# Quick Permutation Test: feature filtering of n-gram data

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#### Introduction

N-grams (k-tuples) are vectors of n characters derived from input sequence(s). They may form continuous sub-sequences or be discontinuous. Important n-gram parameter is its position. Instead of just counting n-grams, one may want to count how many n-grams occur at a given position in multiple (e.g. related) sequences.

Originally developed for natural language processing, n-grams are also used in genomics (Fang et al., 2011), transcriptomics (Wang et al., 2014) and proteomics (Guo et al., 2014).

	P1	P2	P3	P4	P5	P6
S1	4	4	4	2	1	1
S2	4	1	4	4	1	2
S3	1	2	3	2	2	1

	$P1_{-}1$	$P2_{-}1$	$P3_1$	$P4_1$	$P5_1$	$P6_1$	$P1_2$	$P2_2$	$P3_2$	$P4_2$	$P5_2$	$P6_2$	P1_3
<u>C 1</u>		<u> </u>		<u> </u>	1	1	<u> </u>			1		0	
21	U	U	U	U	Т	Т	U	U	U	Τ	U	U	0
S2	0	1	0	0	1	0	0	0	0	0	0	1	0
53		U	U	U	U	1	U		U			U	0

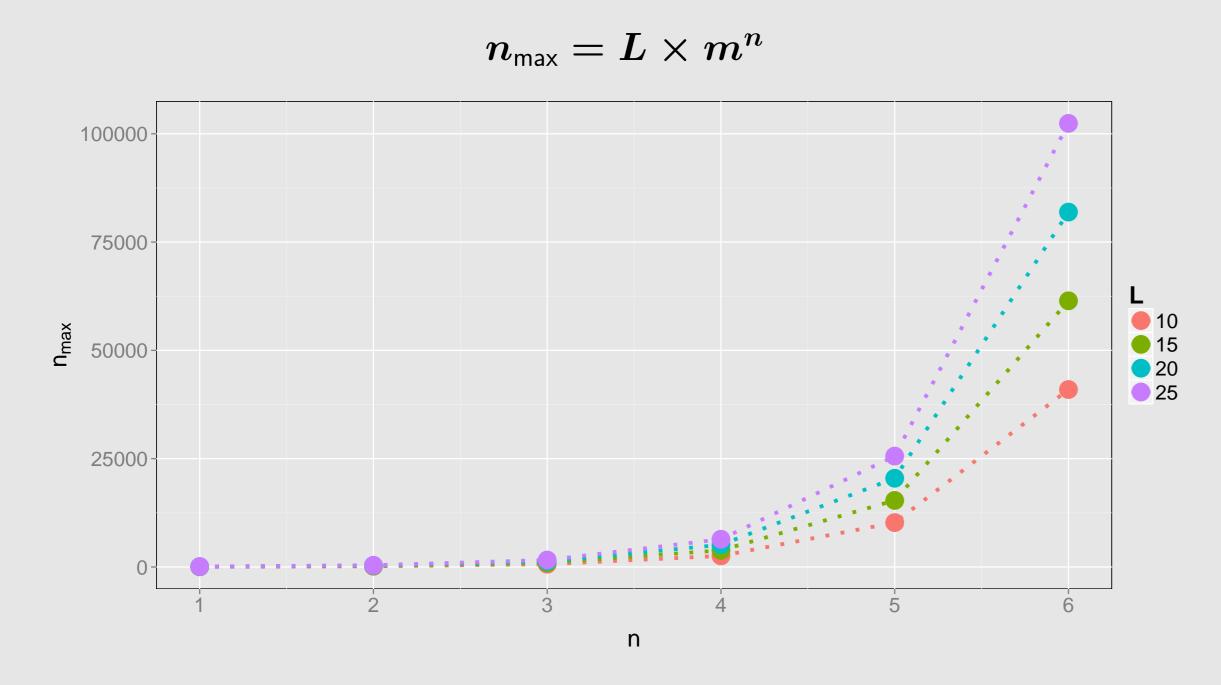
Unigram counts.

A fraction of possible unigrams with position information.

## Curse of dimensionality

Sample sequences. S - sequence, P - postion.

Even when we limit ourselves to only continuous positioned n-grams build on m possible characters, feature space growths rapidly with the number of elements in n-gram (n) and the length of the sequence (L). The number of possible positioned n-grams:



## Feature selecting permutation tests

Model and statistic independent permutation tests can be used to filter features obtained through counting n-grams.

