AUA CS 108, Statistics, Fall 2019 R Lab Session 01

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Here is a link to a reference book for R: An Introduction to R

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The output will be dispayed on the next line, and start with a number in a parenthesis, say,

2+3

[1] 5

Here '##' sign is for the slides, \mathbf{R} will not show that sign. It is to emphasize the \mathbf{R} output line. Also note that the \mathbf{R} code in my slides will be written in a color (and will not start by the ">" sign) 1 .

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The symbol [1] after the ## sign in the output shows the position in the output of the first element in the row. Let me explain by examples:

```
x <- c(12,3,43,24); x
## [1] 12 3 43 24
```

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The symbol [1] after the ## sign in the output shows the position in the output of the first element in the row. Let me explain by examples:

Here the first element in the output row, 12, is the first element in the output, so this line starts by [1].

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Now, let us run the following:

[39]

##

```
seq(7, 120, 2)
     [1]
                        13
                             15
                                                    25
##
           7
                    11
                                  17
                                      19
                                           21
                                               23
                                                         27
                                                             29
   [20]
                    49
                             53
                                  55
                                      57
                                           59
                                               61
                                                    63
                                                         65
                                                             67
##
          45
               47
                        51
                                                                  69
```

99 101 103 105 10

Now, let us run the following:

```
seq(7, 120, 2)
```

[1] ## ## [20] ## [39] 99 101 103 105

Here, in the output, the command prints all odd numbers from 7 to 120.

 $^{^2}$ This is in my slides, which I am prepared using **RMarkdown**. If you will run the code in **R** console, you can have just 3 lines (btw, not all elements are shown in the slide, the output is wide for the slides)

Now, let us run the following:

```
seq(7, 120, 2)
## [1] 7 9 11 13 15 17 19 21 23 25 27 29 3
```

[20] ## ## [39] 99 101 103 105

Here, in the output, the command prints all odd numbers from 7 to 120. As you can see, the output is given in 4 lines². [1] in the first line shows that the first element in that row, 7, is the no. 1 element in the output. [18] at the beginning of the second line means that the first element in that row, 41, is the 18-th element in the output, and hence, 43 is the 19-th one. So 109 is the 52-nd element in the output, 111 is the 53-rd one, and you can calculate that we have 57 elements in the output in total.

 $^{^2}$ This is in my slides, which I am prepared using **RMarkdown**. If you will run the code in **R** console, you can have just 3 lines (btw, not all elements are shown in the slide, the output is wide for the slides)

Working in the Console is not too hard. Say, pi is the π , and "^" means "to the power":

```
pi<sup>2</sup>
```

```
## [1] 9.869604
```

Hitting the up/down arrows in Console will run over the Commands History.

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This is because, for instanse, you can write at most one command in the Console (unless you put ";" sign between 2 commands), and also the code written in the Console will not be saved (well, will be saved in the History, in fact).

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This is because, for instanse, you can write at most one command in the Console (unless you put ";" sign between 2 commands), and also the code written in the Console will not be saved (well, will be saved in the History, in fact).

So we will write our code in **.r** files, so we can run, update, change our code when we wish to.

And please send your **R** homework as **.r** files $\stackrel{..}{\smile}$

To create a New R Script:

ightharpoonup use File ightarrow New File ightarrow R Script

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- or just create a file SomeName.R by using your favourite text editor (and open it in, say, R Studio)

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To load your saved script from R:

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▶ just put the cursor at that line and press *Ctrl* + *Enter*

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- select that block and press Ctrl + Enter
- Say, Ctrl + A, Ctrl + Enter will execute the whole script. The same can be done by Ctrl + Alt + R

Commenting and Clearing the Console

▶ Use the symbol # to write a comment

```
Example:
```

```
4+5+6
```

1+2+3

```
## [1] 15
```

Commenting and Clearing the Console

▶ Use the symbol # to write a comment

Example:

```
# 1+2+3
4+5+6
```

```
## [1] 15
```

when you are in the console, use Ctrl + L to clear the console (without deleting the variables and data you have)

R Basic Operations and Commands

Here are some simple calculation examples. Try to run the following lines in the ${\bf R}$ Console:

```
pi*sqrt(10)+exp(4)

## [1] 64.53274

2^10

## [1] 1024

sin(2*pi)

## [1] -2.449213e-16
```

Usually, we are giving some names to quantities we calculate, to use them later. In ${\bf R}$ this can be done in two ways:

$$x = 10+20$$

or

 $^{^3}$ You can read more about the difference between these assignment operators here or here

Usually, we are giving some names to quantities we calculate, to use them later. In $\bf R$ this can be done in two ways:

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R community is usually using the last way to assign a value to a variable, and we will follow the community $\ddot{}$ 3

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You can also do in this way:

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You can see that in both cases, x is assigned the value (say, you can see this in the *Environment* tab of **R Studio**), but the result is not printed on the screen.

