

CSC411 - Project #3

Yui Chit (Michael) Wong - 999806232
Yijin (Catherine) Wang - 998350476

March 21, 2017

Part 1

Question Describe the datasets. You will be predicting whether the review is positive or negative from keywords that appear in the review. Is that feasible? Give 3 examples of specific keywords that may be useful, together with statistics on how often they appear in positive and negative reviews.

Answer It is feasible. The word "best" appears in 489 positive reviews and 365 negative reviews. The word "horrendous" appears in 3 positive reviews and 9 negative reviews. The word "awful" appears in 19 positive reviews and 103 negative reviews. Therefore, "best" could be useful to identify positive review, while "horrendous" and "awful" could be used to identify negative review. (There are 1000 positive reviews and 1000 negative reviews in total.)

Part 2

Question Implement the Naive Bayes algorithm for predicting whether the review is positive or negative. Tune the parameter m using the validation set, and report how you did it and what was the result. Report the performance on the training and the test sets that you obtain. Note that computing products of many small numbers leads to underflow. Use the fact that $a_1 a_2 \cdots a_n = \exp(\log a_1 + \log a_2 + \cdots \log a_n)$. In your report, explain how you used that fact.

Answer In order to predict the review, we use the formula:

$$P(class|a_1, \dots, a_n) = \frac{P(a_1, \dots, a_n|class)P(class)}{P(a_1, \dots, a_n)}$$

If $P(positive|a_1, \dots, a_n) \geq P(negative|a_1, \dots, a_n)$, we predict the review to be positive. Otherwise, we predict the review to be negative. Because $P(a_1, \dots, a_n)$ is the same for $P(positive|a_1, \dots, a_n)$ and $P(negative|a_1, \dots, a_n)$, we only need to compare $P(a_1, \dots, a_n|positive)P(positive)$ and $P(a_1, \dots, a_n|negative)P(negative)$.

$$\begin{aligned} P(a_1, \dots, a_n|class)P(class) &= P(a_1|class)P(a_2|class) \cdots P(a_n|class)P(class) \\ &= \exp(\log(P(a_1|class)) + \cdots + \log(P(a_n|class)) + \log(P(class))) \end{aligned}$$

Based on the formula above, we only need to compare $\log(P(a_1|positive)) + \cdots + \log(P(a_n|positive)) + \log(P(positive))$ and $\log(P(a_1|negative)) + \cdots + \log(P(a_n|negative)) + \log(P(negative))$. Therefore, we implemented our part 2 python program based on the comparison.

Part 3

Question List the 10 words that most strongly predict that the review is positive, and the 10 words that most strongly predict that the review is negative. State how you obtained those in terms of the conditional probabilities used in the Naive Bayes algorithm.

Answer

$$P(class|a_i) = \frac{P(a_i|class)P(class)}{P(a_i)}$$
$$P(class|a_i) = \exp(\log(P(a_i|class)) + \log(P(class)) - \log(P(a_i)))$$

We use the formula above to compute and compare $P(positive|a_i)$ for all words in positive reviews and $P(negative|a_i)$ for all words in negative reviews.

The top 10 words that predicts positive are:

'ziembicki', 'unites', 'ulu', 'torrance', 'toiling', 'ties', 'swope', 'salability', 'rothchild', 'rollergirl'

The top 10 words that predicts negative are:

'zaltar', 'workout', 'unmercifully', 'szwarc', 'stuffing', 'slunk', 'salkinds', 'refugees', 'popeye', 'omega-hedron'

Although most of the words does not make sense intuitively to make strong prediction, they showed up in the result because they only appeared in one class. For example, 'ziembicki' is only in positive reviews, 'popeye' is only in negative reviews.

Part 4

Question Train a Logistic Regression model on the same dataset. For a single movie review, For a single review r the input to the Logistic Regression model will be a k -dimensional vector v , where $v[k] = 1$ if the k -th keyword appears in the review r . The set of keywords consists of all the words that appear in all the reviews.