During a permutation test class labels are randomly exchanged during computation of a significance statistic. p-values are defined as:

p-value 
$$= \frac{N_{T_P > T_R}}{N}$$

where  $N_{T_P>T_R}$  is number of times when  $T_P$  (permuted test statistic) was more extreme than  $T_R$  (test statistic for non-permuted data). Permutation tests are computationally expensive (especially considering precise estimation of small p-values, because the number of permutations is inversely proportional to the interval between p-values).

## QuiPT concept

In each permutation, for every observation, there are four possible results:

$$P(Target, Feature) = (1,1)) = p \cdot q$$
 $P(Target, Feature) = (1,0)) = p \cdot (1-q)$ 
 $P(Target, Feature) = (0,1)) = (1-p) \cdot q$ 
 $P(Target, Feature) = (0,0)) = (1-p) \cdot (1-q)$ 

Where p and q are fractions of positive observations in target and feature respectively. An another view at permutation test is therefore that we get a contingency table, which is to be tested for independence. Computing probability of a such table with two constraints,  $n_{1,\cdot}=n_{1,1}+n_{1,0}$  and  $n_{\cdot,1}=n_{1,1}+n_{0,1}$ , and conditioning on  $n_{1,1}$ ,

leads to hypergeometric distribution.  $n_{i,j}$  denotes number of observations for which (Target, Feature) = (i,j)

This is in fact exact two-sided Fisher's test (Lehmann, 1986).

## Computational cost

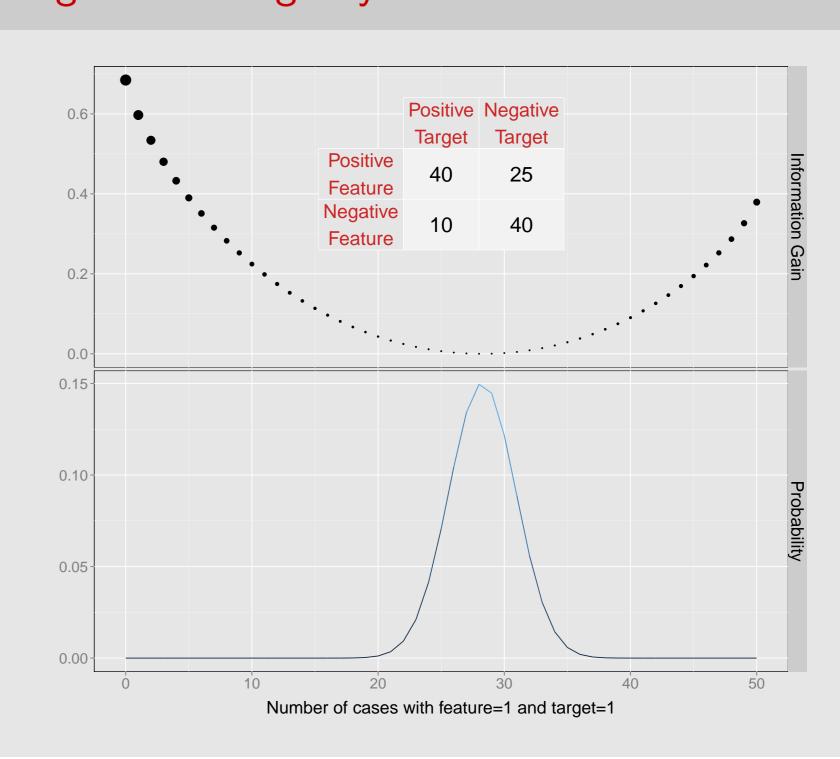
The cost of performing QuiPT is equal to computing a test statistic and probability of occurrence for  $n_{1,1} + n_{0,1}$  contingency tables.

Suppose we consider 6-grams build on sequences of length 25 build of four characters. Then there are around 100,000 n-grams (features) to test. This means that for Benjamini-Hochberg procedure, we need to calculate p-values with accuracy of  $0.05 \times 10^{-5}$ . This requires at least 2 million permutations. Each permutation, apart from reshuffling labels, requires computation of a test statistic. Since n-gram features are very sparse vectors, QuiPT needs to evaluate only few contingency tables.

