AUA CS108, Statistics, Fall 2020 Lecture 00, Intro to R

Michael Poghosyan

26 Aug 2020

► **R** is freeware

- **R** is freeware
- ► To install R, visit https://www.r-project.org/.

- **R** is freeware
- ► To install R, visit https://www.r-project.org/.
- Recommendation: Install also R Studio (freeware): https://www.rstudio.com/

- **R** is freeware
- ► To install R, visit https://www.r-project.org/.
- Recommendation: Install also R Studio (freeware): https://www.rstudio.com/
- ▶ I will use the following version: R version 4.0.2 (2020-06-22)

- **R** is freeware
- ► To install R, visit https://www.r-project.org/.
- Recommendation: Install also R Studio (freeware): https://www.rstudio.com/
- ▶ I will use the following version: R version 4.0.2 (2020-06-22)
- ▶ To find some R Studio shortcuts, hit *Alt* + *Shift* + *K*

- **R** is freeware
- ► To install R, visit https://www.r-project.org/.
- Recommendation: Install also R Studio (freeware): https://www.rstudio.com/
- ▶ I will use the following version: R version 4.0.2 (2020-06-22)
- ▶ To find some R Studio shortcuts, hit *Alt* + *Shift* + *K*

Here is a link to a reference book for R: An Introduction to R

You can start working with ${\bf R}$ in a Console, say, in ${\bf R}$ Studio or in R Terminal.

You can start working with **R** in a Console, say, in **R Studio** or in R Terminal. The Console shows the ">" sign, and you can write a command at that line and execute it by hitting *Enter*.

You can start working with **R** in a Console, say, in **R Studio** or in R Terminal. The Console shows the ">" sign, and you can write a command at that line and execute it by hitting *Enter*.

The output will be dispayed on the next line, and start with a number in a parenthesis, say,

2+3

[1] 5

Here '##' sign is for the slides, \mathbf{R} will not show that sign. It is to emphasize the \mathbf{R} output line. Also note that the \mathbf{R} code in my slides will be written in a color (and will not start by the ">" sign) 1 .

 $^{^{1}}$ I am using the **R Markdown**, which gives a possibility to integrate R code with **LaTeX**.

Here '##' sign is for the slides, \mathbf{R} will not show that sign. It is to emphasize the \mathbf{R} output line. Also note that the \mathbf{R} code in my slides will be written in a color (and will not start by the ">" sign) 1 .

The symbol [1] after the ## sign in the output shows the position in the output of the first element in the row. Let me explain by examples:

```
x <- c(12,3,43,24); x
## [1] 12 3 43 24
```

 $^{^{1}}$ I am using the **R Markdown**, which gives a possibility to integrate R code with **LaTeX**.

Here '##' sign is for the slides, \mathbf{R} will not show that sign. It is to emphasize the \mathbf{R} output line. Also note that the \mathbf{R} code in my slides will be written in a color (and will not start by the ">" sign) 1 .

The symbol [1] after the ## sign in the output shows the position in the output of the first element in the row. Let me explain by examples:

Here the first element in the output row, 12, is the first element in the output, so this line starts by [1].

 $^{^{1}}$ I am using the **R Markdown**, which gives a possibility to integrate R code with **LaTeX**.

Now, let us run the following:

[39]

##

```
seq(7, 120, 2)
     [1]
                        13
                             15
                                                    25
##
           7
                    11
                                  17
                                      19
                                           21
                                               23
                                                         27
                                                             29
   [20]
                    49
                             53
                                  55
                                      57
                                           59
                                               61
                                                    63
                                                         65
                                                             67
##
          45
               47
                        51
                                                                  69
```

99 101 103 105 10

Now, let us run the following:

```
seq(7, 120, 2)
```

[1] ## ## [20] ## [39] 99 101 103 105

Here, in the output, the command prints all odd numbers from 7 to 120.

 $^{^2}$ This is in my slides, which I am prepared using **RMarkdown**. If you will run the code in **R** console, you can have just 3 lines (btw, not all elements are shown in the slide, the output is wide for the slides)

Now, let us run the following:

```
seq(7, 120, 2)
## [1] 7 9 11 13 15 17 19 21 23 25 27 29 3
```

[20] ## ## [39] 99 101 103 105

Here, in the output, the command prints all odd numbers from 7 to 120. As you can see, the output is given in 4 lines². [1] in the first line shows that the first element in that row, 7, is the no. 1 element in the output. [18] at the beginning of the second line means that the first element in that row, 41, is the 18-th element in the output, and hence, 43 is the 19-th one. So 109 is the 52-nd element in the output, 111 is the 53-rd one, and you can calculate that we have 57 elements in the output in total.

