

# Null and Alternative Hypotheses

If the original claim includes equality  $\leq$ ,  $=$ , or  $\geq$ , it is the **null hypothesis**. If the original claim does **not** include equality ( $<$ ,  $\neq$ ,  $>$ ) then the **null hypothesis** is the complement of the original claim. The **null hypothesis** always includes the **equal** sign. The decision is based on the **null hypothesis**.

## Example 1 :

A statistician read that **at least** 77% of the population oppose replacing \$1 bills with \$1 coins. To see if this claim is valid, the statistician selected a sample of 80 people and found that 55 were opposed to replacing the \$1 bills.

State the hypotheses and identify the claim.

$H_0: p \geq 0.77$  (**claim**) This is the null hypothesis since the claim had equality  
 $H_1: p < 0.77$  This is the alternative hypothesis – the complement.

## Example 2 :

YoYo Health Insurance Co. claims that in 2016, the average monthly premium paid for individual health coverage was \$283. Suppose you are suspicious that the average, or mean, cost is actually higher.

State the hypotheses and identify the claim.

$H_0: \mu = 283$  (**claim**) This is the null hypothesis since the claim had equality  
 $H_1: \mu > 283$  This is the alternative hypothesis

## Example 3 :

A local pizza shop advertises “an average delivery time of less than 20 minutes”, but it does not offer a guarantee such as a free pizza. The manager, Guido Marinara wonders if her employees are fulfilling the claim.

State the hypotheses and identify the claim

$H_0: \mu \geq 20$  This is the null hypothesis since it has equality  
 $H_1: \mu < 20$  (**claim**) This is the alternative hypothesis

1 - 13 Express the null hypothesis and the alternative hypothesis in symbolic form. Determine which is the claim. Use the correct symbol ( $\mu$ ,  $p$ ,  $\sigma$ ) for the indicated parameter.

- 1) A researcher claims that the proportion of Americans that have seen a UFO,  $p$ , is less than 3 in every one thousand.

A)  $H_0: p > 0.003$

$H_1: p \leq 0.003$  claim

C)  $H_0: p \geq 0.003$

$H_1: p < 0.003$  claim

B)  $H_0: p = 0.003$  claim

$H_1: p > 0.003$

D)  $H_0: p < 0.003$  claim

$H_1: p \geq 0.003$

- 2) A research article in an entomological journal claims that fewer than 7 in ten thousand male fireflies are unable to produce light due to a genetic mutation. Use the parameter  $p$ , the true proportion of fireflies unable to produce light.

A)  $H_0: p \geq 0.0007$

$H_1: p < 0.0007$  claim

C)  $H_0: p > 0.0007$  claim

$H_1: p \leq 0.0007$

B)  $H_0: p = 0.0007$

$H_1: p > 0.0007$  claim

D)  $H_0: p \neq 0.0007$  claim

$H_1: p \geq 0.0007$

- 3) Bedazzled Motor Company claims that its new sedan, the Glitteratti, will average better than 26 miles per gallon in the city. Use  $\mu$ , the true average mileage of the Glitteratti.

A)  $H_0: \mu \leq 26$

$H_1: \mu > 26$  claim

C)  $H_0: \mu > 26$  claim

$H_1: \mu \leq 26$

B)  $H_0: \mu < 26$

$H_1: \mu \geq 26$  claim

D)  $H_0: \mu = 26$

$H_1: \mu < 26$  claim

- 4) The owner of a soccer team claims that the average attendance at games is over 62,900, and he is therefore justified in moving the team to a city with a larger stadium.

A)  $H_0: \mu < 62,900$

$H_1: \mu \geq 62,900$  claim

C)  $H_0: \mu > 62,900$

$H_1: \mu \leq 62,900$  claim

B)  $H_0: \mu = 62,900$  claim

$H_1: \mu < 62,900$

D)  $H_0: \mu \leq 62,900$

$H_1: \mu > 62,900$  claim

5) A UFO researcher claims that more than 4.1 percent of the population have been abducted by Aliens. Use  $p$ , to determine the true percentage of the population that have been abducted by Aliens.

A)  $H_0: p \leq 4.1\%$

$H_1: p > 4.1\%$  claim

C)  $H_0: p = 4.1\%$  claim

$H_1: p < 4.1\%$

B)  $H_0: p < 4.1\%$

$H_1: p \geq 4.1\%$  claim

D)  $H_0: p > 4.1\%$  claim

$H_1: p \leq 4.1\%$

6) The manufacturer of a refrigeration system for wine produces refrigerators that are supposed to maintain a true mean temperature,  $\mu$ , of  $43^\circ\text{F}$ , ideal for a certain type of French wine. The owner of the Je T'Aime Vin winery does not agree with the refrigerator manufacturer, and claims he can prove that the true mean temperature is incorrect.

