# Quick Permutation Test: feature filtering of n-gram data

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#### Introduction

N-grams (k-tuples) are vectors of n characters derived from input sequence(s). They may form continuous sub-sequences or be discontinuous. Another important n-gram parameter is its position. Instead of just counting n-grams, one may want to count how many n-grams occur at a given position in multiple (e.g. related) sequences.

Originally developed for natural language processing, n-grams are also used in proteomics, genomics (Fang et al., 2011) and transcriptomics.

	P1	P2	P3	P4	P5	P6
S1	3	1	1	2	3	2
<b>S</b> 2	3	3	4	4	4	2
<b>S</b> 3	3	4	4	4	3	3
	Sar	nple	sec	luen	ces.	

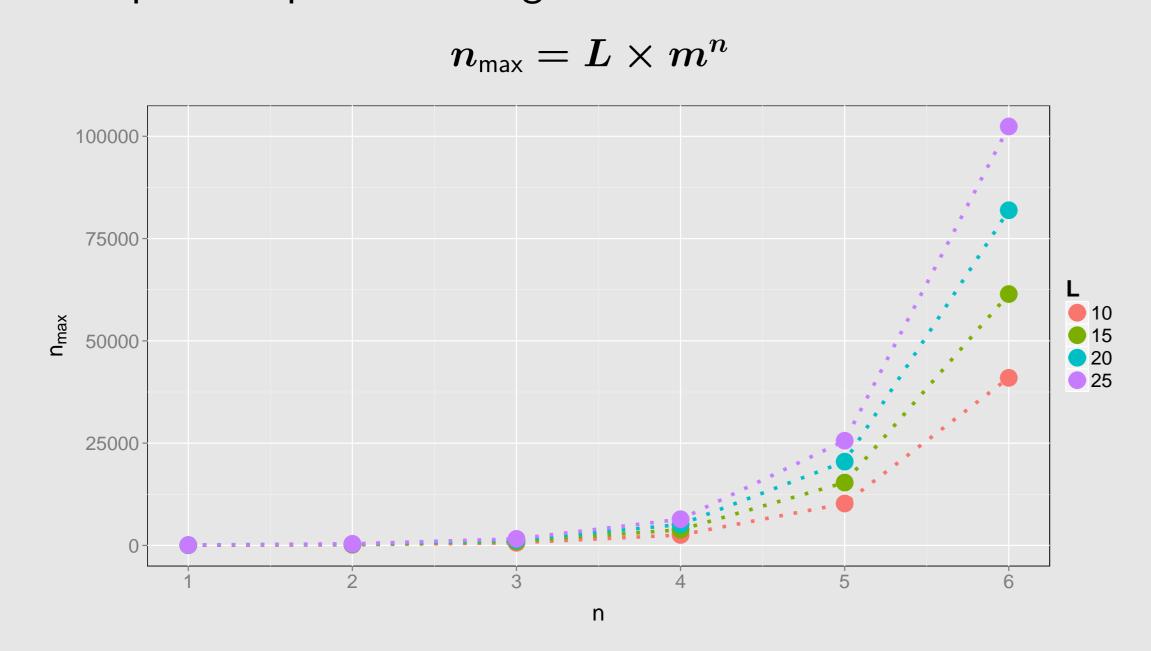
P1_1	P2_1	P3_1	P4_1	P5_1	P6_1	P1_2	P2_2	P3_2	P4_2	P5_2	P6_2	P1_3
0	1	1	0	0	0	0	0	0	1	0	1	1
0	0	0	0	0	0	0	0	0	0	0	1	1
0	0	0	0	0	0	0	0	0	0	0	0	1

A fraction of possible unigrams with position information.

#### Curse of dimensionality

Even when we limit ourselves to only continuous positioned n-grams, feature space growths rapidly with the number of elements in n-gram (n) and length of the sequence (L).

Number of possible positioned n-grams:



#### Feature selecting permutation tests

Model and statistic independent permutation tests can be used to filter features obtained through counting n-grams.

During a permutation test class labels are randomly exchanged during computation of significance statistic. p-values are defined as:

p-value 
$$= rac{N_{T_P > T_R}}{N}$$

where  $N_{T_P>T_R}$  is number of times when  $T_P$  (permuted test statistic) was more extreme than  $T_R$  (test statistic for non-permuted data). Permutation tests are computationally expensive (especially precise estimation of low p-values, because the number of permutations is inversely proportional to the interval between p-values).

