

## Homework 3 - Problem 2

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clear;clc;

% Setup Portion
% Dynamic equations using Newton-Euler formulation
syms d_2 dDot_2 dDotDot_2 theta1 thetaDot_1 thetaDotDot_1 theta2 thetaDot_2 thetaDotDot_2 g Ixx_1 Iyy_1 Izz_1 m1 m2;
linkTable = [0 0 0 theta1; -pi/2 0 d_2 0];

% Define transforms for each link from table
T01 = functions.links.Link2Transform(linkTable(1,:));
T12 = functions.links.Link2Transform(linkTable(2,:));

% Pull and define rotations from transforms
R01 = functions.transform.rotationFromTransform(T01);
R12 = functions.transform.rotationFromTransform(T12);

% Define position, centroid, inertial, and initial angular velocity/accel vectors
P_01 = functions.transform.positionFromTransform(T01);
P_12 = functions.transform.positionFromTransform(T12);
Pc_11 = [0 0 0].';
Pc_22 = [0 0 0].';
Ic_11 = [Ixx_1 0 0; 0 Iyy_1 0; 0 0 Izz_1];
Ic_22 = 0;
w_0 = 0;
wDot_0 = 0;
v0_dot = [0 0 g].';

% Velocity Propagation:
% Define velocity conditions at first joint
w_11 = functions.dynamics.omega_ip1ip1(R01.',w_0,thetaDot_1);
wDot_11 = functions.dynamics.omegaDot_ip1ip1(R01.',wDot_0,w_0,thetaDot_1,thetaDotDot_1);
vDot_11 = functions.dynamics.vDot_ip1ip1(R01.',wDot_0,P_01,w_11,v0_dot);
vcDot_11 = functions.dynamics.vcDot_ip1ip1(wDot_11,Pc_11,w_11,vDot_11);

% Define force and torque conditions at first joint
F_11 = functions.dynamics.F_ip1ip1(m1,vcDot_11);
N_11 = functions.dynamics.N_ip1ip1(wDot_11,w_11,Ic_11);

% Define velocity conditions at second joint
w_22 = functions.dynamics.omega_ip1ip1(R12.',w_11,0);
wDot_22 = functions.dynamics.omegaDot_ip1ip1(R12.',wDot_11,w_11,0,0);
vDot_22 = functions.dynamics.vDot_ip1ip1_prism(R12.',wDot_11,P_12,w_11,vDot_11,w_22,dDot_2,dDotDot_2);
vcDot_22 = functions.dynamics.vcDot_ip1ip1(wDot_22,Pc_22,w_22,vDot_22);

% Define force and torque conditions at second joint
F_22 = functions.dynamics.F_ip1ip1(m2,vcDot_22);
N_22 = functions.dynamics.N_ip1ip1(wDot_22,w_22,Ic_22);

% Force Propagation:
% Summarize force and torque conditions at second joint
f_22 = F_22;
n_22 = functions.dynamics.n_ii(N_22,0,0,Pc_22,F_22,Pc_22,0);
tau_2 = functions.dynamics.tau_i(f_22);

% Summarize force and torque conditions at first joint
f_11 = functions.dynamics.f_ii(R12,f_22,F_11);
n_11 = functions.dynamics.n_ii(N_11,R12,n_22,Pc_11,F_11,P_12,F_22);
tau_1 = functions.dynamics.tau_i(n_11);

% Cleanup tau_1 and tau_2
syms c1 c2 s1 s2;
tau_1 = subs(tau_1,[cos(theta1),cos(theta2),sin(theta1),sin(theta2)], [c1,c2,s1,s2]);
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tau_2 = subs(tau_2,[cos(theta1),cos(theta2),sin(theta1),sin(theta2)],[c1,c2,s1,s2]);  
display(tau_1);  
display(tau_2);
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tau\_1 =

$I_{zz\_1} \ddot{\theta}_1 + d_2 m_2 (2 \dot{d}_2 \dot{\theta}_1 + d_2 \ddot{\theta}_1)$

tau\_2 =

$m_2 (-d_2 \dot{\theta}_1^2 + \ddot{d}_2)$