

DATA STRUCTURES AND ALGORITHMS

SEARCHING

Searching

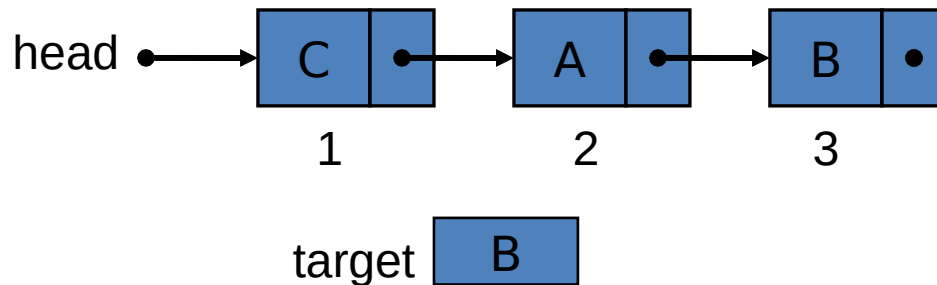
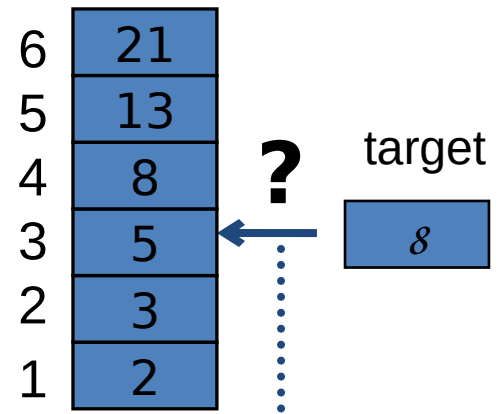
- Computer systems are often used to store large amounts of data from which individual records must be retrieved according to some search criterion.
- Thus the efficient storage of data to facilitate fast searching is an important issue.

Search: Applications

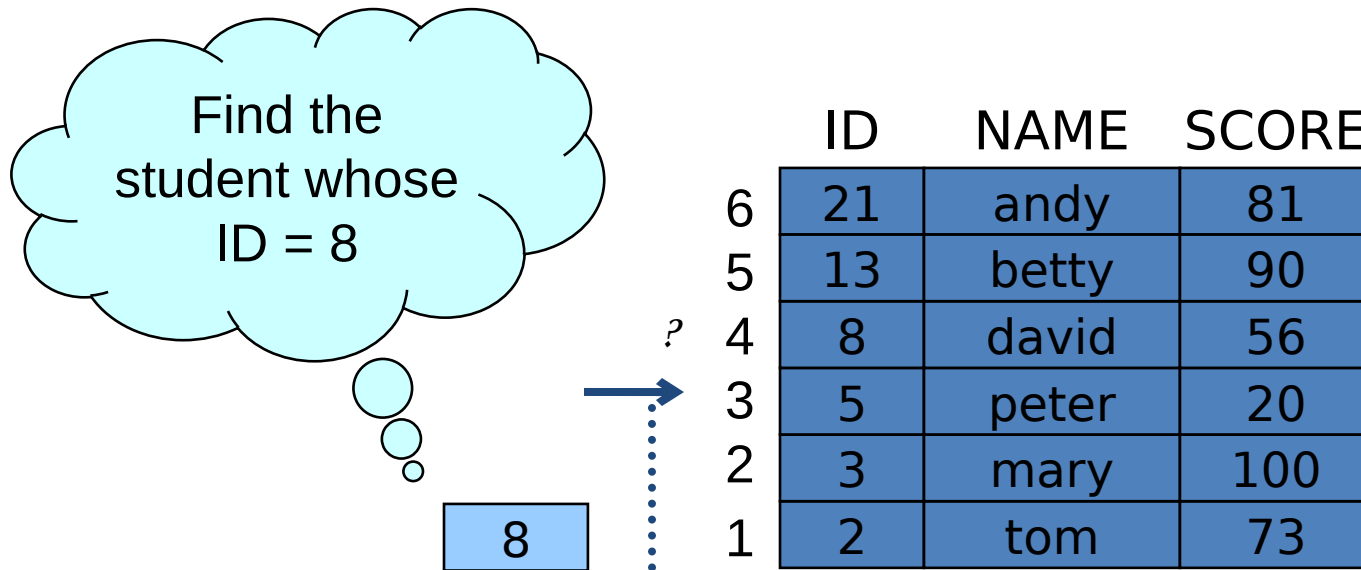
- Search is used everywhere in our daily life.
 - Search telephone number in telephone book
 - Search course schedule on registration guide
 - Search flight schedule on airline
 - Anything else?
- Search is performed the most often in database

Search

A set of records are stored in array, linked list, or others. Given a **target key**, find the record(s) that have the same **key**.