A)  $H_0: \mu \neq 43^\circ$

$H_1: \mu = 43^\circ$  claim

C)  $H_0: \mu \geq 43^\circ$  claim

$H_1: \mu < 43^\circ$

B)  $H_0: \mu \leq 43^\circ$

$H_1: \mu > 43^\circ$  claim

D)  $H_0: \mu = 43^\circ$  claim

$H_1: \mu \neq 43^\circ$

7) A researcher claims that 62% of voters in Silicon Valley are in favor of free internet for everyone.

A)  $H_0: p = 0.62$  claim

$H_1: p \neq 0.62$

C)  $H_0: p \geq 0.62$  claim

$H_1: p < 0.62$

B)  $H_0: p < 0.62$  claim

$H_1: p \geq 0.62$

D)  $H_0: p \neq 0.62$  claim

$H_1: p = 0.62$

8) The principal of a middle school claims that test scores of the seventh-graders at her school vary less than the test scores of seventh-graders at a neighboring school, which have variation described by  $\sigma = 14.7$ .

A)  $H_0: \sigma = 14.7$  claim

$H_1: \sigma \neq 14.7$

C)  $H_0: \sigma > 14.7$

$H_1: \sigma \leq 14.7$  claim

B)  $H_0: \sigma < 14.7$

$H_1: \sigma > 14.7$  claim

D)  $H_0: \sigma < 14.7$  claim

$H_1: \sigma \geq 14.7$

9) Ole Chips and Salsa Company claims that the mean weight of their medium size bag of tortilla chips is at least 14 oz.

A)  $H_0: \mu > 14$  claim

$H_1: \mu \leq 14$

B)  $H_0: \mu < 14$

$H_1: \mu \geq 14$  claim

C)  $H_0: \mu \geq 14$  claim

$H_1: \mu < 14$

D)  $H_0: \mu = 14$  claim

$H_1: \mu > 14$

10) An automobile insurance company, Regressive, claims that more than 3.3 percent of the population lie on their applications. Use  $p$ , the true percentage of the population that lie on their applications.

A)  $H_0: p = 3.3\%$

$H_1: p \neq 3.3\%$  claim

C)  $H_0: p > 3.3\%$  claim

$H_1: p \leq 3.3\%$

B)  $H_0: p < 3.3\%$

$H_1: p \geq 3.3\%$  claim

D)  $H_0: p \leq 3.3\%$

$H_1: p > 3.3\%$  claim

11) A chocolate researcher claims that the proportion of Americans that dislike chocolate,  $p$ , is less than 2 in every one thousand.

A)  $H_0: p \leq 0.002$  claim

$H_1: p > 0.002$

C)  $H_0: p < 0.002$  claim

$H_1: p \geq 0.002$

B)  $H_0: p \geq 0.002$

$H_1: p < 0.002$  claim

D)  $H_0: p > 0.002$

$H_1: p \leq 0.002$  claim

12) A coffee company claims that the mean price of an order at one of its airport shops, Starcups is at least \$14.

A)  $H_0: \mu > 14$  claim

$H_1: \mu \leq 14$

B)  $H_0: \mu \geq 14$  claim

$H_1: \mu < 14$

C)  $H_0: \mu = 14$

$H_1: \mu \neq 14$  claim

D)  $H_0: \mu < 14$

$H_1: \mu \geq 14$  claim

13) An ice cream sundae researcher claims that the amount of hot fudge pumped out of the automatic hot fudge machine has a standard deviation different from the  $\sigma = 3.3$  oz claimed by the manufacturer.

A)  $H_0: \sigma \leq 3.3$  oz

$H_1: \sigma > 3.3$  oz claim

C)  $H_0: \sigma \neq 3.3$  oz claim

$H_1: \sigma = 3.3$  oz

B)  $H_0: \sigma \geq 3.3$  oz claim

$H_1: \sigma < 3.3$  oz

D)  $H_0: \sigma = 3.3$  oz

$H_1: \sigma \neq 3.3$  oz claim

14) Which of the following would be an appropriate null hypothesis?

I. The mean of a population is equal to 55.

II. The mean of a sample is equal to 55.

III. The mean of a population is greater than 55.

A) I only

C) II only

B) III only

D) Only I and III are appropriate.

