦ (Redirected from Ridge regression)

- lasso set coe === zero , while ridge not
- least absolute shrinkage and selection operator

```
# bayesian :
- http://uc-r.github.io/naive_bayes
his is primarily because what is usually needed is not a propensity (exact posterior probability) for each record that is accurate in absolute terms but just a reasonably
```

accurate rank ordering of propensities.

#z Gini index: Mainly used with tree-based methods and commonly referred to as a measure of purity where a small value indicates that a node contains predominantly observations from a single class. Objective: minimize

# A simple way to detect collinearity is to look at the correlation matrix of the predictors. An element of this matrix that is large in absolute value indicates a pair of high

# Leave-one-out cross-validation

- Filter methods are generally used as a preprocessing step. The selection of features is independent of any machine learning algorithms. Instead, features are selected on the basis of their scores in various statistical tests for their correlation with the outcome variable. The correlation is a subjective term here. For basic guidance, you can refer to the following table for defining correlation coefficients.

fs1

Pearson's Correlation: It is used as a measure for quantifying linear dependence between two continuous variables X and Y. Its value varies from -1 to +1. Pearson's correlation is given as:

fs2

LDA: Linear discriminant analysis is used to find a linear combination of features that characterizes or separates two or more classes (or levels) of a categorical variable.

ANOVA: ANOVA stands for Analysis of variance. It is similar to LDA except for the fact that it is operated using one or more categorical independent features and one continuous dependent feature. It provides a statistical test of whether the means of several groups are equal or not.

Chi-Square: It is a statistical test applied to the groups of categorical features to evaluate the likelihood of correlation or association between them using their frequency distribution.

看看 如何 logistic odds之类的  
sensitivity and specificity  
knn



```
# model transfer
- https://newonlinecourses.science.psu.edu/stat501/node/320/
```

```
# Variance Inflation Factors (VIF)
```

```
#chi
```

A chi-squared test, also written as  $\chi^2$  test, is any statistical hypothesis test where the sampling distribution of the test statistic is a chi-squared distribution when the null hypothesis is true. Without other qualification, 'chi-squared test' often is used as short for Pearson's chi-squared test. The chi-squared test is used to determine whether there is a significant difference between the expected frequencies and the observed frequencies in one or more categories.

```
# PCA和LDA (linear discriminant analysis) 都可以用来减少feature。PCA保留variation最大的feature, LDA保留对于结果最容易进行分类的feature。
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My name is JIASHU MIAO and im currently a third year student at ucla double majors in math of computation and staistics. These two majors are a actually a great overlap which contains knowledge of mathematics, statistics and programming and scripting languages. The combined study occupies necessary basics for data science and I also get many past experince working as an intern or lab assistant in the fields of data analysis in different indusstris like healthcare, biomedicine, educatoinal it company and financial service. I like data science and never feel that involves so many topics.

RAM

```
# database optimization
- probr index
- rettrove relevant data
- getting rid of corredlate subs
- avoid coding loops
```