

$$V_a(t) = R_a i_a(t) + L \frac{di_a(t)}{dt} + V_e(t)$$

$$V_e(t) = K_b \cdot \Omega_m$$

$$T(t) = J_m \ddot{\theta}_m + B_m \dot{\theta}_m \quad ; \quad T(t) = K_t i_a(t)$$

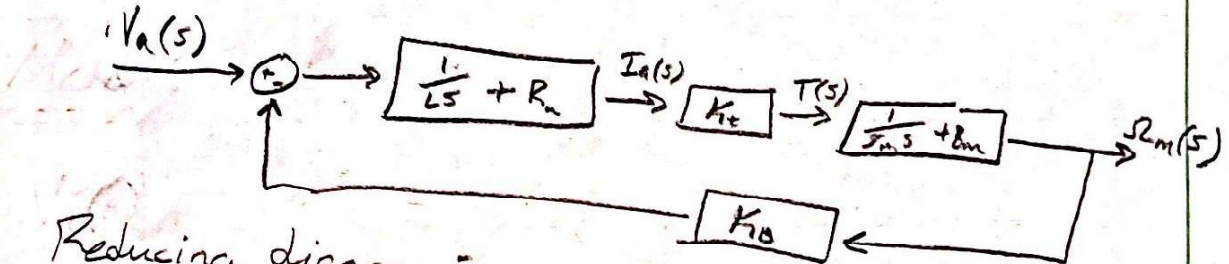
Laplace:  $V_a(s) = R_a i_a(s) + L s i_a(s) + V_e(s)$

$$V_a(s) = (Ls + R_a) i_a(s) + V_e(s) \quad ; \quad V_e(s) = K_b \cdot \Omega_m(s)$$

$$T(s) = (J_m s + B_m) \Omega_m(s) \quad ; \quad T(s) = K_t i_a(s)$$

$$\Omega_m(s) = \frac{T(s)}{J_m s + B_m}$$

Model:



Reducing diagram:

$$G(s) = \left[ \frac{1}{Ls + R_a} \right] \cdot K_t \cdot \left[ \frac{1}{J_m s + B_m} \right] H(s) = K_b$$

$$\frac{\Omega(s)}{V_a(s)} = \frac{K_t}{(Ls + R_a)(J_m s + B_m)} \cdot \frac{1}{1 + \frac{K_t K_b}{(Ls + R_a)(J_m s + B_m)}} = \frac{K_t}{(Ls + R_a)(J_m s + B_m) + K_t K_b}$$

$$\frac{\Omega(s)}{V_a(s)} = \frac{K_t}{(2 \cdot J_m) s^2 + (R_a \cdot J_m + B_m \cdot L) s + (K_t K_b + R_a B_m)}$$