USACO NOV08 Problem 'buyhay' Analysis

by Neal Wu

This problem is a typical knapsack problem and can be solved using dynamic programming. We keep an array called best [] such that best [h] is the minimum cost possible to obtain exactly h pounds of hay. For each supplier given, we do a simple traversal from 0 to H to update the values in the array. In particular, if (best [i] + the cost of one package) is better than best [i + the weight of one package], we update this value accordingly.

At the end, our answer is simply the minimum cost of any value in the array that is at position H or after. Since our algorithm does H iterations for each of the N suppliers, our overall runtime is O(NH).

The following is a sample solution:

```
#include <cstdio>
#include <cstring>
using namespace std;
FILE *fout = fopen ("buyhay.out", "w");
FILE *fin = fopen ("buyhay.in", "r");
const int INF = 10000000000;
const int MAXH = 60005;
int N, H, P, C;
int best [MAXH];
int ans = INF;
int main ()
// initialize to infinity
   memset (best, 63, sizeof (best));
   best [0] = 0;
    fscanf (fin, "%d %d", &N, &H);
    while (N--)
        fscanf (fin, "%d %d\n", &P, &C);
// update values in the array; only necessary to go up to {\tt H}
       for (int i = 0; i < H; i++)
            if (best [i] + C < best [i + P])
                best [i + P] = best [i] + C;
    }
// find best cost for any amount that is at least H
    for (int i = H; i < MAXH; i++)
        if (best [i] < ans)
            ans = best [i];
    fprintf (fout, "%d\n", ans);
    return 0;
}
```