

If the cookie had candy, then very few bites would have no candy.

$$\Pr(\text{no candy bite} \mid \text{candy cookie}) = \frac{1}{3}$$

The probability of a no-candy bite, given a candy cookie, is 1/3.



If the cookie had no candy, then every bite would have no candy.

$$\Pr(\text{no candy bite} \mid \text{no candy cookie}) = 1$$

The probability of a no-candy bite, given a no-candy cookie, is 1.

# CS 1671 / CS 2071 / ISSP 2071

## Human Language Technologies

Session 2: Probability and linear algebra review

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Michael Miller Yoder

January 14, 2026

# About Zhuochun Li (TA)

- 3rd year Information Science PhD student
- Website: <https://zhuochunli.github.io/>
- Research interests:
  - NLP and Machine Learning
    - LLMs Reasoning
    - Knowledge Distillation
- Office Hours:
  - Wednesdays 12-1pm, IS 707
  - Email: zhl163@pitt.edu



# Overview: Linear algebra and probability review

1. Course logistics and Top Hat
2. JupyterHub setup and Jupyter notebook intro
3. Probability review
4. Linear algebra review

# Course logistics

- No class next Mon for MLK Day
- Next class is Wed Jan 21 on Python for data science

# Top Hat

We'll be using Top Hat to:

- Take attendance (occasionally)
- Do ungraded comprehension checks in class
- Text chat questions (new, will see if it works)
  - “In-class questions and comments” discussion