 $^{^2}$ This is in my slides, which I am prepared using **RMarkdown**. If you will run the code in **R** console, you can have just 3 lines (btw, not all elements are shown in the slide, the output is wide for the slides)

Working in the Console is not too hard. Say, pi is the π , and "^" means "to the power":

```
pi<sup>2</sup>
```

```
## [1] 9.869604
```

Hitting the up/down arrows in Console will run over the Commands History.

Working in the Console is not too hard. Say, pi is the π , and "^" means "to the power":

```
pi<sup>2</sup>
```

```
## [1] 9.869604
```

Hitting the up/down arrows in Console will run over the Commands History. But it is not too convenient to work in the Console.

Working in the Console is not too hard. Say, pi is the π , and "^" means "to the power":

```
pi<sup>2</sup>
```

```
## [1] 9.869604
```

Hitting the up/down arrows in Console will run over the Commands History. But it is not too convenient to work in the Console.

This is because, for instanse, you can write at most one command in the Console (unless you put ";" sign between 2 commands), and also the code written in the Console will not be saved (well, will be saved in the History, in fact).

Working in the Console is not too hard. Say, pi is the π , and "^" means "to the power":

```
pi^2
```

```
## [1] 9.869604
```

Hitting the up/down arrows in Console will run over the Commands History. But it is not too convenient to work in the Console.

This is because, for instanse, you can write at most one command in the Console (unless you put ";" sign between 2 commands), and also the code written in the Console will not be saved (well, will be saved in the History, in fact).

So we will write our code in **.r** files, so we can run, update, change our code when we wish to.

And please send your **R** homework as **.r** files $\stackrel{..}{\smile}$

To create a New R Script:

ightharpoonup use File ightarrow New File ightarrow R Script

To create a New **R** Script:

- ightharpoonup use File ightharpoonup New File ightharpoonup R Script
- ightharpoonup or hit Ctrl + Shift + N

To create a New **R** Script:

- ightharpoonup use File ightharpoonup New File ightharpoonup R Script
- \triangleright or hit Ctrl + Shift + N
- or just create a file SomeName.R by using your favourite text editor (and open it in, say, R Studio)

To create a New **R** Script:

- ightharpoonup use File ightharpoonup New File ightharpoonup R Script
- ▶ or hit *Ctrl* + *Shift* + *N*
- or just create a file SomeName.R by using your favourite text editor (and open it in, say, R Studio)

To load your saved script from R:

ightharpoonup use File ightharpoonup Open File...

To run the command on some line of your R Script

▶ just put the cursor at that line and press *Ctrl* + *Enter*

To run the command on some line of your R Script

- ▶ just put the cursor at that line and press *Ctrl* + *Enter*
- or hit the Run button when the cursor is on that line

To run the command on some line of your R Script

- ▶ just put the cursor at that line and press *Ctrl* + *Enter*
- or hit the Run button when the cursor is on that line

To run a block of commands of your R Script

select that block and press Ctrl + Enter

To run the command on some line of your R Script

- ▶ just put the cursor at that line and press Ctrl + Enter
- or hit the Run button when the cursor is on that line

To run a block of commands of your R Script

- select that block and press Ctrl + Enter
- Say, Ctrl + A, Ctrl + Enter will execute the whole script. The same can be done by Ctrl + Alt + R

Commenting and Clearing the Console

▶ Use the symbol # to write a comment

```
Example:
```

```
4+5+6
```

1+2+3

```
## [1] 15
```

Commenting and Clearing the Console

▶ Use the symbol # to write a comment

Example:

```
# 1+2+3
4+5+6
```

```
## [1] 15
```

when you are in the console, use Ctrl + L to clear the console (without deleting the variables and data you have)

R Basic Operations and Commands

Here are some simple calculation examples. Try to run the following lines in the ${\bf R}$ Console:

```
pi*sqrt(10)+exp(4)

## [1] 64.53274

2^10

## [1] 1024

sin(2*pi)

## [1] -2.449213e-16
```