#### QuiPT idea

If probability that target equals 1 is p and probability that feature equals 1 is q then we can compute the probability of given observations, eg.

$$P(Target, Feature) = (1,1)) = p \cdot q$$

Therefore another view at permutation test is that we get a contingency table, which needs to be tested for independance.

#### Independence test

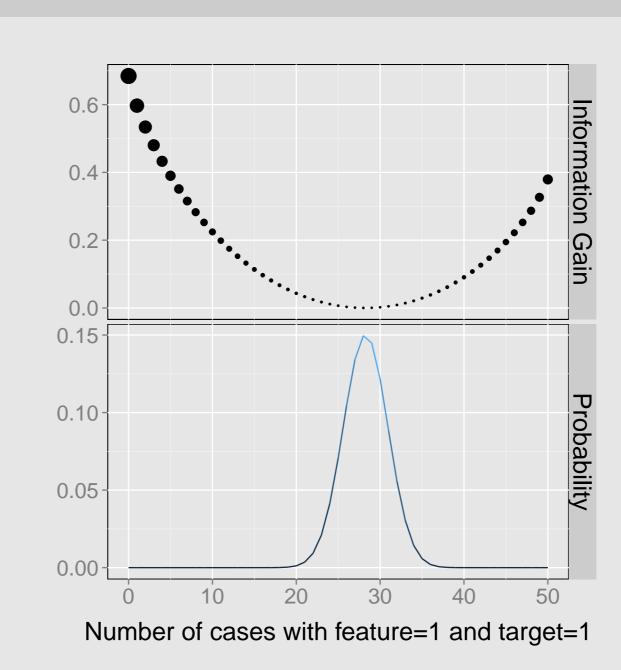
$$\mathsf{F}(\mathsf{n}_{1,1},n_{1,0},n_{0,1},n_{0,0}) = \binom{n}{n_{1,1}} (p \cdot q)^{n_{1,1}} \binom{n-n_{1,1}}{n_{1,0}} (p \cdot (1-q))^{n_{1,0}} \\ \binom{n-n_{1,1}-n_{1,0}}{n_{0,1}} ((1-p) \cdot q)^{n_{0,1}} \binom{n-n_{1,1}-n_{1,0}-n_{0,1}}{n_{0,0}} ((1-p) \cdot (1-q))^{n_{0,0}} \\ \mathsf{This} \ \mathsf{distribution} \ \mathsf{comes} \ \mathsf{with} \ \mathsf{two} \ \mathsf{constraints} \colon \ n_{1,\cdot} = n_{1,1} + n_{1,0} \ \mathsf{and} \\ n_{\cdot,1} = n_{1,1} + n_{0,1}. \ \mathsf{Thus}, \ \mathsf{conditioning} \ \mathsf{on} \ n_{1,1}, \ \mathsf{we} \ \mathsf{get} \ \mathsf{hypergeometric} \\ \mathsf{distribution}.$$

This is in fact exact two-sided Fisher's test. Information Gain is used here as a way of deciding which contingency tables are more extreme.

#### Computational cost

The cost of performing QuiPT is equal to computing Information Gain and probability of occurence for  $n_{1,1}+n_{0,1}$  contingency tables. Suppose we consider 6-grams build on sequences of length 25 build of four characters. Then there are around 100,000 n-grams, features to test. This means that for Benjamini-Hochberg procedure, we need to calculate p-values with accuracy of  $0.05\times 10^{-5}$ . This requires at least 2 million permutations. Each permutation, apart from reshuffling labels, requires computation of IG. Since n-gram features are very sparse vectors, QuiPT needs to evaluate only few contingency tables.