- 15) Which of the following would be an appropriate null hypothesis?
- A) The sample proportion is no less than 0.65.
  - B) The population proportion is less than 0.65.
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**Answer Key**  
**INTRO TO HYPOTHESIS TEST**

- 1) C
- 2) A
- 3) A
- 4) D
- 5) A
- 6) D
- 7) A
- 8) D
- 9) C
- 10) D
- 11) B
- 12) B
- 13) D
- 14) A
- 15) D
- 16) B
- 17) B

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- 2) A research article in an entomological journal claims that fewer than 7 in ten thousand male fireflies are unable to produce light due to a genetic mutation. Use the parameter  $p$ , the true proportion of fireflies unable to produce light.
- 3) Bedazzled Motor Company claims that its new sedan, the Glitteratti, will average better than 26 miles per gallon in the city. Use  $\mu$ , the true average mileage of the Glitteratti.
- 4) The owner of a soccer team claims that the average attendance at games is over 62,900, and he is therefore justified in moving the team to a city with a larger stadium.
- 5) A UFO researcher claims that more than 4.1 percent of the population have been abducted by Aliens. Use  $p$ , to determine the true percentage of the population that have been abducted by Aliens.
- 6) The manufacturer of a refrigeration system for wine produces refrigerators that are supposed to maintain a true mean temperature,  $\mu$ , of 43°F, ideal for a certain type of French wine. The owner of the Je T'Aime Vin winery does not agree with the refrigerator manufacturer, and claims he can prove that the true mean temperature is incorrect.
- 7) A researcher claims that 62% of voters in Silicon Valley are in favor of free internet for everyone.
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- 10) An automobile insurance company, Regressive, claims that more than 3.3 percent of the population lie on their applications. Use  $p$ , the true percentage of the population that lie on their applications.
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## Answer Key

### INTRO TO HYPOTHESIS TEST FREE RESPONSE

- 1)  $H_0: p \geq 0.003$   
 $H_1: p < 0.003$  claim
- 2)  $H_0: p \geq 0.0007$   
 $H_1: p < 0.0007$  claim
- 3)  $H_0: \mu \leq 26$   
 $H_1: \mu > 26$  claim
- 4)  $H_0: \mu \leq 62,900$   
 $H_1: \mu > 62,900$  claim
- 5)  $H_0: p \leq 4.1\%$   
 $H_1: p > 4.1\%$  claim
- 6)  $H_0: \mu = 43^\circ$  claim  
 $H_1: \mu \neq 43^\circ$
- 7)  $H_0: p = 0.62$  claim  
 $H_1: p \neq 0.62$
- 8)  $H_0: \sigma < 14.7$  claim  
 $H_1: \sigma \geq 14.7$
- 9)  $H_0: \mu \geq 14$  claim  
 $H_1: \mu < 14$
- 10)  $H_0: p \leq 3.3\%$   
 $H_1: p > 3.3\%$  claim
- 11)  $H_0: p \geq 0.002$   
 $H_1: p < 0.002$  claim
- 12)  $H_0: \mu \geq 14$  claim  
 $H_1: \mu < 14$
- 13)  $H_0: \sigma = 3.3$  oz  
 $H_1: \sigma \neq 3.3$  oz claim
- 14) A
- 15) D
- 16) B
- 17) B

# Null and Alternative Hypotheses

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A statistician read that **at least** 77% of the population oppose replacing \$1 bills with \$1 coins. To see if this claim is valid, the statistician selected a sample of 80 people and found that 55 were opposed to replacing the \$1 bills.

State the hypotheses and identify the claim.

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## Example 3 :

A local pizza shop advertises “an average delivery time of less than 20 minutes”, but it does not offer a guarantee such as a free pizza. The manager, Guido Marinara wonders if her employees are fulfilling the claim.

State the hypotheses and identify the claim

$H_0: \mu \geq 20$  This is the null hypothesis since it has equality  
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- 1) A researcher claims that the proportion of Americans that have seen a UFO,  $p$ , is less than 3 in every one thousand.

A)  $H_0: p > 0.003$

$H_A: p \leq 0.003$  claim

C)  $H_0: p \geq 0.003$

$H_A: p < 0.003$  claim

B)  $H_0: p = 0.003$  claim

$H_A: p > 0.003$

D)  $H_0: p < 0.003$  claim

$H_A: p \geq 0.003$

- 2) A research article in an entomological journal claims that fewer than 7 in ten thousand male fireflies are unable to produce light due to a genetic mutation. Use the parameter  $p$ , the true proportion of fireflies unable to produce light.