Search: Key



The key is the field in your record that is used for searching. In the above example, student ID is the key.

Search algorithm

- A step-by-step description of how to solve the search problem
- Some search algorithms:
 - sequential search
 - binary search

Sequential Search

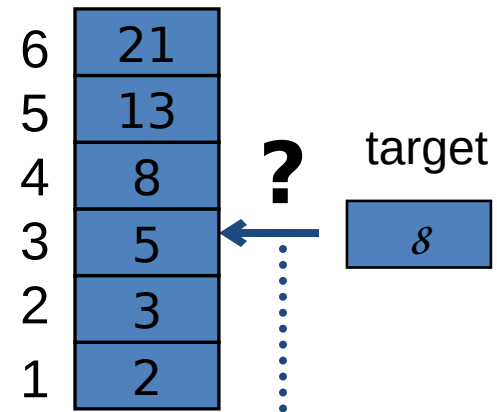
- A simple search algorithm
 - compare the target key to the key of records one by one starting from the first record
- Easy to implement for Array and Linked List

Sequential Search For Array

- An Array *db* which stores integer numbers
- Searching 8 in this array
- If found, return index
- Otherwise, return -1

Pseudo-code of Sequential Search For Array

```
int SequentialSearch( int key, int db[] )  
{   int index;  
    for( index=0; index<db.length; index++  
    )  
        {if( db[index]==key )  
            return index;  
        }  
    return -1;  
}
```



Complexity of Sequential Search

- Suppose there are n records
- In the best case, the target is the first entry. It only takes 1 step
- In the worst case, the target is the last entry, or it cannot be found. Sequential search has to scan all n records and takes totally n steps.
- Cost: $O(n)$

Linear Search Program

```
/* C++ Program to
   Implement Linear
   Search */
#include<iostream>
using namespace std;
int main()
{
int arr[10], i, num, index;
cout<<"Enter 10
Numbers: ";

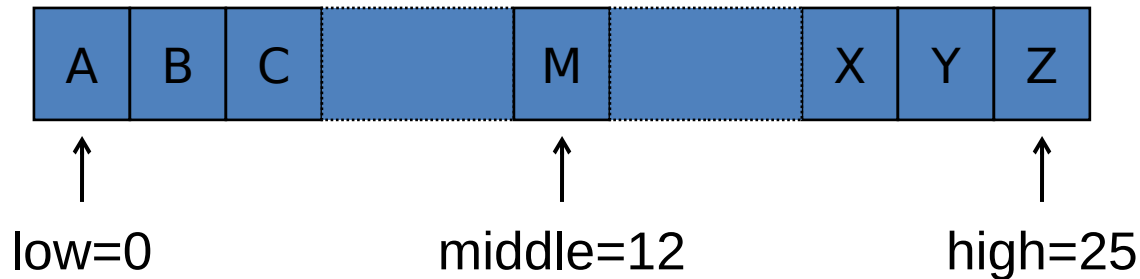
for(i=0; i<10; i++) cin>>arr[i];
cout<<"\nEnter a Number to
Search: ";
cin>>num;
for(i=0; i<10; i++)
{ if(arr[i]==num)
{ index = i; break; } }
cout<<"\nFound at Index
No."<<index;
cout<<endl;
return 0; }
```

Binary Search

- In binary search, we first compare the key with the item in the middle (after sorting them) position of the array.
- If there's a match, we can return immediately. If the key is less than the middle key, then the item sought must lie in the lower half of the array; if it's greater than the item sought must lie in the upper half of the array.
- So we repeat the procedure on the lower (or upper) half of the array.