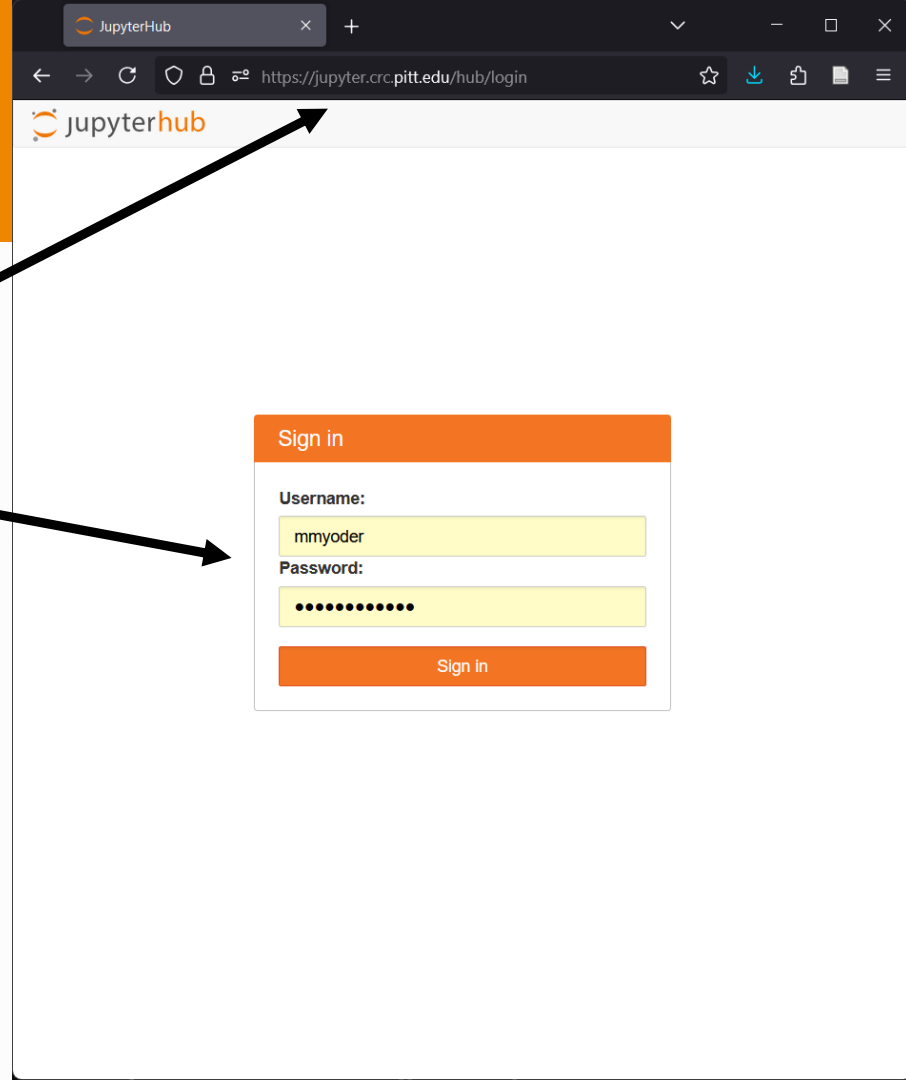
# JupyterHub setup

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# Logging in to your CRCSD JupyterHub account

1. Go to `jupyter.crc.pitt.edu` in a web browser
2. Log in with your Pitt credentials (lowercase)

Note that if you are off-campus, you have to log in to the Pitt VPN first through the GlobalProtect app. Instructions: <https://services.pitt.edu/TDClient/33/Portal/KB/ArticleDet?ID=3426>





# Starting a Jupyter Notebook on the CRCRD JupyterHub

1. Partition: **TEACH** – 6 CPUs – 45 GB  
*We will use the GPU options later on in the course*
2. Under **Select Virtual Environment**, select **Provide custom path**
3. **Custom Environment Path:**  
`/ix1/cs1671-2026s/class_env`
4. Click **Start**
5. Wait for the server to start up

JupyterHub

jupyter.crc.pitt.edu/hub/spawn

jupyterhub Home Token mmyoder Logout

## Server Options

### JupyterHub Session Configuration

**Select Partition:**

TEACH - 6 CPUs - 45GB

**Select Virtual Environment:**

Provide custom path

**Custom Environment Path:**

/ix1/cs1671-2026s/class\_env

**Select Modules to Load:**

Amber 2024  
Cuda 12.3  
OpenJDK 21.0.2

Hold Ctrl/Cmd to select multiple modules

**Account:** your class account

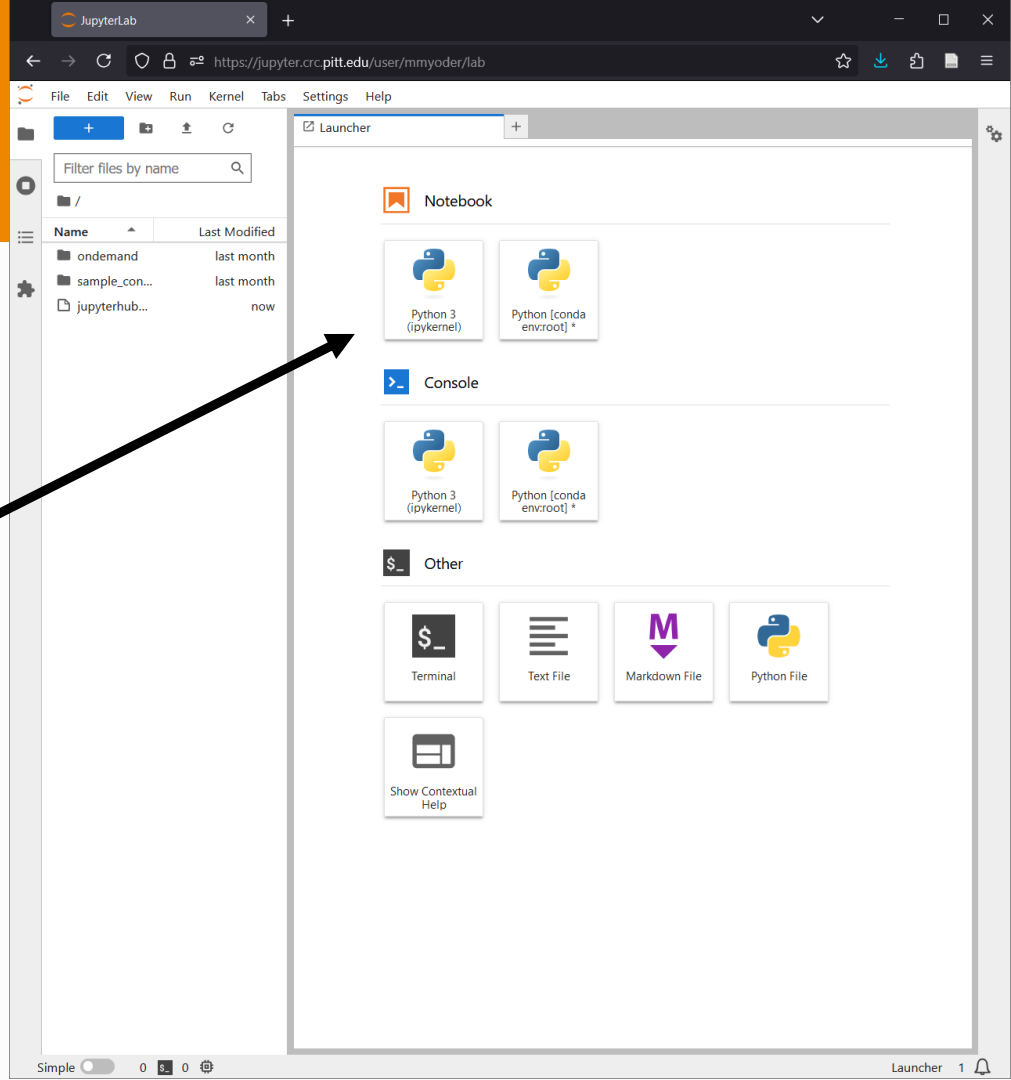
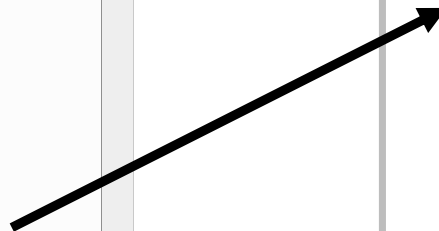
Start