Usually, we are giving some names to quantities we calculate, to use them later. In ${\bf R}$ this can be done in two ways:

$$x = 10+20$$

or

 $^{^3}$ You can read more about the difference between these assignment operators here or here

Usually, we are giving some names to quantities we calculate, to use them later. In $\bf R$ this can be done in two ways:

$$x = 10+20$$

or

$$x < -10+20$$

R community is usually using the last way to assign a value to a variable, and we will follow the community $\ddot{}$ 3

 $^{^3}$ You can read more about the difference between these assignment operators here or here

Usually, we are giving some names to quantities we calculate, to use them later. In $\bf R$ this can be done in two ways:

$$x = 10+20$$

or

$$x < -10+20$$

R community is usually using the last way to assign a value to a variable, and we will follow the community $\ddot{}$ 3

You can also do in this way:

³You can read more about the difference between these assignment operators here or here

You can see that in both cases, x is assigned the value (say, you can see this in the *Environment* tab of **R Studio**), but the result is not printed on the screen.

You can see that in both cases, x is assigned the value (say, you can see this in the *Environment* tab of **R Studio**), but the result is not printed on the screen.

If you want to see the result of the assignment, just type \boldsymbol{X} after the assignment:

```
x
## [1] 30
or use
print(x)
## [1] 30
```

Defining Variables

You can see that in both cases, x is assigned the value (say, you can see this in the *Environment* tab of **R Studio**), but the result is not printed on the screen.

If you want to see the result of the assignment, just type \boldsymbol{X} after the assignment:

```
## [1] 30
or use
print(x)
## [1] 30
The other way is to run
```

[1] 30

(x < -10 + 20)

Example

Here is a piece of code, just some calculations:

```
x <- 20
y <- 2*(x-pi)
z <- sin(y)
z
## [1] 0.7451132
```

Example

Here is a piece of code, just some calculations:

```
x \leftarrow 20

y \leftarrow 2*(x-pi)

z \leftarrow \sin(y)

z

## [1] 0.7451132

You can write several commands in a line, by separating them by ";":

x \leftarrow 10; y \leftarrow \exp(2); z \leftarrow \sin(1); print(x+y+z)
```

```
## [1] 18.23053
```

Example

Here is a piece of code, just some calculations:

```
x <- 20
y <- 2*(x-pi)
z <- sin(y)
z
```

[1] 0.7451132

You can write several commands in a line, by separating them by ";":

```
x \leftarrow 10; y \leftarrow exp(2); z \leftarrow sin(1); print(x+y+z)
```

```
## [1] 18.23053
```

To remove the variable x from the memory (to "forget" the variable x), just run

```
rm(x)
```

The following assignment

$$x \leftarrow c(1,3,5, -3, 2.3)$$

assigns *x* to be the vector x = (1, 3, 5, -3, 2.3).

The following assignment

$$x \leftarrow c(1,3,5, -3, 2.3)$$

assigns x to be the vector x = (1, 3, 5, -3, 2.3). And you can use then

X

```
## [1] 1.0 3.0 5.0 -3.0 2.3
```

The following assignment

```
x \leftarrow c(1,3,5, -3, 2.3)
```

assigns x to be the vector x = (1, 3, 5, -3, 2.3). And you can use then

X

```
## [1] 1.0 3.0 5.0 -3.0 2.3
```

x[2]

```
## [1] 3
```

The following assignment

```
x \leftarrow c(1,3,5, -3, 2.3)
```

assigns x to be the vector x = (1, 3, 5, -3, 2.3). And you can use then

```
Х
```

```
## [1] 1.0 3.0 5.0 -3.0 2.3
```

```
x[2]
```

```
## [1] 3
```

$$x[-1]$$

```
## [1] 3.0 5.0 -3.0 2.3
```

The following will make an empty vector:

$$x \leftarrow c()$$

The following will make an empty vector:

$$x \leftarrow c()$$

c in the vecor definition comes from **concatinate**.

The following will make an empty vector:

```
x <- c()
```

c in the vecor definition comes from concatinate.

Using c, you can add an element to a vector:

```
x <- c(x, 2)
```

[1] 2

x was an empty vector, not we have added an element, and now x=(2)=2.

The following will make an empty vector:

```
x <- c()
```

c in the vecor definition comes from concatinate.

Using c, you can add an element to a vector:

```
x <- c(x, 2)
x
```

[1] 2

x was an empty vector, not we have added an element, and now x=(2)=2.

