

## Homework 3 - Problem 1

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```
clear;clc;
% Setup portion
% Define necessary link parameters and link table
syms m1 m2 L1 L2 theta1 thetaDot_1 thetaDotDot_1 theta2 thetaDot_2 thetaDotDot_2 g;
linkTable = [0 0 0 theta1; pi/2 L1 0 theta2; 0 L2 0 0];

% Generate transforms from link table
T01 = functions.links.Link2Transform(linkTable(1,:));
T12 = functions.links.Link2Transform(linkTable(2,:));
T23 = functions.links.Link2Transform(linkTable(3,:));
T03 = functions.links.Link2Transform(linkTable);

% Pull and define rotations from transforms
R01 = functions.transform.rotationFromTransform(T01);
R12 = functions.transform.rotationFromTransform(T12);
R23 = functions.transform.rotationFromTransform(T23);

% Define position, centroid, inertial, and initial angular velocity/accel vectors
P_01 = [0 0 0];
P_12 = L1*[1 0 0];
Pc_11 = L1*[1 0 0].';
Pc_22 = L2*[1 0 0].';
Ic_11 = 0;
Ic_22 = 0;
w_0 = 0;
wDot_0 = 0;
v0_dot = [0 0 g].';

% Velocity Propagation:
% Define velocity conditions at first joint
w_11 = functions.dynamics.omega_ip1ip1(R01.',w_0,thetaDot_1);
wDot_11 = functions.dynamics.omegaDot_ip1ip1(R01.',wDot_0,w_0,thetaDot_1,thetaDotDot_1);
vDot_11 = functions.dynamics.vDot_ip1ip1(R01.',wDot_0,P_01,w_11,v0_dot);
vcDot_11 = functions.dynamics.vcDot_ip1ip1(wDot_11,Pc_11,w_11,vDot_11);

% Define force and torque conditions at first joint
F_11 = functions.dynamics.F_ip1ip1(m1,vcDot_11);
N_11 = functions.dynamics.N_ip1ip1(wDot_11,w_11,Ic_11);

% Define velocity conditions at second joint
w_22 = functions.dynamics.omega_ip1ip1(R12.',w_11,thetaDot_2);
wDot_22 = functions.dynamics.omegaDot_ip1ip1(R12.',wDot_11,w_11,thetaDot_2,thetaDotDot_2);
vDot_22 = functions.dynamics.vDot_ip1ip1(R12.',wDot_11,P_12,w_11,vDot_11);
vcDot_22 = functions.dynamics.vcDot_ip1ip1(wDot_22,Pc_22,w_22,vDot_22);

% Define force and torque conditions at second joint
F_22 = functions.dynamics.F_ip1ip1(m2,vcDot_22);
N_22 = functions.dynamics.N_ip1ip1(wDot_22,w_22,Ic_22);

% Force Propagation:
% Summarize force and torque conditions at second joint
f_22 = F_22;
n_22 = functions.dynamics.n_ii(N_22,R23,0,Pc_22,F_22,Pc_22,0);
tau_2 = functions.dynamics.tau_i(n_22);

% Summarize force and torque conditions at first joint
f_11 = functions.dynamics.f_ii(R12,f_22,F_11);
n_11 = functions.dynamics.n_ii(N_11,R12,n_22,Pc_11,F_11,P_12,0);
tau_1 = functions.dynamics.tau_i(n_11);

% Cleanup tau_1 and tau_2 and display
syms c1 c2 s1 s2;
tau_1 = subs(tau_1,[cos(theta1),cos(theta2),sin(theta1),sin(theta2)], [c1,c2,s1,s2]);
tau_2 = subs(tau_2,[cos(theta1),cos(theta2),sin(theta1),sin(theta2)], [c1,c2,s1,s2]);
display(tau_1);
display(tau_2);
```

$\tau_1 =$

$$L_1^2 m_1 \ddot{\theta}_1 + L_2 c_2 m_2 (L_1 \ddot{\theta}_1 + L_2 (c_2 \ddot{\theta}_1 - s_2 \dot{\theta}_1 \dot{\theta}_2) - L_2 s_2 \dot{\theta}_1 \dot{\theta}_2)$$

$\tau_2 =$

$$L_2 m_2 (L_2 \ddot{\theta}_2 + c_2 g + L_1 s_2 \dot{\theta}_1^2 + L_2 c_2 s_2 \dot{\theta}_1^2)$$