Binary search

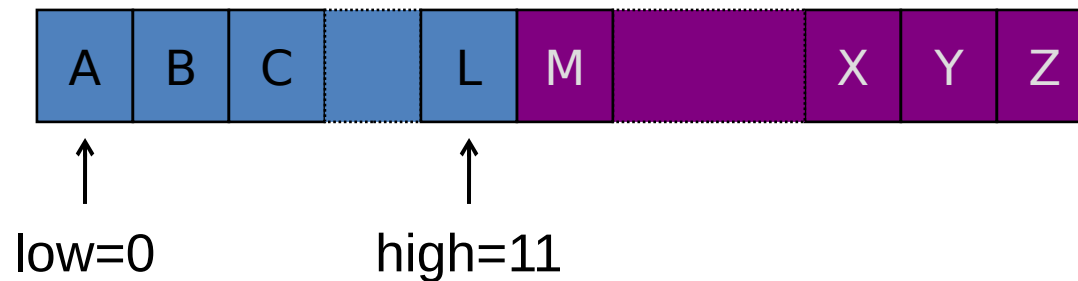
- If the target is present in the list, it must be one between 'low' and 'high'



Take a look at the middle one.
$$\text{middle} = (\text{low} + \text{high}) / 2$$

Binary search

- Assume target is 'E'

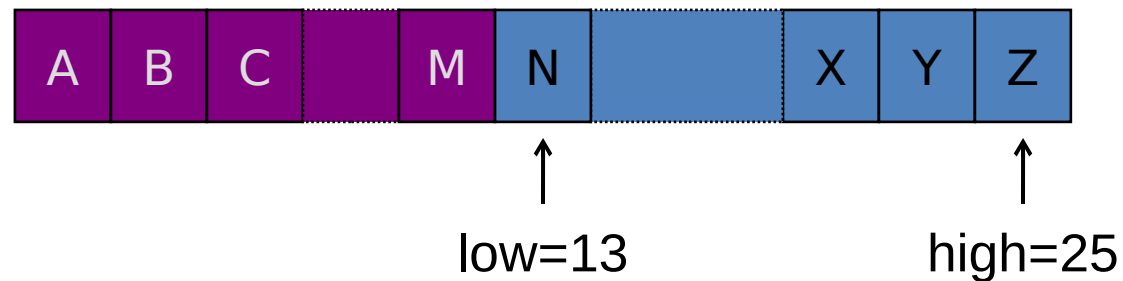


If target < the key value in the middle position, we know that it can not be found in the right half.

We only need to search in the left half. $high = middle - 1;$

Binary search

- Assume target is 'P'



If target > the key value in the middle position, we know that it can not be found in the left half.

We only need to search the right half. $low = middle + 1;$

Pseudo-code of Binary Search

```
int BinarySearch(char target, char
    array[])
{
    int n=20; // assume array seize is
    20
    int low=0, high =(n-1), middle;
    while( low<=high)
    {
        middle = (low+high)/2;
        if( array[middle]==target )
            return middle;
        else if( array[middle]<target )
            low = middle + 1;
        else
            high = middle - 1;
    }
    return -1;
}
```


How Binary Search Works

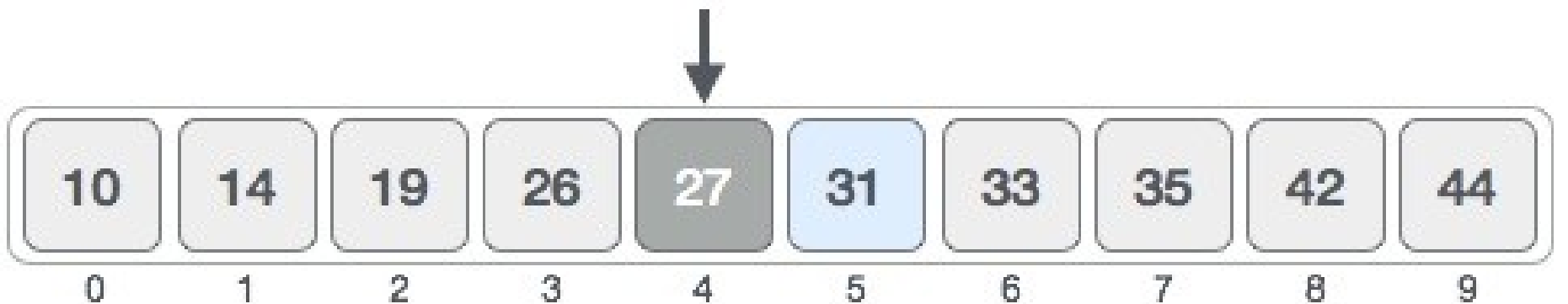
- For a binary search to work, it is mandatory for the target array to be sorted.
- The following is our sorted array and let us assume that we need to search the location of value 31 using binary search.