We can concatenate also several vectors:

```
x \leftarrow c(1,2,3); y \leftarrow c(4,5,6); z \leftarrow c(x,y)
```

(x < -1:10)

Besides the above method, by specifying all elements of the vector, we can make some standard vectors using appropriate commands:

```
## [1] 1 2 3 4 5 6 7 8 9 10
a <- seq(from=1, to=10, by=2); a

## [1] 1 3 5 7 9
b <- seq(from=1, to=10, length.out = 7); b

## [1] 1.0 2.5 4.0 5.5 7.0 8.5 10.0</pre>
```

```
y \leftarrow rep(1, 5); y
## [1] 1 1 1 1 1
z \leftarrow rep(1:3, 4); z
## [1] 1 2 3 1 2 3 1 2 3 1 2 3
t \leftarrow rep(1:3, each = 4); print(t)
## [1] 1 1 1 1 2 2 2 2 3 3 3 3
w \leftarrow rep(c(1,3), 2); w
## [1] 1 3 1 3
```

Another useful method to generate vectors is to choose random samples:

```
# Uniform Sample of size 10 from [0,3]
x \leftarrow runif(10, min = 0, max = 3)
Х
##
   [1] 1.8438019 1.0636570 0.8362773 1.8863407 1.8961920 3
##
    [8] 0.8500620 2.4509963 2.9031644
# Normal Sample of size 15 with Mean O and Standard Deviat
x \leftarrow rnorm(15, mean = 0, sd = 2)
Х
##
    [1] -5.2290711 -1.0571118 2.8299235 -0.7741859 -1.4399
    [7] 1.6455064 -1.6083296 -0.5446899 -0.4510518 0.7010
##
## [13] -3.6048588 0.9346354 1.0930198
```

Another useful method to generate vectors is to choose random samples:

```
# Uniform Sample of size 10 from [0,3]
x \leftarrow runif(10, min = 0, max = 3)
Х
##
   [1] 1.8438019 1.0636570 0.8362773 1.8863407 1.8961920 3
   [8] 0.8500620 2.4509963 2.9031644
##
# Normal Sample of size 15 with Mean O and Standard Deviat
x \leftarrow rnorm(15, mean = 0, sd = 2)
Х
   [1] -5.2290711 -1.0571118 2.8299235 -0.7741859 -1.4399
##
    [7] 1.6455064 -1.6083296 -0.5446899 -0.4510518 0.7016
##
## [13] -3.6048588 0.9346354 1.0930198
```

Later we will talk about distributions in **R** and random samples.

[1] -115

```
For a vector
x \leftarrow c(-1, 2.3, 10, 5)
we can calculate
length(x) #The Lenght of a vector
## [1] 4
sum(x) # The sum of elements
## [1] 16.3
cumsum(x) # The cumulative sum, x_1, x_1+x_2,...
## [1] -1.0 1.3 11.3 16.3
prod(x)
```

```
cumprod(x)
## [1] -1.0 -2.3 -23.0 -115.0
mean(x) # The mean of the elements
## [1] 4.075
max(x); min(x)
## [1] 10
## [1] -1
sin(x)
## [1] -0.8414710 0.7457052 -0.5440211 -0.9589243
x^2
## [1] 1.00 5.29 100.00 25.00
```

Sorting a vector is easy:

```
sort(x)
## [1] -1.0 2.3 5.0 10.0
```

```
Sorting a vector is easy:
```

```
sort(x)
## [1] -1.0 2.3 5.0 10.0
```

Sorting in the decreasing order is easy too:

```
sort(x, decreasing = TRUE)
## [1] 10.0 5.0 2.3 -1.0
```

Let

$$x \leftarrow c(3, -1, 4, 3, 2, 5)$$

Let

$$x \leftarrow c(3, -1, 4, 3, 2, 5)$$

Then we can use

```
x[2] #The second element
```

```
## [1] -1
```

$$x[-3]$$
 #everything without $x[3]$

A little bit complicated example is

```
x[x>0] #all positive elements
```

```
## [1] 3 4 3 2 5
```

A little bit complicated example is

```
x[x>0] #all positive elements
```

[1] 3 4 3 2 5

You can use x>0 to see what this command is doing:

```
x>0
```

```
## [1] TRUE FALSE TRUE TRUE TRUE TRUE
```