# Welcome to your JupyterLab

Files are here



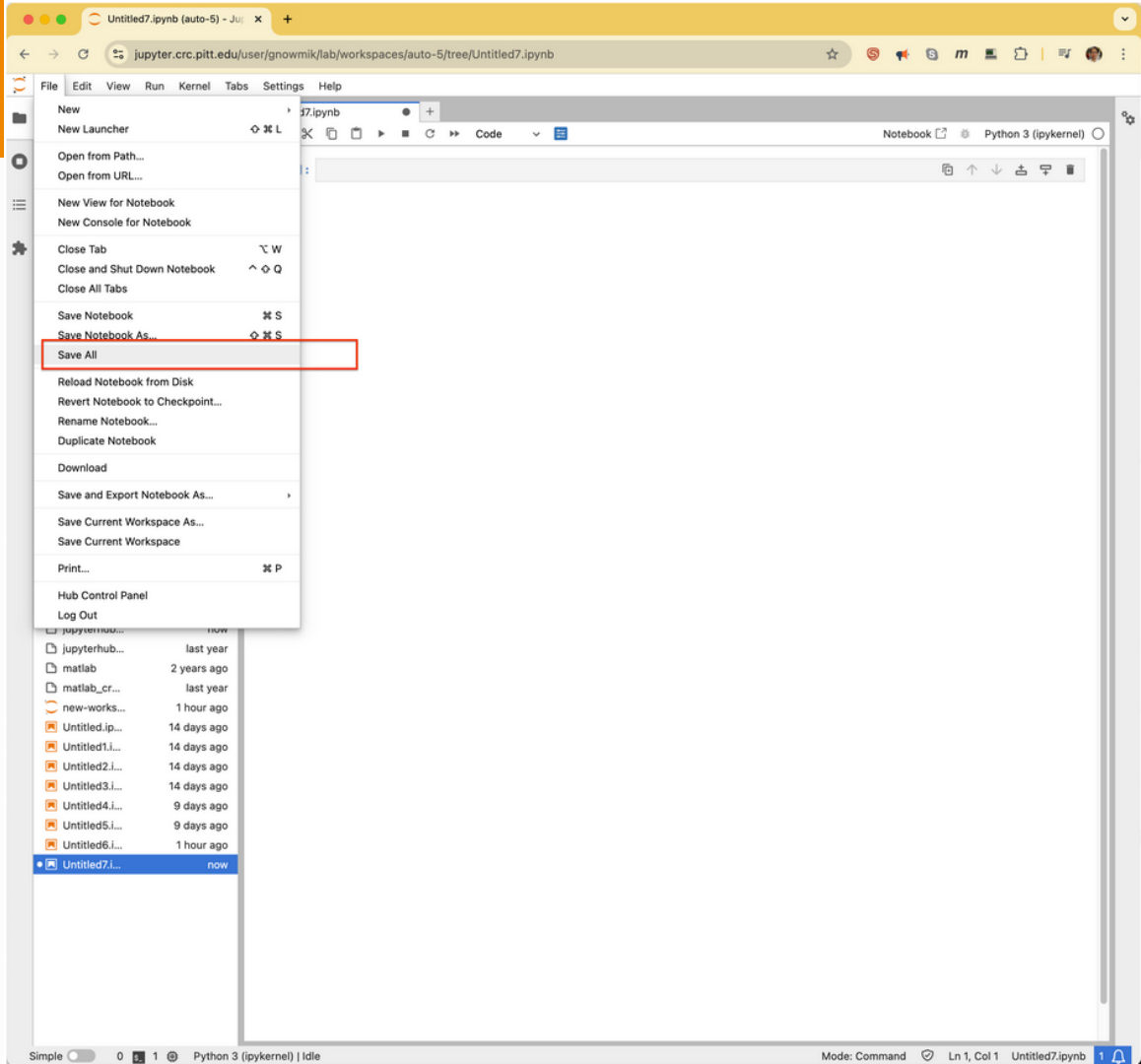
You can launch a new Jupyter Notebook by clicking Python 3 (ipykernel) under Notebook



