Statistics 12, Lab 3

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Exercise 1

a) I ran the following code.

```
linear_model <- lm(soil$lead ~ soil$zinc)
summary(linear_model)</pre>
```

This output the following statistics.

Call:

lm(formula = soil\$lead ~ soil\$zinc)

Residuals:

```
Min 1Q Median 3Q Max -79.853 -12.945 -1.646 15.339 104.200
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 17.367688   4.344268   3.998 9.92e-05 ***
soil$zinc   0.289523   0.007296   39.681   < 2e-16 ***
```

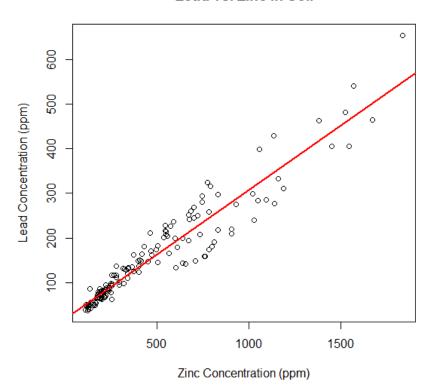
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Residual standard error: 33.24 on 153 degrees of freedom Multiple R-squared: 0.9114, Adjusted R-squared: 0.9109 F-statistic: 1575 on 1 and 153 DF, p-value: < 2.2e-16

b) I ran the following code.

This generated the following plot.

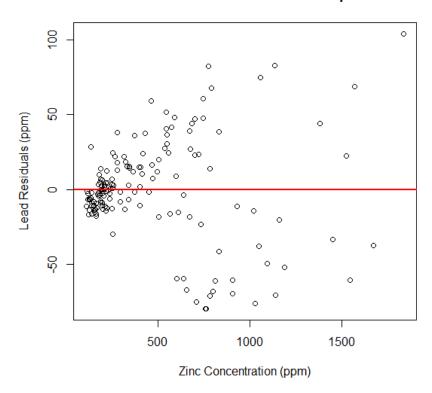
Lead vs. Zinc in Soil



c) I ran the following code

This generated the following plot.

Lead vs. Zinc in Soil Residuals plot



d) The equation of the regression line is the following.

$$y = 0.289523x + 17.367688$$

- e) We would expect the lead concentration to be 306.89 ppm.
- f) We would expect the lead concentration to be 28.95 ppm higher.
- g) The R-squared value is 0.9114. In this context it means that 91.14% of the variation in the lead concentration can be determined by the variation in zinc concentration.

h) I believe that linearity, symmetry, and are met for this data. The data appears very straight and the residuals look symmetrical. However, the condition for equal variance is not met. The residuals appear to become more spread out as the zinc concentration becomes greater. This would indicate that our model does not capture all the details of our system. Perhaps of the logarithms of both zinc and lead would be more appropriate to compare with each other.

Exercise 2

a) I ran the following code.

```
linear_model2 <- lm(ice$Extent ~ ice$Date)
summary(linear_model2)</pre>
```

This output the following statistics.