The relative difference in speed between QuiPT and normal permutation tests depends on several factors, as a number of permutations and input data. For example, for simulation scheme presented below, QuiPT was on average 93 times faster than normal permutation test with  ${\bf 10}^5$  permutations.

## Distribution of Information Gain for given contingency table

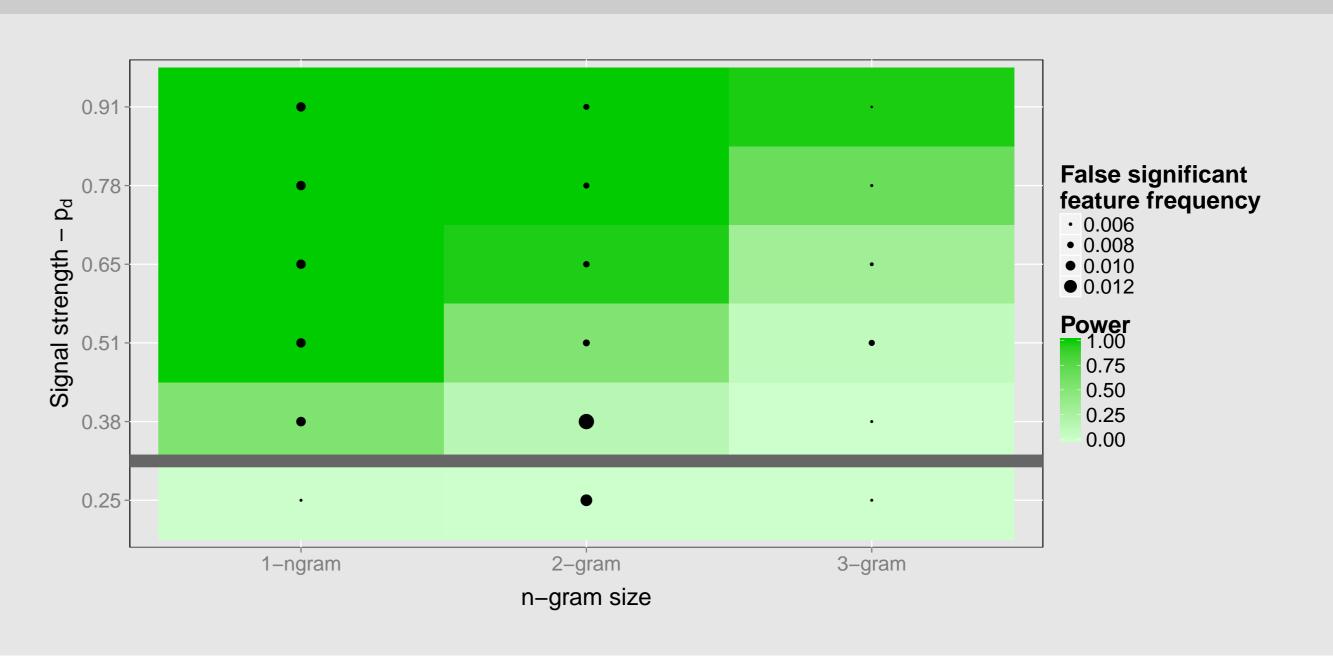
Given constraint on  $n_{1,1}+n_{0,1}$ , probability distribution on contingency tables, which permutations might produce, can be computed exactly.



## Simulation scheme - genomics

- 1. Random 4000 sequences (20 nucleotides each). The half of the sequences has label 0.
- 2. Choose a single position between 3 and 18 (to avoid border cases)
- 3. Resample nucleotides at chosen position. The dominant nucleotide has probability of occurrence  $p_d=0.25$ . Other nucleotides have probability of occurrence  $p_o=(1-p_d)/3$ .
- 4. Perform QuiPT (Information Gain as test statistic) and choose significant features (with p-value < 0.001).
- 5. Iterate steps 1-4 over other values of  $p_d$  0.38, 0.51, 0.65, 0.78, 0.91.
- 6. Repeat steps 1-5 200 times.

## Power and False discoveries



## Summary

Quick permutation test is a powerful and quick equivalent of permutation test in a binary feature – binary target testing scenario. It is especially useful when precisely computed p-values are required and features are sparse vectors.

## **Avaibility**

QuiPT is a part of **biogram** R package devoted to the analysis of n-grams extracted from biological sequences: http://cran.r-project.org/web/packages/biogram/

## Bibliography

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