# Jupyter Notebook basics

- Each block is called a “cell”
  - Has input and possibly output
  - Input can be Python code, Markdown or shell commands (after !)
- Modes
  - Command mode
    - Move, select, manipulate cells
    - Get into command mode by clicking anywhere outside of a cell
  - Edit mode
    - Blinky cursor within a cell, which is highlighted with a blue border
    - Edit content of a particular cell
- Running cells
  - Click “Run” button or do Ctrl+Enter (on Windows or Linux, Cmd+Enter on Mac) to run code or render Markdown
  - Any result will be shown in the output of the cell

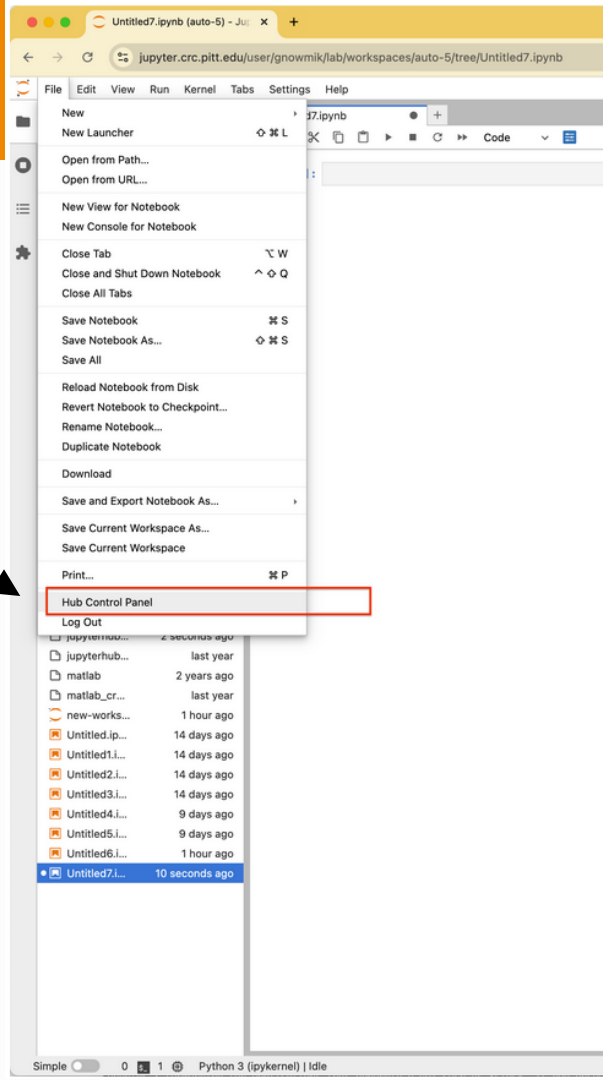
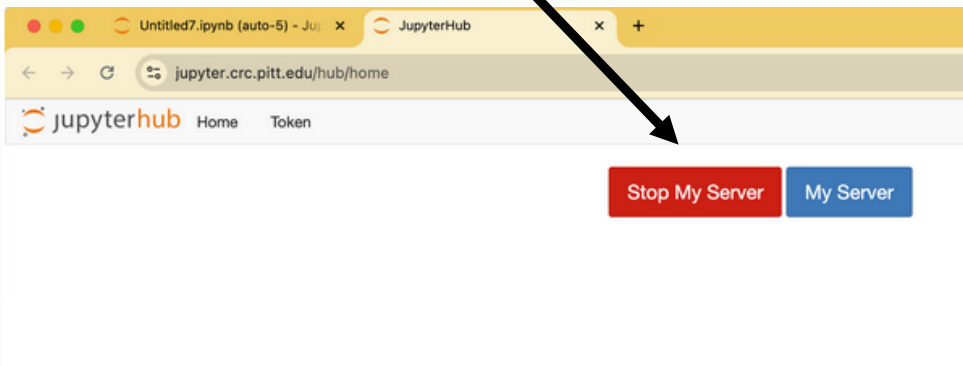
# Saving your work