A)  $H_0: p \geq 0.0007$

$H_A: p < 0.0007$  claim

C)  $H_0: p > 0.0007$  claim

$H_A: p \leq 0.0007$

B)  $H_0: p = 0.0007$

$H_A: p > 0.0007$  claim

D)  $H_0: p \neq 0.0007$  claim

$H_A: p \geq 0.0007$

- 3) Bedazzled Motor Company claims that its new sedan, the Glitteratti, will average better than 26 miles per gallon in the city. Use  $\mu$ , the true average mileage of the Glitteratti.

A)  $H_0: \mu \leq 26$

$H_A: \mu > 26$  claim

C)  $H_0: \mu > 26$  claim

$H_A: \mu \leq 26$

B)  $H_0: \mu < 26$

$H_A: \mu \geq 26$  claim

D)  $H_0: \mu = 26$

$H_A: \mu < 26$  claim

- 4) The owner of a soccer team claims that the average attendance at games is over 62,900, and he is therefore justified in moving the team to a city with a larger stadium.

A)  $H_0: \mu < 62,900$

$H_A: \mu \geq 62,900$  claim

C)  $H_0: \mu > 62,900$

$H_A: \mu \leq 62,900$  claim

B)  $H_0: \mu = 62,900$  claim

$H_A: \mu < 62,900$

D)  $H_0: \mu \leq 62,900$

$H_A: \mu > 62,900$  claim

5) A UFO researcher claims that more than 4.1 percent of the population have been abducted by Aliens. Use  $p$ , to determine the true percentage of the population that have been abducted by Aliens.

A)  $H_0: p \leq 4.1\%$

$H_A: p > 4.1\%$  claim

C)  $H_0: p = 4.1\%$  claim

$H_A: p < 4.1\%$

B)  $H_0: p < 4.1\%$

$H_A: p \geq 4.1\%$  claim

D)  $H_0: p > 4.1\%$  claim

$H_A: p \leq 4.1\%$

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A)  $H_0: \mu \neq 43^\circ$

$H_A: \mu = 43^\circ$  claim

C)  $H_0: \mu \geq 43^\circ$  claim

$H_A: \mu < 43^\circ$

B)  $H_0: \mu \leq 43^\circ$

$H_A: \mu > 43^\circ$  claim

D)  $H_0: \mu = 43^\circ$  claim

$H_A: \mu \neq 43^\circ$

7) A researcher claims that 62% of voters in Silicon Valley are in favor of free internet for everyone.

A)  $H_0: p = 0.62$  claim

$H_A: p \neq 0.62$

C)  $H_0: p \geq 0.62$  claim

$H_A: p < 0.62$

B)  $H_0: p < 0.62$  claim

$H_A: p \geq 0.62$

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$H_A: \sigma > 14.7$  claim

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$H_A: \mu \geq 14$  claim

C)  $H_0: \mu \geq 14$  claim

$H_A: \mu < 14$

D)  $H_0: \mu = 14$  claim

$H_A: \mu > 14$

10) An automobile insurance company, Regressive, claims that more than 3.3 percent of the population lie on their applications. Use  $p$ , the true percentage of the population that lie on their applications.

A)  $H_0: p = 3.3\%$

$H_A: p \neq 3.3\%$  claim

C)  $H_0: p > 3.3\%$  claim

$H_A: p \leq 3.3\%$

B)  $H_0: p < 3.3\%$

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A)  $H_0: p \leq 0.002$  claim

$H_A: p > 0.002$

C)  $H_0: p < 0.002$  claim

$H_A: p \geq 0.002$

B)  $H_0: p \geq 0.002$

$H_A: p < 0.002$  claim

D)  $H_0: p > 0.002$

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12) A coffee company claims that the mean price of an order at one of its airport shops, Starcups is at least \$14.

A)  $H_0: \mu > 14$  claim

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B)  $H_0: \mu \geq 14$  claim

$H_A: \mu < 14$

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A)  $H_0: \sigma \leq 3.3$  oz

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$H_A: \sigma < 3.3$  oz

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$H_A: \sigma \neq 3.3$  oz claim

14) Which of the following would be an appropriate null hypothesis?

I. The mean of a population is equal to 55.

II. The mean of a sample is equal to 55.

III. The mean of a population is greater than 55.

A) I only

C) II only

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D) Only I and III are appropriate.