Call:

```
lm(formula = ice$Extent ~ ice$Date)
```

Residuals:

```
Min 1Q Median 3Q Max -9.445 -5.439 1.442 5.599 7.564
```

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.011e+01 1.558e+00 6.486 4.11e-10 ***
ice$Date 1.438e-04 1.411e-04 1.019 0.309
---
```

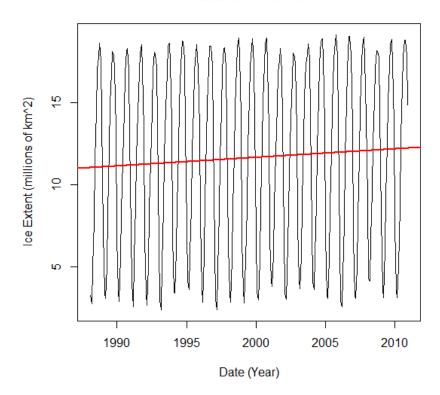
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.654 on 273 degrees of freedom Multiple R-squared: 0.003787, Adjusted R-squared: 0.0001377 F-statistic: 1.038 on 1 and 273 DF, p-value: 0.3093

b) I ran the following code.

This generated the following plot.

Ice Extent Over Time

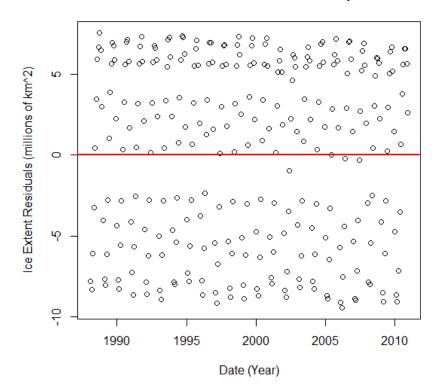


There does seem to be a slight upwards trend in this data as shown by the regression line. However, the main change in sea ice extent seems to come from the change in the seasons. The sea periodically rises and falls with a period of a year.

c) I ran the following code

This generated the following plot.

Ice Extent Over Time Residuals plot



The assumption about the model that we should be concerned about is the linearity assumption. The residuals have bands where the density changes, which indicates that our model consistently over and under predicts the sea ice extent within certain time frames. In reality the sea ice extent is probably best modeled by a sinusoidal relationship. If we want a linear model we could also take the average ice size over the year or only record the ice size during a specific season.

Exercise 3

a) There is an $\frac{8}{36}$ chance that Adam will double his money in the first round of the game and a $\frac{4}{36}$ chance that Adam will lose his money in the first round of the game.

b) I ran the following code.

```
set.seed(123)
faces = 1:6
rolls = do(5000) * sample(faces, 2, replace=TRUE)
sums = rowSums(rolls)
```

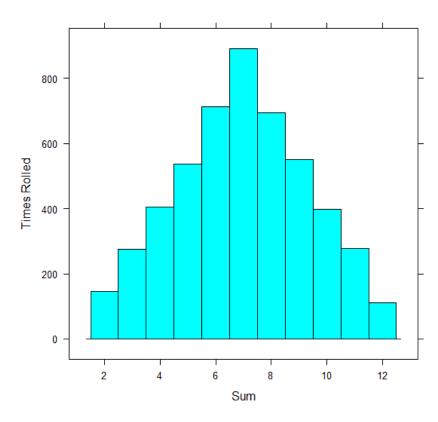
The first five sums that were generated were 9, 7, 10, 7, and 9.

c) I ran the following code.

```
histogram(sums, main="Sum of Two Fair Six-Sided Dice Rolls", xlab="Sum", ylab="Times Rolled", n=11, type="count")
```

This generated the following plot.

Sum of Two Fair Six-Sided Dice Rolls



d) I ran the following code.

```
mean(sums == 7 | sums == 11)
mean(sums == 2 | sums == 3 | sums == 12)
```

This output that Adam doubled his money 23.36% of the time in the simulation and lost his money 10.64% of the time in the simulation.

- **e)** They are mutually exclusive and not independent. This is because Adam cannot both win money and lose money on the first round at the same time. If they were independent, the probability of both events happening would be nonzero and equal to the product of the probabilities of the two independent events.
- **f)** Let's assume that event A is Adam doubling his money and event B is Adam losing his money. Assume for contradiction that A and B are independent. Then we have the following.

$$P(A \cap B) = P(A)P(B) = \frac{8}{36} \frac{4}{36} = \frac{2}{81}$$

But we know that $P(A \cap B) = 0$, a contradiction. Thus A and B are not independent.

Exercise 4

- a) We have that n = 365 and p = 0.4.
- **b)** We have the mean np = 146 and the standard deviation $\sqrt{np(1-p)} = 9.359$.
- c) I ran the following code.

```
dbinom(145, size=365, prob=0.4)
```

This output that there is a 4.239996% chance of heavy rain on exactly 145 days in 2017.

d) I ran the following code.

```
sum = 0
for (num in 125:175) {
   sum = sum + dbinom(num, size=365, prob=0.4)
}
```

This output that there is a 98.88137% chance of heavy rain on 125 to 175 days inclusive in 2017.

e) I ran the following code.

```
1-pnorm(230, mean=200, sd=20)
```

This output that there is a 6.68072% chance of the park experiencing more than 230 inches of rain in 2017.