# Ending your session

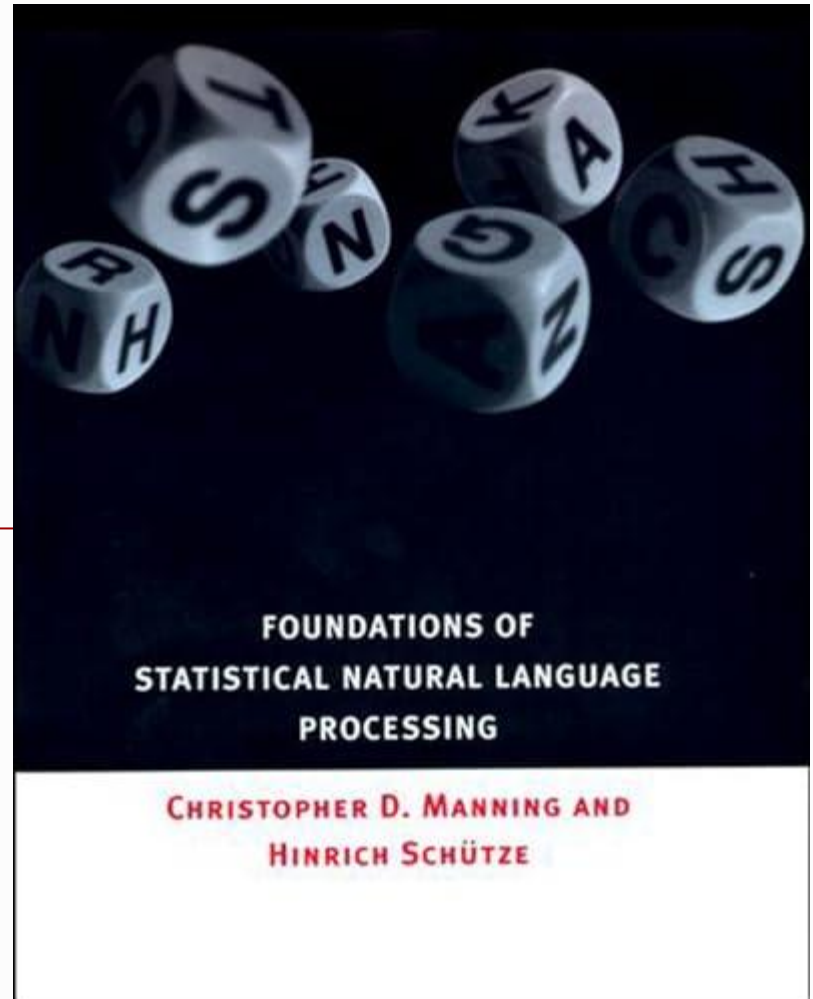
Be sure to save your work before ending the session