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**Answer Key**  
**INTRO TO HYPOTHESIS TEST**

- 1) C
- 2) A
- 3) A
- 4) D
- 5) A
- 6) D
- 7) A
- 8) D
- 9) C
- 10) D
- 11) B
- 12) B
- 13) D
- 14) A
- 15) D
- 16) B
- 17) B

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- 4) The owner of a soccer team claims that the average attendance at games is over 62,900, and he is therefore justified in moving the team to a city with a larger stadium.
- 5) A UFO researcher claims that more than 4.1 percent of the population have been abducted by Aliens. Use  $p$ , to determine the true percentage of the population that have been abducted by Aliens.
- 6) The manufacturer of a refrigeration system for wine produces refrigerators that are supposed to maintain a true mean temperature,  $\mu$ , of 43°F, ideal for a certain type of French wine. The owner of the Je T'Aime Vin winery does not agree with the refrigerator manufacturer, and claims he can prove that the true mean temperature is incorrect.
- 7) A researcher claims that 62% of voters in Silicon Valley are in favor of free internet for everyone.
- 8) The principal of a middle school claims that test scores of the seventh-graders at her school vary less than the test scores of seventh-graders at a neighboring school, which have variation described by  $\sigma = 14.7$ .
- 9) Ole Chips and Salsa Company claims that the mean weight of their medium size bag of tortilla chips is at least 14 oz.



- 10) An automobile insurance company, Regressive, claims that more than 3.3 percent of the population lie on their applications. Use  $p$ , the true percentage of the population that lie on their applications.
- 11) A chocolate researcher claims that the proportion of Americans that dislike chocolate,  $p$ , is less than 2 in every one thousand.
- 12) A coffee company claims that the mean price of an order at one of its airport shops, Starcups is at least \$14.
- 13) An ice cream sundae researcher claims that the amount of hot fudge pumped out of the automatic hot fudge machine has a standard deviation different from the  $\sigma = 3.3$  oz claimed by the manufacturer.
- 14) Which of the following would be an appropriate null hypothesis?
  - I. The mean of a population is equal to 55.
  - II. The mean of a sample is equal to 55.
  - III. The mean of a population is greater than 55.

A) I only  
B) III only  
C) II only  
D) Only I and III are appropriate.
- 15) Which of the following would be an appropriate null hypothesis?
  - A) The sample proportion is no less than 0.65.
  - B) The population proportion is less than 0.65.
  - C) The sample proportion is less than 0.65.
  - D) The population proportion is not less than 0.65.
- 16) Which of the following would be an appropriate alternative hypothesis?
  - A) The mean of a population is equal to 55.
  - B) The mean of a population is greater than 55.
  - C) The mean of a sample is equal to 55.
  - D) The mean of a sample is greater than 55.
- 17) Which of the following would be an appropriate alternative hypothesis?
  - A) The sample proportion is less than 0.65.
  - B) The population proportion is less than 0.65.
  - C) The sample proportion is not less than 0.65.
  - D) The population proportion is not less than 0.65.

## Answer Key

### INTRO TO HYPOTHESIS TEST FREE RESPONSE

- 1)  $H_0: p \geq 0.003$   
 $H_A: p < 0.003$  claim
- 2)  $H_0: p \geq 0.0007$   
 $H_A: p < 0.0007$  claim
- 3)  $H_0: \mu \leq 26$   
 $H_A: \mu > 26$  claim
- 4)  $H_0: \mu \leq 62,900$   
 $H_A: \mu > 62,900$  claim
- 5)  $H_0: p \leq 4.1\%$   
 $H_A: p > 4.1\%$  claim
- 6)  $H_0: \mu = 43^\circ$  claim  $H_1: \mu \neq 43^\circ$
- 7)  $H_0: p = 0.62$  claim  $H_1: p \neq 0.62$
- 8)  $H_0: \sigma < 14.7$  claim  $H_1: \sigma \geq 14.7$
- 9)  $H_0: \mu \geq 14$  claim  $H_1: \mu < 14$
- 10)  $H_0: p \leq 3.3\%$   
 $H_A: p > 3.3\%$  claim
- 11)  $H_0: p \geq 0.002$   
 $H_A: p < 0.002$  claim
- 12)  $H_0: \mu \geq 14$  claim  $H_1: \mu < 14$
- 13)  $H_0: \sigma = 3.3$  oz  
 $H_A: \sigma \neq 3.3$  oz claim
- 14) A
- 15) D
- 16) B
- 17) B