A little bit complicated example is

```
x[x>0] #all positive elements
```

```
## [1] 3 4 3 2 5
```

You can use x>0 to see what this command is doing:

```
x>0
```

```
## [1] TRUE FALSE TRUE TRUE TRUE TRUE
```

Another example:

```
x[x\%2 == 0] #only the even elements of x
```

```
## [1] 4 2
```

Making a DataFrame

DataFrame is one of the important objects in Data Analysis. It is a rectangular data set, similar to the MS Excel Table/Spreadsheet, if you know what it is $\ddot{\ }$

Let us make a DataFrame in R:

```
x <- c(22,43,16,38)
y <- c(76, 81, 55, 66)
df <- data.frame(age=x, weight=y)</pre>
```

And here is our DataFrame:

df

Viewing/Editing DataFrames

Well, besides just typing the name of the DataFrame, or calling print(df), one can use the following command to view the DataFrame:

View(df)

or to edit the DataFreame:

edit(df)

Accessing the columns/rows of a DataFrame

```
You can access the column "weight" by
df[,2]
## [1] 76 81 55 66
or by
df[,'weight'] # also df[,"weight"]
## [1] 76 81 55 66
or by
df$weight
## [1] 76 81 55 66
```

```
Some Examples
   mean(df$age) # mean age
   ## [1] 29.75
   sum(df$weight) # sum of weights, total weight
   ## [1] 278
   length(df$weight) # the number of elements in df$weights
   ## [1] 4
   sum(df$weight)/length(df$weight) # same as the mean(df$wei
   ## [1] 69.5
   sort(df$weight) # weights in the increasing order
   ## [1] 55 66 76 81
   sort(df$age, decreasing = T) # ages in the decreasing order
```

R Built-In Datasets

The Basic \boldsymbol{R} includes many Datasets to analyse. You can see the datasets supplied by the datasets package by running

data()

Or, if you will run

data(package="MASS")

it will show the avalable datasets in the ${f R}$ package MASS.

R Built-In Datasets

The Basic ${\bf R}$ includes many Datasets to analyse. You can see the datasets supplied by the datasets package by running

```
data()
```

cars

Or, if you will run

```
data(package="MASS")
```

it will show the avalable datasets in the ${f R}$ package MASS.

For example, cars is one of the standard datasets in **R**. To see the content, just run

speed dist

R Built-In Datasets

In our previous example, the dataset was too large to fit into the slide (try to run it in $\bf R$ console by yourself). To see the first/last few rows of the dataset, use

```
head(cars) #first six rows
```

```
## speed dist
## 1 4 2
## 2 4 10
## 3 7 4
## 4 7 22
## 5 8 16
## 6 9 10
```

or

```
tail(cars, 1) #last 1 row
```

```
## speed dist
## 50 25 85
```

Installing a Package

There are a lot of supplementary packages designed for extra tasks, giving us different functions and datasets. To install a package, run install.packages("name_of_the_package"). For example, to install the ggplot2 package (for nice graphics, gg=grammar of graphics, not a taxi service), you need to run

install.packages("ggplot2")

Using a function from a Package

If you want to use a function or a dataset from a package, you need to load that package first, then use the function/dataset. Say, we want to use the rmvnorm function from the package mvtnorm to generate a random sample of size 100 from the multivariate Normal Distribution. First, install mvtnorm by using

```
install.packages("mvtnorm")
```

Using a function from a Package

If you want to use a function or a dataset from a package, you need to load that package first, then use the function/dataset. Say, we want to use the rmvnorm function from the package mvtnorm to generate a random sample of size 100 from the multivariate Normal Distribution. First, install mvtnorm by using

```
install.packages("mvtnorm")
```

Then run:

```
library(mvtnorm)
mu <- c(1,2) #The Mean of our Bivariate Normal Distribution
sigma <- matrix(c(4,2,2,3), ncol = 2) # The Covariance Matrix
x <- rmvnorm(n = 100, mean = mu, sigma = sigma)</pre>
```

Here the command library(mvtnorm) is similar to include of C++ or import of Python, and the above code will give an error without this line.

Using a function from a Package

Another way, without importing the package by the library command, is to use

```
x <- mvtnorm::rmvnorm(n = 100, mean = mu, sigma = sigma)
```

Using a function from a Package

Another way, without importing the package by the library command, is to use

```
x <- mvtnorm::rmvnorm(n = 100, mean = mu, sigma = sigma)
```

Anothe example:

MASS::SP500

will print the SP500 dataset of the MASS package (returns of the S&P500 index in 1990's).