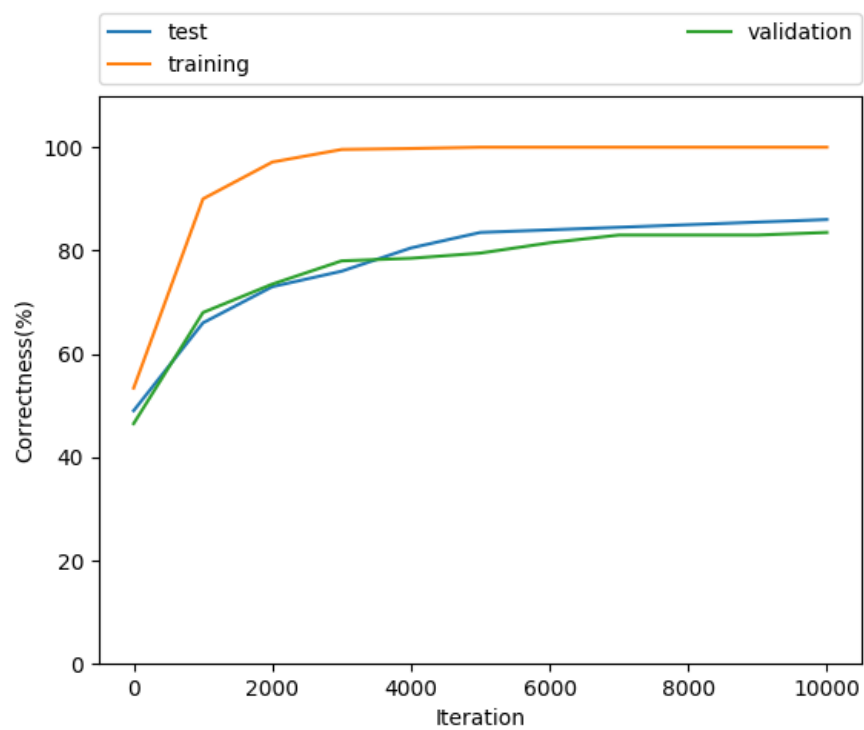
Plot the learning curves (performance vs. iteration) of the Logistic Regression model. Describe how you selected the regularization parameter (and describe the experiments you used to select it).

Answer When working on this part of the project, we first obtained the whole list of keywords from the training set (both positive and negative reviews). Then for each review in the testing and validation set, we will create a k -dimensional vector v , where $v[k] = 1$ if the k -th keyword appears in the review. If a review from the test or validation set contains a keyword that isn't in the training keyword set, it would be ignored. We then stack the vectors together to get a ' x ' for each of the training, test, and validation.

We then used the x_{train} to train the model and test the performance on x_{test}, x_{val} . We used tensorflow to implement the architecture of the model. We used one-hot encoding for the output. For the network model, we only have 1 input layer and an output layer that has sigmoid activation function. We also have a $L2$ penalty for the weight (used as regularization). The training step is done by the Adam Optimizer, which is a variant of gradient descend. Also, each iteration we will take a randomly chosen mini batch from the original training set to speed the process and avoid running into local minima.

When picking the parameter, it's done mostly by trial and error. We tested different values for the parameters, and selected the best one based on the performance on validation.

I ran the training step for 10000 iterations, and the final performance on training set and test set are 100% and 86% respectively. The result of the training vs. iteration is summarized below:



Learning curve

Part 5

Question At test time, both Logistic Regression and Naive Bayes can be formulated as computing

$$\theta_0 + \theta_1 I_1(x) + \theta_2 I_2(x) + \cdots + \theta_k I_k(x) > thr$$

in order to decide whether to classify x as 1 or 0 . Explain, in each case, what the θ s and the I s are.

Answer Assume x is one review which is a k -dimensional vector where k is the total number of unique words in the set.

$$\theta_0 = \log(P(positive)) - \log(P(negative)).$$

$I_i(x)$ is the i th word of input x . $I_i(x)$ is either 1 or 0, where 1 means that i th word is in review x , 0 means that i th word is not in review x .

$$\theta_i = \log(P(word_i|positive)) - \log(P(word_i|negative))$$

Part 6

Question Compare the top 100 θ s that you obtained using Naive Bayes and Logistic Regression.

Answer The average of θ from Naive Bayes is 0.176375, with standard deviation 0.125596.
The average of θ from logistic regression is 0.004004, with standard deviation 0.001090.

By comparing the top 100 θ s with corresponding words from Naive Bayes and Logistic Regression, we found that:

Common positive words are:
'hilarious', 'outstanding', 'terrific', 'change', 'memorable'

Common negative words are:
'bad', 'waste', 'stupid', 'nothing', 'boring'

Number of positive words from Naive Bayes = 59
Number of positive words from Logistic Regression = 40
Number of negative words from Naive Bayes = 41
Number of negative words from Logistic Regression = 60

Although not many words are in common, it is clear to see that most of the words do strongly predicts positive or negative.

Part 7

Question

Answer

Part 8

Question

Answer