#### Validation procedure

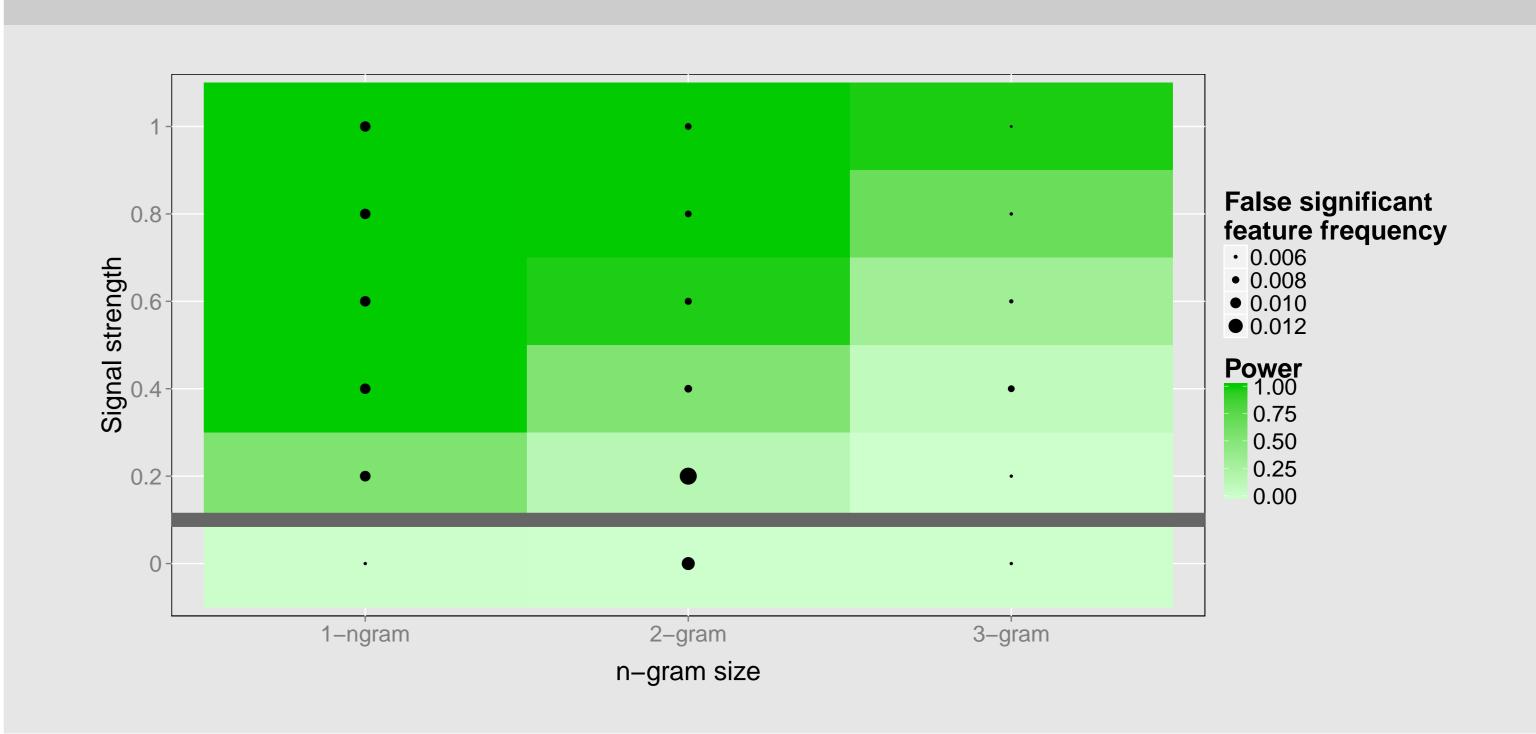


	Target	Feature	Freq
1	0	0	40
2	1	0	10
3	0	1	25
4	1	1	40

#### Simulation scheme

- 1. Random 4000 sequences (20 nucleotides each). The half of the sequences has label 0.
- 2. Choose a single position between 3 and 18 (to avoid border cases).
- 3. Resample nucleotides at chosen position. The dominant nucletoide has probability of occurrence  $p_d=0.25$ . Other nucleotides have probability of occurrence  $p_o=(1-p_d)/3$ .
- 4. Perform QuiPT (Information Gain) and choose significant features (with p-value < 0.001).
- 5. Iterate steps 1-4 over other values of  $p_d$  0.38, 0.51, 0.65, 0.78, 0.91.
- 6. Repeat steps 1-5 200 times.

## Power and False discoveries



## Summary

Quick permutation test is a powerful and quick equivalent of permutation test in binary feature-binary target testing scenario.

### **Avaibility**

biogram R package:

http://cran.r-project.org/web/packages/biogram/

#### Bibliography

Fang, Y.-C., Lai, P.-T., Dai, H.-J., and Hsu, W.-L. (2011). Meinfotext 2.0: gene methylation and cancer relation extraction from biomedical literature. *BMC Bioinformatics*, 12(1):471.