First, we shall determine half of the array by using this formula –

$$\text{mid} = (\text{low} + \text{high}) / 2$$

Here it is, $(9 + 0) / 2 = 4$ (integer value of 4.5). So, 4 is the mid of the array.



Now we compare the value stored at location 4, with the value being searched, i.e. 31. We find that the value at location 4 is 27, which is not a match. As the value is greater than 27 and we have a sorted array, so we also know that the target value must be in the upper portion of the array.



We change our low to $mid + 1$ and find the new mid value again.

$low = mid + 1$

$mid = (low + high) / 2$

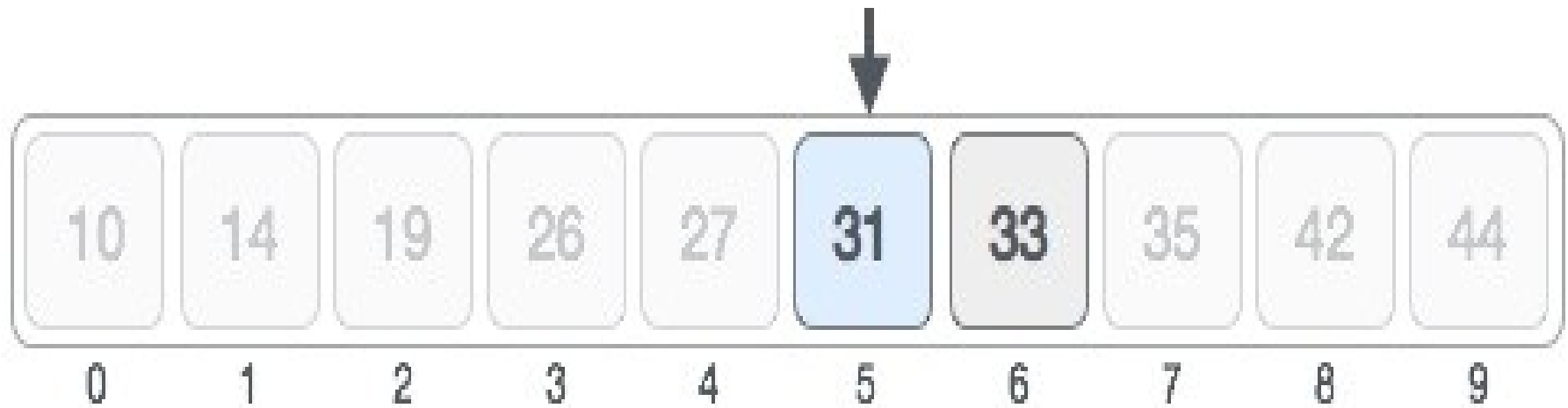
Our new mid is 7 now. We compare the value stored at location 7 with our target value 31.



The value stored at location 7 is not a match, rather it is more than what we are looking for. So, the value must be in the lower part from this location.



Hence, we calculate the mid again. This time it is 5.



We compare the value stored at location 5 with our target value. We find that it is a match.

10	14	19	26	27	31	33	35	42	44
0	1	2	3	4	5	6	7	8	9

We conclude that the target value 31 is stored at location 5.

Binary search halves the searchable items and thus reduces the count of comparisons to be made to very less numbers.

Complexity For Binary Search

- Analysis
 - Each step of the algorithm divides the block of items being searched in half. We can divide a set of ***n*** items in half at most **$\log_2 n$** times.
 - Thus the running time of a binary search is proportional to **$\log n$** and we say this is a **$O(\log n)$** algorithm.
 - Binary search requires a more complex program than sequential search and thus for *small n* it may run slower than the simple linear search.

END.

WAIRAGU G.R.