1. Select **File > Hub Control Panel**
2. Click **Stop My Server**



# Probability review

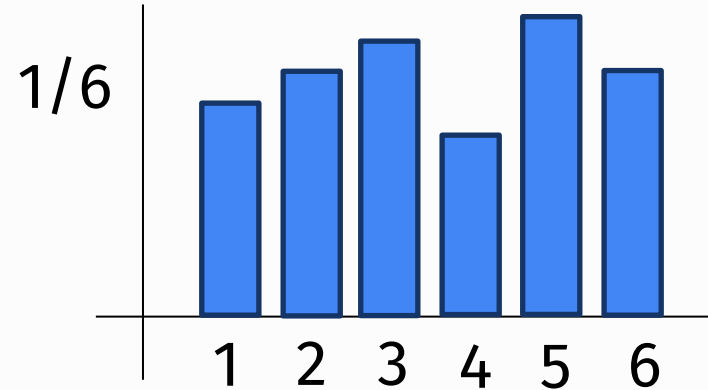
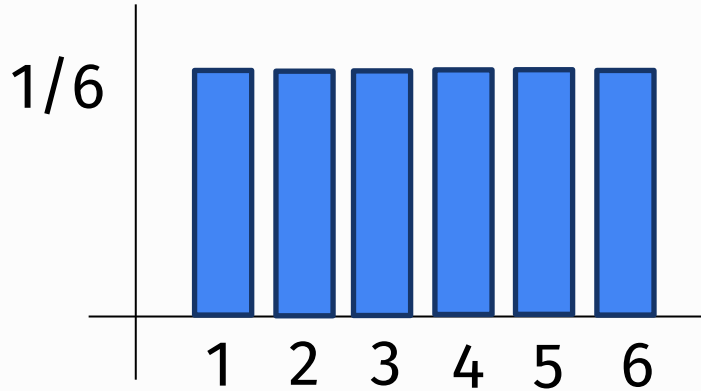
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# Probability

- Probability of an event  $a$  occurring
- $P(a)$ 
  - For example,  $a$  could be a die showing a 2 out of  $\{1, 2, 3, 4, 5, 6\}$
- Estimate  $P(a)$  as  $\frac{\text{count}(a)}{\text{count}(\text{all events})}$ 
  - Relative frequency or maximum likelihood estimate (MLE)

# Probability distributions





# Random variables

- **Random variable:** a mapping from a domain of possible outcomes in a sample space to a range of measurable space, such as counts
  - Typically the “result of an experiment”
  - For example, flipping a coin multiple times (possible outcomes {H, T}) and recording the result as 0 for tails and 1 for heads
- Distribution of a random variable  $X$ 
  - $P(X)$  is a probability distribution over all possible values in the sample space. Probability mass function
  - $P(X = x)$  is the probability that the random variable  $X$  has the value  $x$
  - $P(X = \text{heads})$ , where  $X$  is the random variable of a coin flip

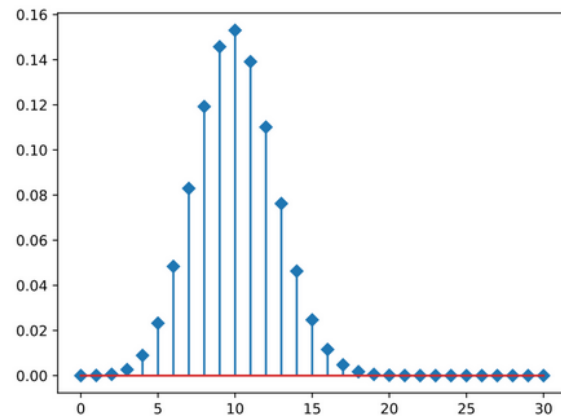


Figure 7.1:  $P(k \text{ heads})$  in 30 tosses, success prob  $1/3$ .