Using a function from a Package

Another way, without importing the package by the library command, is to use

```
x <- mvtnorm::rmvnorm(n = 100, mean = mu, sigma = sigma)
```

Anothe example:

MASS::SP500

will print the SP500 dataset of the MASS package (returns of the S&P500 index in 1990's).

To see the list of loaded base/attached packages, you can use

```
sessionInfo()
```

Using Help

To open the \mathbf{R} 's help page for some command, say, for the sum command, you can use on of the following options:

?sum

or

help(sum)

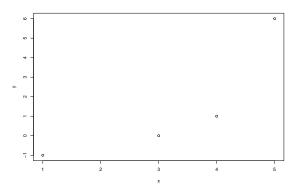
or, in **R Studio**, just put the cursor at some place on the word sum and hit F1. Anothe method is just to use the Google $\ddot{-}$

Here we will use the default package for plots⁴.

⁴More you can get using the ggplot2 package

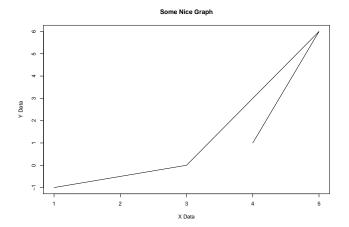
Here we will use the default package for plots⁴. First, let us plot some points (x_i, y_i) , i = 1, ..., n:

```
x \leftarrow c(1,3,5,4); y \leftarrow c(-1, 0,6, 1)
plot(x,y)
```



⁴More you can get using the ggplot2 package

Now, we join the points with line segments, add a title and axis labels to our graph:



Comments:

- type is the type of the plot. type="1" means that the type is set to lines. Try without the type parameter, or by type = "h", type = "s"
- main is the title of the graph
- xlab and ylab are the axis labels (names)

In **R**, we have low-level and high-level graphical commands. The plot command is a low-level plot. If you will use 2 plot commands one after another, the last command will draw on a new canvas. So if you want to draw two graphs one over anoher, you cannot just use two plot commands consecutively.

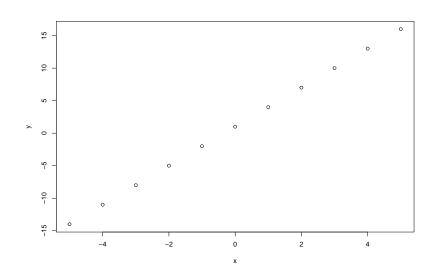
 $^{^{5}}$ In fact, in **R Studio**, under the **Plots** tab, you can navigate through the plots

In **R**, we have low-level and high-level graphical commands. The plot command is a low-level plot. If you will use 2 plot commands one after another, the last command will draw on a new canvas. So if you want to draw two graphs one over anoher, you cannot just use two plot commands consecutively. In general, when using 2 low-level graphical commands, the last one will "overwrite" the previous plot ⁵. But, when using high-level plotting commands after the low-level one, you will have the high-level plot added to the low-level one. High-level plot examples are points and lines.

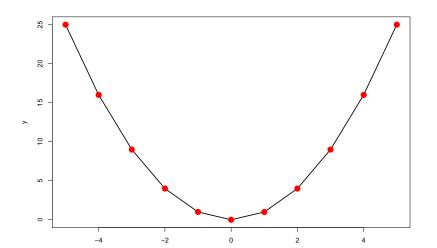
 $^{^{5}}$ In fact, in **R Studio**, under the **Plots** tab, you can navigate through the plots

Making Plots, Example $x \leftarrow -5:5$; $y \leftarrow 3*x+1$

plot(x,y)



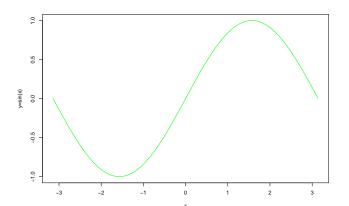
```
x <- -5:5; y <- x^2
plot(x,y, type = "1", lwd = 2)
points(x,y, pch = 16, col = "red", cex = 2)</pre>
```



