$$f(z) = -\log z$$

$$Df(x, y) = \frac{x}{y} - \log \frac{x}{y} - 1$$

$h(z)$