# Joint probability

- Probability of 2 events both occurring

$$P(A \cap B)$$

$$P(A, B)$$

- When rolling 2 dice, what's the probability of getting two 5s?

Let  $D_1$  be dice 1,  $D_2$  be dice 2. These events are independent, so:

$$P(D_1 = 5, D_2 = 5) = P(D_1 = 5) \cdot P(D_2 = 5)$$

$$\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} \text{ since there are 36 different possible combinations}$$

# Conditional probability

- Probability distributions sometimes change if you know another event has occurred or not occurred
- **Conditional** probability of an event  $a$  occurring **given that another event,  $b$ , has already occurred**
  - $P(a|b)$
- Assume
  - $X$  is the outcome of rolling a die once
  - $F$  is the event  $X = 6$
  - $E$  is the event  $X > 4$
- Die is rolled and we are told that  $E$  has occurred
- What is  $P(F|E)$ , that is,  $P(X=6|X>4)$ ?

# Conditional probability

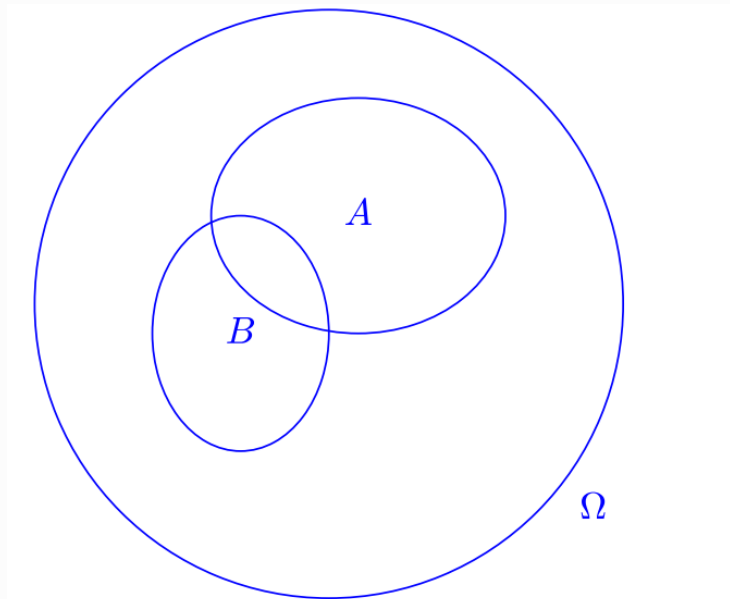


Figure 4.1: Events on the dart board

- Assume a very bad dart thrower (maybe Michael)

$$\mathbf{P}(A) = \frac{\mathbf{area}(A)}{\mathbf{area}(\Omega)}$$

# Conditional probability

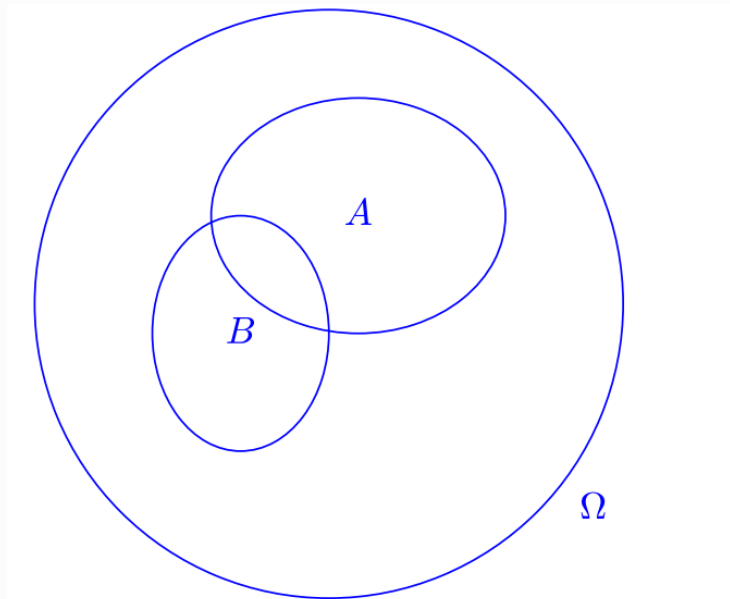


Figure 4.1: Events on the dart board

- You don't see the throw, but somebody tells you that the dart landed in  $B$  (so  $B$  occurred)
- What is the formula for  $P(A|B)$ ?