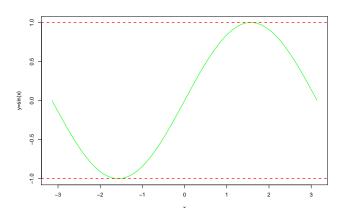
Comments:

- ▶ 1wd is the *line width*
- pch is the *point character*, try to change 16 to other integers
- col is the color
- cex is the character size, point size

Let us plot the graph of $y = \sin(x)$, $x \in [-\pi, \pi]$:



Now, let us add horizontal lines $y = \pm 1$ to previous plot:

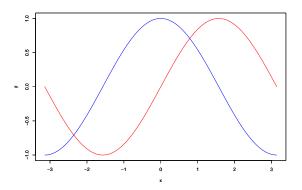


Comments:

- ▶ abline is to draw a line $y = a + b \cdot x$, you can give parameters $h = h_0$ for a horizontal line $y = h_0$ or $v = v_0$ for a vertical line $x = v_0$. abline is a high-level graphical command
- ▶ 1ty is the *line type*, try changing the values to see the difference (here we have a dotted line)

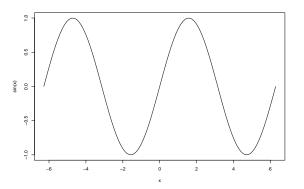
Now, let us draw two plots one over another:

```
x <- seq(from = -pi, to = pi, by = 0.01)
y <- sin(x); z <- cos(x)
plot(x,y, type = "l", lwd =1.5, col = 'red')
par(new = TRUE) #setting a parameter to keep the previous plot(x,z, type = "l", lwd =1.5, col = 'blue')</pre>
```



Another method to draw graphs is to use the curve command:

```
curve(\sin, from = -2*pi, to = 2*pi)
```



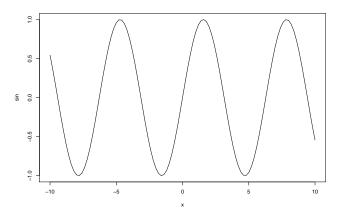
Try also⁶

```
\underline{\text{curve}(\sin(x), \text{from = }-2*pi, \text{to = }2*pi)}
```

⁶If the variable x is not defined!

Yet another method to draw graphs is to use the plot command with function name:

```
plot(sin, -10, 10)
```



It is easy to define a function in \mathbf{R} . You just need to use the following template:

```
For example, let us define the function z = x^2 + 2 * \arctan \frac{x}{x + \sin(x)}:
```

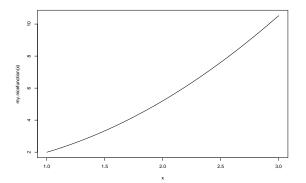
```
my.nicefunction <- function (x){
  z = x^2 +2* atan(x/(x+sin(x)))
  return(z)
}</pre>
```

Now, we can calculate our function's value at, say, the point 3, and plot its graph:

```
my.nicefunction(3)
```

```
## [1] 10.52485
```

curve(my.nicefunction, 1, 3) #or plot(my.nicefunction, 1,



Now, let us define a function of 2 variables:

```
my_fun1 <- function (x, y){
  return(x+y^2)
}</pre>
```

In this case, to calculate the value at (1,2), you just write

```
my_fun1(1,2)
```

```
## [1] 5
```

You can define also functions with default values:

```
my fun2 <- function (x, y = 0){
  return(x+y^2)
}
Now, my_fun(2) will give my_fun(2,0), and my_fun(2, 4) will
calculate my_fun(2,4):
my_fun2(2)
## [1] 2
my fun2(2,4)
## [1] 18
```

By the way, if you will give default values to each variable, like here:

```
my_fun3 <- function (x = 0, y = 0){
  return(x+y^2)
```

Then you can use the followings to calculate my fun3(2,1):

```
my_fun3(2,1)
## [1] 3
my_fun3(x = 2, y = 1)
## [1] 3
my fun3(y = 1, x = 2)
## [1] 3
```

Actually, most of the built-in ${\bf R}$ functions have named variables with default values. Say, use

You will see the help page, containing the usage of the function rnorm, in the form:

```
rnorm(n, mean = 0, sd = 1)
```

This means, that if you will use rnorm(10), it will assume mean = 0 and sd = 1. And you can mix the order of the *named* variables, say, run rnorm(10, sd = 3, mean = -1). But please note that you cannot skip the first variable, the value of n, since it has no default value!