SATB

A Colourful Game of Musical Puzzles

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1 Rhythm

Time is divided up into a sequence of beats.

R1 Each voice can play a single colour on each beat.

R2 At least one voice must play on every beat.

2 Melody

A *melody* consists of a sequence of *prhases*. Each phrase is a sequence of colours that obeys the *phrasing* rules:

M1 A repeat must be followed by a step.

M2 A skip must be followed by a step in the opposite direction.

Example 1 There are two two-beat phrases that start with R:

$$[R \quad W] \qquad [R \quad Y]$$

and four three-beat phrases that start with R:

$$\begin{bmatrix} R & B & W \end{bmatrix} \qquad \begin{bmatrix} R & G & Y \end{bmatrix} \qquad \begin{bmatrix} R & R & Y \end{bmatrix} \qquad \begin{bmatrix} R & R & W \end{bmatrix}$$

3 Harmony

Harmony is when several different colours are played on the same beat. A *chord* is a set of colours that obey the *consonance* rule:

H1 No more than two colours in a chord may be adjacent.

Example 2 There are five one-colour chords:

$$[R]$$
 $[W]$ $[B]$ $[G]$ $[Y]$

ten two-colour chords:

$$\begin{bmatrix} R \\ W \end{bmatrix} \quad \begin{bmatrix} W \\ B \end{bmatrix} \quad \begin{bmatrix} B \\ G \end{bmatrix} \quad \begin{bmatrix} G \\ Y \end{bmatrix} \quad \begin{bmatrix} Y \\ R \end{bmatrix} \quad \begin{bmatrix} R \\ B \end{bmatrix} \quad \begin{bmatrix} W \\ G \end{bmatrix} \quad \begin{bmatrix} B \\ Y \end{bmatrix} \quad \begin{bmatrix} R \\ G \end{bmatrix} \quad \begin{bmatrix} W \\ Y \end{bmatrix}$$

and five three-colour chords:

$$\begin{bmatrix} R \\ G \\ B \end{bmatrix} \qquad \begin{bmatrix} W \\ Y \\ G \end{bmatrix} \qquad \begin{bmatrix} B \\ Y \\ R \end{bmatrix} \qquad \begin{bmatrix} G \\ R \\ W \end{bmatrix} \qquad \begin{bmatrix} Y \\ W \\ B \end{bmatrix}$$

A three-note chord consists of two adjacent colours and a third isolated colour. This isolated colour is called the *root* of the chord.

Example 3 R is the root of the three-note chord $\begin{bmatrix} R & G & B \end{bmatrix}^{\top}$.

4 Counterpoint

Counterpoint is when several voices play simultaneously. A pair of voices in *similar motion* if they both step or skip in the same direction. A pair of voices moves in *contrary motion* if they step or skip in opposite directions. A pair of voices move in *oblique motion* if one voice repeats a colour while the other voice changes colours. A group of melodies played in counterpoint must satisfy the *voice leading* rules:

C1 At least one voice must move on each beat.

C2 At least on pair of voices must move in contrary or oblique motion on each beat.

Example 4 This composition follows the rules established above:

$$\begin{bmatrix} B & Y & G & W & B \\ G & G & B & G & Y \\ R & W & B & W & R \end{bmatrix}$$