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If you want to see the result of the assignment, just type \boldsymbol{X} after the assignment:

```
x
## [1] 30
or use
print(x)
## [1] 30
```

Defining Variables

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```
## [1] 30
or use
print(x)
## [1] 30
The other way is to run
```

[1] 30

(x < -10 + 20)

Example

Here is a piece of code, just some calculations:

```
x <- 20
y <- 2*(x-pi)
z <- sin(y)
z
## [1] 0.7451132
```

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```
x \leftarrow 20

y \leftarrow 2*(x-pi)

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You can write several commands in a line, by separating them by ";":

x \leftarrow 10; y \leftarrow \exp(2); z \leftarrow \sin(1); print(x+y+z)
```

```
## [1] 18.23053
```

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```

```
## [1] 18.23053
```

To remove the variable x from the memory (to "forget" the variable x), just run

```
rm(x)
```

The following assignment

$$x \leftarrow c(1,3,5, -3, 2.3)$$

assigns *x* to be the vector x = (1, 3, 5, -3, 2.3).

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X

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X

```
## [1] 1.0 3.0 5.0 -3.0 2.3
```

x[2]

```
## [1] 3
```

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```
Х
```

```
## [1] 1.0 3.0 5.0 -3.0 2.3
```

```
x[2]
```

```
## [1] 3
```

$$x[-1]$$

```
## [1] 3.0 5.0 -3.0 2.3
```

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Using c, you can add an element to a vector:

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x <- c(x, 2)
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[1] 2

x was an empty vector, not we have added an element, and now x=(2)=2.

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```

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We can concatenate also several vectors:

```
x \leftarrow c(1,2,3); y \leftarrow c(4,5,6); z \leftarrow c(x,y)
```

(x < -1:10)

Besides the above method, by specifying all elements of the vector, we can make some standard vectors using appropriate commands:

```
## [1] 1 2 3 4 5 6 7 8 9 10
a <- seq(from=1, to=10, by=2); a

## [1] 1 3 5 7 9
b <- seq(from=1, to=10, length.out = 7); b

## [1] 1.0 2.5 4.0 5.5 7.0 8.5 10.0</pre>
```

```
y \leftarrow rep(1, 5); y
## [1] 1 1 1 1 1
z \leftarrow rep(1:3, 4); z
## [1] 1 2 3 1 2 3 1 2 3 1 2 3
t \leftarrow rep(1:3, each = 4); print(t)
## [1] 1 1 1 1 2 2 2 2 3 3 3 3
w \leftarrow rep(c(1,3), 2); w
## [1] 1 3 1 3
```

Another useful method to generate vectors is to choose random samples:

```
# Uniform Sample of size 10 from [0,3]
x \leftarrow runif(10, min = 0, max = 3)
X
##
   [1] 0.4924354 1.1149195 2.6196978 2.4271227 2.8708527
##
   [8] 0.8951109 0.2501558 2.2553890
# Normal Sample of size 15 with Mean O and Standard Deviat
x \leftarrow rnorm(15, mean = 0, sd = 2)
х
## [1] -1.29047522 1.00992019 1.18918428 -1.24092485 -1
## [7] 0.69802600 1.63067232 -3.39887823 -0.13533879 2
## [13] 0.08266733 5.27828355 -2.59519514
```

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## [13] 0.08266733 5.27828355 -2.59519514
```

Later we will talk about distributions in \mathbf{R} and random samples.