# Linear algebra review

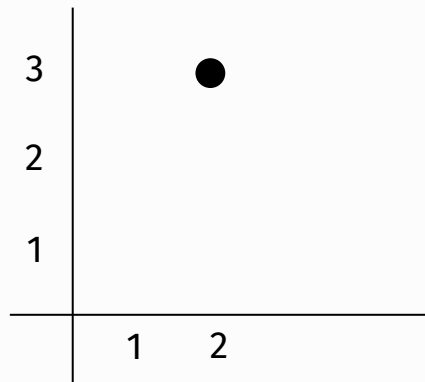
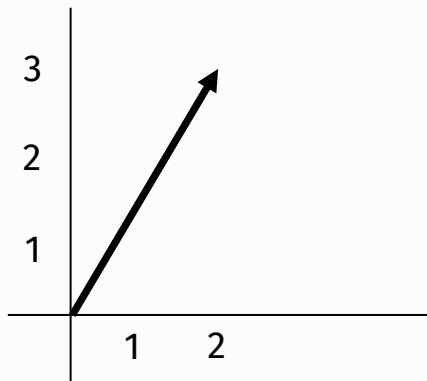
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# Vectors

An array of numbers with  $D$  dimensions

[ 2 3 ]

Can be represented as a point in  $D$ -dimensional space



# Dot product: vector $\cdot$ vector

Sum of the products of each vector dimension

$$\begin{matrix} \mathbf{v} & & \mathbf{w} \\ \begin{matrix} v_1 & v_2 & \cdots & v_N \end{matrix} & \cdot & \begin{matrix} w_1 \\ w_2 \\ \vdots \\ w_N \end{matrix} \end{matrix}$$

$$\mathbf{v} \cdot \mathbf{w} = \sum_{i=1}^N v_i w_i = v_1 w_1 + v_2 w_2 + \cdots + v_N w_N$$



# Matrices

A matrix is an array of numbers

$$\begin{bmatrix} 6 & 4 & 24 \\ 1 & -9 & 8 \end{bmatrix}$$

Two rows, three columns.

## It's Easy to Multiply a Matrix by a Scalar

$$2 \cdot \begin{bmatrix} 5 & 2 \\ 3 & 1 \end{bmatrix} = \begin{bmatrix} 2 \cdot 5 & 2 \cdot 2 \\ 2 \cdot 3 & 2 \cdot 1 \end{bmatrix} = \begin{bmatrix} 10 & 4 \\ 6 & 2 \end{bmatrix}$$

# Dot product: vector $\cdot$ matrix

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \phantom{a} \\ \phantom{a} \\ \phantom{a} \end{bmatrix}$$

# Dot product: matrix · matrix

Let  $a_1$  and  $a_2$  be the row vectors of matrix  $A$  and  $b_1$  and  $b_2$  be the column vectors of a matrix  $B$ . Find  $C = AB$

$$\begin{bmatrix} \boxed{1} & \boxed{7} \\ \boxed{2} & \boxed{4} \end{bmatrix} \cdot \begin{bmatrix} \boxed{3} & \boxed{3} \\ \boxed{5} & \boxed{2} \end{bmatrix} = \begin{bmatrix} \boxed{a_1 \cdot b_1} & \boxed{a_1 \cdot b_2} \\ \boxed{a_2 \cdot b_1} & \boxed{a_2 \cdot b_2} \end{bmatrix} = \begin{bmatrix} \boxed{\phantom{00}} & \boxed{\phantom{00}} \\ \boxed{\phantom{00}} & \boxed{\phantom{00}} \end{bmatrix}$$

$A$  must have the same number of rows as  $B$  has columns.

*Questions?*

No class next Mon for MLK Day.  
Will see you again on Wed.