

# Hashing

int a[N]  
"avichal" 5

"abcde"

basic hash  $a \cdot 30^4 + b \cdot 30^3 + c \cdot 30^2 + d \cdot 30^1 + e$

polynomial hash

String S 
$$h(S) = \sum_{i=0}^{n-1} S[i] * b^{n-i-1} \% P$$

abcdeedcba  $N \leq 10^5$   
 $\underbrace{\hspace{1.5cm}}_{(1,1)}$   
 $\underbrace{\hspace{1.5cm}}_{(1,1)}$

mods in division

$73 \cdot b^2 \% 13$

$5 \cdot b^2$

$5 / 73 \neq 73$

$h[l] = d \cdot b^5 + e \cdot b^4 + d \cdot b^3$

$+ c \cdot b^2 + b \cdot b + a \cdot b$

$h[r] = c \cdot b^2 + b \cdot b + a \cdot b$

$h[l] - h[r] \text{ NOT POSSIBLE}$

$\frac{h[l] - h[r]}{r - l}$

$a^{p-1} \equiv 1 \pmod{p}$

POSSIBLE:

$a \cdot a^{p-2} \equiv 1 \pmod{p}$

$(h[l] - h[r]) \cdot a^{p-2}$

$(h[l] - h[r]) \pmod{p}$

if you want to divide by x,  
multiply by  $x^{p-2} \pmod{p}$

# Hashing

$$x^{100} = ? \quad \text{Let's say we know } x^{50} = 4$$

$$\therefore x^{100} = 16. \quad \text{Now what if } x^{50} = ?$$

$$x^{25} = ? \quad x^{12} = 4$$

$$x^{12} \cdot x^{12} \cdot x = x^{25}$$

$$O(\log b) \quad a^b \bmod p$$

$$a^{\frac{b}{2}} \text{ multiplied by } a \text{ if } b \% 2 == 1$$

Use or compare something more easily

$$A \cdot B \bmod C \equiv 1$$

B is inv mod of A

# Suffix Arrays

" " " "  
no char < a

5	avichal	a*****
0	vichal	avichal
3	ichal	chal...
4	chal	hal...
2	hal	ichal...
6	a	l...
1		vichal...

0 1 2 3 4 5 6

avichal\*\*\*\*\*

sa[i][k]

rank of

compare(a, b)

length 1

substring starting at i

return s[a] < s[b]

length  $2^k$

compare(a, b)

length 2

if (s[a] == s[b])

return s[a+1] < s[b+1]

else return s[a] < s[b]

for any power of 2

compare(a, b, k) length 2

if (s[a...a+2<sup>k-1</sup>] == s[b...b+2<sup>k-1</sup>])

look at 2<sup>nd</sup> half [a+2<sup>k-1</sup>...a+2<sup>k</sup>]

if length of suffix array is

not power of two, add \*\*\*

to balance

(-1 considered)