[1] -115

```
For a vector
x \leftarrow c(-1, 2.3, 10, 5)
we can calculate
length(x) #The Lenght of a vector
## [1] 4
sum(x) # The sum of elements
## [1] 16.3
cumsum(x) # The cumulative sum, x_1, x_1+x_2,...
## [1] -1.0 1.3 11.3 16.3
prod(x)
```

```
cumprod(x)
## [1] -1.0 -2.3 -23.0 -115.0
mean(x) # The mean of the elements
## [1] 4.075
max(x); min(x)
## [1] 10
## [1] -1
sin(x)
## [1] -0.8414710 0.7457052 -0.5440211 -0.9589243
x^2
## [1] 1.00 5.29 100.00 25.00
```

Sorting a vector is easy:

```
sort(x)
## [1] -1.0 2.3 5.0 10.0
```

```
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```
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## [1] -1.0 2.3 5.0 10.0
```

Sorting in the decreasing order is easy too:

```
sort(x, decreasing = TRUE)
## [1] 10.0 5.0 2.3 -1.0
```

Let

$$x \leftarrow c(3, -1, 4, 3, 2, 5)$$

Let

$$x \leftarrow c(3, -1, 4, 3, 2, 5)$$

Then we can use

```
x[2] #The second element
```

```
## [1] -1
```

$$x[-3]$$
 #everything without $x[3]$

A little bit complicated example is

```
x[x>0] #all positive elements
```

```
## [1] 3 4 3 2 5
```

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```
x[x>0] #all positive elements
```

[1] 3 4 3 2 5

You can use x>0 to see what this command is doing:

```
x>0
```

```
## [1] TRUE FALSE TRUE TRUE TRUE TRUE
```

A little bit complicated example is

```
x[x>0] #all positive elements
```

```
## [1] 3 4 3 2 5
```

You can use x>0 to see what this command is doing:

```
x>0
```

```
## [1] TRUE FALSE TRUE TRUE TRUE TRUE
```

Another example:

```
x[x\%2 == 0] #only the even elements of x
```

```
## [1] 4 2
```

Making a DataFrame

DataFrame is one of the important objects in Data Analysis. It is a rectangular data set, similar to the MS Excel Table/Spreadsheet, if you know what it is $\ddot{\ }$

Let us make a DataFrame in R:

```
x <- c(22,43,16,38)
y <- c(76, 81, 55, 66)
df <- data.frame(age=x, weight=y)</pre>
```

And here is our DataFrame:

df

Viewing/Editing DataFrames

Well, besides just typing the name of the DataFrame, or calling print(df), one can use the following command to view the DataFrame:

View(df)

or to edit the DataFreame:

edit(df)

Accessing the columns/rows of a DataFrame

```
You can access the column "weight" by
df[,2]
## [1] 76 81 55 66
or by
df[,'weight'] # also df[,"weight"]
## [1] 76 81 55 66
or by
df$weight
## [1] 76 81 55 66
```

```
Some Examples
   mean(df$age) # mean age
   ## [1] 29.75
   sum(df$weight) # sum of weights, total weight
   ## [1] 278
   length(df$weight) # the number of elements in df$weights
   ## [1] 4
   sum(df$weight)/length(df$weight) # same as the mean(df$wei
   ## [1] 69.5
   sort(df$weight) # weights in the increasing order
   ## [1] 55 66 76 81
   sort(df$age, decreasing = T) # ages in the decreasing order
```

R Built-In Datasets

The Basic \boldsymbol{R} includes many Datasets to analyse. You can see the datasets supplied by the datasets package by running

data()

Or, if you will run

data(package="MASS")

it will show the avalable datasets in the ${f R}$ package MASS.

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```
data()
```

cars

Or, if you will run

```
data(package="MASS")
```

it will show the avalable datasets in the ${f R}$ package MASS.

For example, cars is one of the standard datasets in **R**. To see the content, just run

speed dist

R Built-In Datasets

In our previous example, the dataset was too large to fit into the slide (try to run it in $\bf R$ console by yourself). To see the first/last few rows of the dataset, use

```
head(cars) #first six rows
```

```
## speed dist
## 1 4 2
## 2 4 10
## 3 7 4
## 4 7 22
## 5 8 16
## 6 9 10
```

or

```
tail(cars, 1) #last 1 row
```

```
## speed dist
## 50 25 85
```

Installing a Package

There are a lot of supplementary packages designed for extra tasks, giving us different functions and datasets. To install a package, run install.packages("name_of_the_package"). For example, to install the ggplot2 package (for nice graphics, gg=grammar of graphics, not a taxi service), you need to run

install.packages("ggplot2")

Using a function from a Package

If you want to use a function or a dataset from a package, you need to load that package first, then use the function/dataset. Say, we want to use the rmvnorm function from the package mvtnorm to generate a random sample of size 100 from the multivariate Normal Distribution. First, install mvtnorm by using

```
install.packages("mvtnorm")
```

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```
install.packages("mvtnorm")
```

Then run:

```
library(mvtnorm)
mu <- c(1,2) #The Mean of our Bivariate Normal Distribution
sigma <- matrix(c(4,2,2,3), ncol = 2) # The Covariance Matrix
x <- rmvnorm(n = 100, mean = mu, sigma = sigma)</pre>
```

Here the command library(mvtnorm) is similar to include of C++ or import of Python, and the above code will give an error without this line.

Using a function from a Package

Another way, without importing the package by the library command, is to use

```
x <- mvtnorm::rmvnorm(n = 100, mean = mu, sigma = sigma)
```

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Anothe example:

MASS::SP500

will print the SP500 dataset of the MASS package (returns of the S&P500 index in 1990's).

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To see the list of loaded base/attached packages, you can use

```
sessionInfo()
```

Using Help

To open the \mathbf{R} 's help page for some command, say, for the sum command, you can use on of the following options:

?sum

or

help(sum)

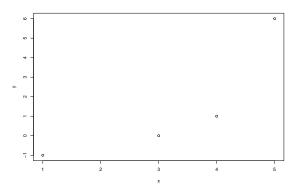
or, in **R Studio**, just put the cursor at some place on the word sum and hit F1. Anothe method is just to use the Google $\ddot{-}$

Here we will use the default package for plots⁴.

⁴More you can get using the ggplot2 package

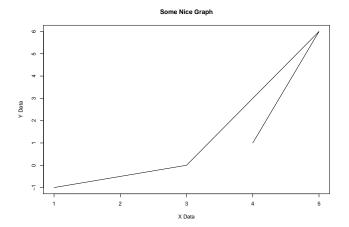
Here we will use the default package for plots⁴. First, let us plot some points (x_i, y_i) , i = 1, ..., n:

```
x \leftarrow c(1,3,5,4); y \leftarrow c(-1, 0,6, 1)
plot(x,y)
```



⁴More you can get using the ggplot2 package

Now, we join the points with line segments, add a title and axis labels to our graph:



Comments:

- type is the type of the plot. type="1" means that the type is set to lines. Try without the type parameter, or by type = "h", type = "s"
- main is the title of the graph
- xlab and ylab are the axis labels (names)

In **R**, we have low-level and high-level graphical commands. The plot command is a low-level plot. If you will use 2 plot commands one after another, the last command will draw on a new canvas. So if you want to draw two graphs one over anoher, you cannot just use two plot commands consecutively.

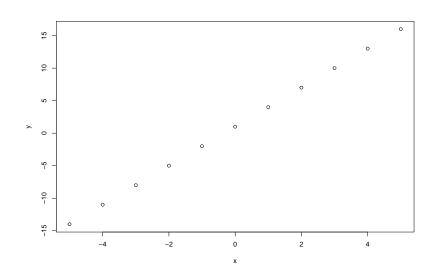
 $^{^{5}}$ In fact, in **R Studio**, under the **Plots** tab, you can navigate through the plots

In **R**, we have low-level and high-level graphical commands. The plot command is a low-level plot. If you will use 2 plot commands one after another, the last command will draw on a new canvas. So if you want to draw two graphs one over anoher, you cannot just use two plot commands consecutively. In general, when using 2 low-level graphical commands, the last one will "overwrite" the previous plot ⁵. But, when using high-level plotting commands after the low-level one, you will have the high-level plot added to the low-level one. High-level plot examples are points and lines.

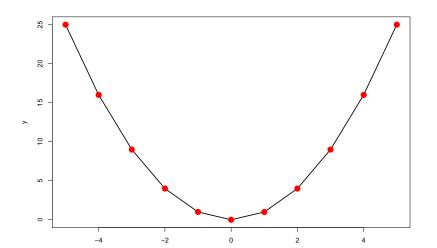
 $^{^{5}}$ In fact, in **R Studio**, under the **Plots** tab, you can navigate through the plots

Making Plots, Example $x \leftarrow -5:5$; $y \leftarrow 3*x+1$

plot(x,y)



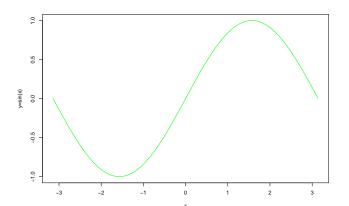
```
x <- -5:5; y <- x^2
plot(x,y, type = "1", lwd = 2)
points(x,y, pch = 16, col = "red", cex = 2)</pre>
```



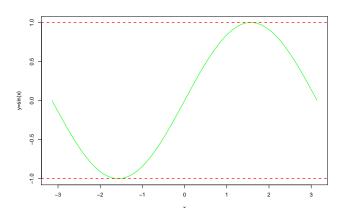
Comments:

- ▶ 1wd is the *line width*
- pch is the *point character*, try to change 16 to other integers
- col is the color
- cex is the character size, point size

Let us plot the graph of $y = \sin(x)$, $x \in [-\pi, \pi]$:



Now, let us add horizontal lines $y = \pm 1$ to previous plot:

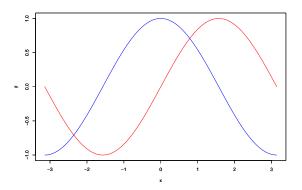


Comments:

- ▶ abline is to draw a line $y = a + b \cdot x$, you can give parameters $h = h_0$ for a horizontal line $y = h_0$ or $v = v_0$ for a vertical line $x = v_0$. abline is a high-level graphical command
- ▶ 1ty is the *line type*, try changing the values to see the difference (here we have a dotted line)

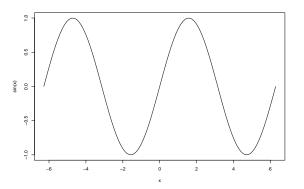
Now, let us draw two plots one over another:

```
x <- seq(from = -pi, to = pi, by = 0.01)
y <- sin(x); z <- cos(x)
plot(x,y, type = "l", lwd =1.5, col = 'red')
par(new = TRUE) #setting a parameter to keep the previous plot(x,z, type = "l", lwd =1.5, col = 'blue')</pre>
```



Another method to draw graphs is to use the curve command:

```
curve(\sin, from = -2*pi, to = 2*pi)
```



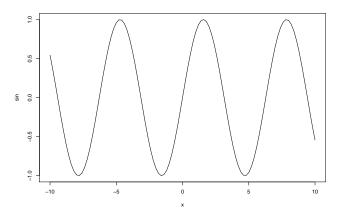
Try also⁶

```
\underline{\text{curve}(\sin(x), \text{from = }-2*pi, \text{to = }2*pi)}
```

⁶If the variable x is not defined!

Yet another method to draw graphs is to use the plot command with function name:

```
plot(sin, -10, 10)
```



It is easy to define a function in \mathbf{R} . You just need to use the following template:

```
For example, let us define the function z = x^2 + 2 * \arctan \frac{x}{x + \sin(x)}:
```

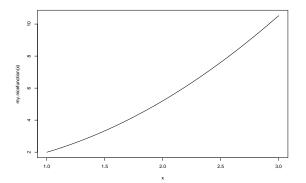
```
my.nicefunction <- function (x){
  z = x^2 +2* atan(x/(x+sin(x)))
  return(z)
}</pre>
```

Now, we can calculate our function's value at, say, the point 3, and plot its graph:

```
my.nicefunction(3)
```

```
## [1] 10.52485
```

curve(my.nicefunction, 1, 3) #or plot(my.nicefunction, 1,



Now, let us define a function of 2 variables:

```
my_fun1 <- function (x, y){
  return(x+y^2)
}</pre>
```

In this case, to calculate the value at (1,2), you just write

```
my_fun1(1,2)
```

```
## [1] 5
```

You can define also functions with default values:

```
my fun2 <- function (x, y = 0){
  return(x+y^2)
}
Now, my_fun(2) will give my_fun(2,0), and my_fun(2, 4) will
calculate my_fun(2,4):
my_fun2(2)
## [1] 2
my fun2(2,4)
## [1] 18
```

By the way, if you will give default values to each variable, like here:

```
my_fun3 <- function (x = 0, y = 0){
  return(x+y^2)
```

Then you can use the followings to calculate my fun3(2,1):

```
my_fun3(2,1)
## [1] 3
my_fun3(x = 2, y = 1)
## [1] 3
my fun3(y = 1, x = 2)
## [1] 3
```

Actually, most of the built-in ${\bf R}$ functions have named variables with default values. Say, use

You will see the help page, containing the usage of the function rnorm, in the form:

```
rnorm(n, mean = 0, sd = 1)
```

This means, that if you will use rnorm(10), it will assume mean = 0 and sd = 1. And you can mix the order of the *named* variables, say, run rnorm(10, sd = 3, mean = -1). But please note that you cannot skip the first variable, the value of n, since it has no default value!