# Quick Permutation Test: feature filtering of n-gram data

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#### Introduction

N-grams (k-tuples) are vectors of n characters derived from input sequence(s). They may form continuous sub-sequences or be discontinuous. Important n-gram parameter is its position. Instead of just counting n-grams, one may want to count how many n-grams occur at a given position in multiple (e.g. related) sequences.

Originally developed for natural language processing, n-grams are also used in genomics (Fang et al., 2011), transcriptomics (Wang et al., 2014) and proteomics (Guo et al., 2014).

Sample sequences. S - sequence, P - postion.

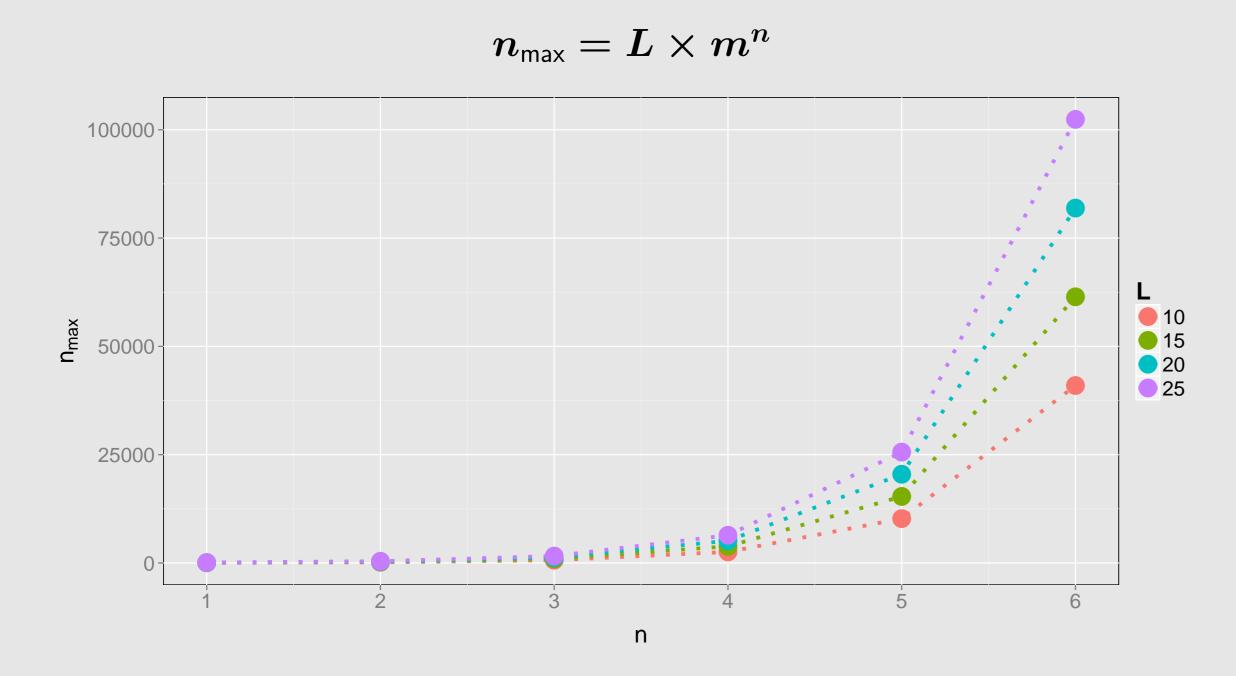
Unigram counts.

	P1_1	P2_1	P3_1	P4_1	P5_1	P6_1	P1_2	P2_2	P3_2	P4_2	P5_2	P6_2	P1_3
S1	1	0	0	0	0	1	0	1	0	0	0	0	0
S2	0	0	0	0	0	0	0	0	1	0	1	0	0
<b>S</b> 3	0	0	1	0	1	0	1	0	0	0	0	0	0

A fraction of possible unigrams with position information.

#### Curse of dimensionality

Even when we limit ourselves to only continuous positioned n-grams, build on m possible characters, feature space growths rapidly with the number of elements in n-gram (n) and the length of the sequence (L). The number of possible positioned n-grams:



#### Feature selecting permutation tests

Model and statistic independent permutation tests can be used to filter features obtained through counting n-grams.

During a permutation test class labels are randomly exchanged during computation of a significance statistic. p-values are defined as:

p-value 
$$= \frac{N_{T_P > T_R}}{N}$$

where  $N_{T_P>T_R}$  is number of times when  $T_P$  (permuted test statistic) was more extreme than  $T_R$  (test statistic for non-permuted data). Permutation tests are computationally expensive (especially considering precise estimation of low p-values, because the number of permutations is inversely proportional to the interval between p-values).

#### QuiPT concept

In each permutation, for every observation, there are four possible results.

$$P(Target, Feature) = (1, 1)) = p \cdot q$$
 $P(Target, Feature) = (1, 0)) = p \cdot (1 - q)$ 
 $P(Target, Feature) = (0, 1)) = (1 - p) \cdot q$ 
 $P(Target, Feature) = (0, 0)) = (1 - p) \cdot (1 - q)$ 

Where p and q are fractions of positive observations in target and feature respectively. An another view at permutation test is therefore that we get a contingency table, which is to be tested for independence. Computing probability of a such table with two constraints,  $n_1 = n_1 + n_2$  and  $n_3 = n_4 + n_5$  and conditioning on  $n_4 = n_4$ .

 $n_{1,\cdot}=n_{1,1}+n_{1,0}$  and  $n_{\cdot,1}=n_{1,1}+n_{0,1}$ , and conditioning on  $n_{1,1}$ , leads to hypergeometric distribution.  $n_{i,j}$  denotes number of observations for which (Target, Feature)=(i,j)

This is in fact exact two-sided Fisher's test (Lehmann, 1986).

### Computational cost

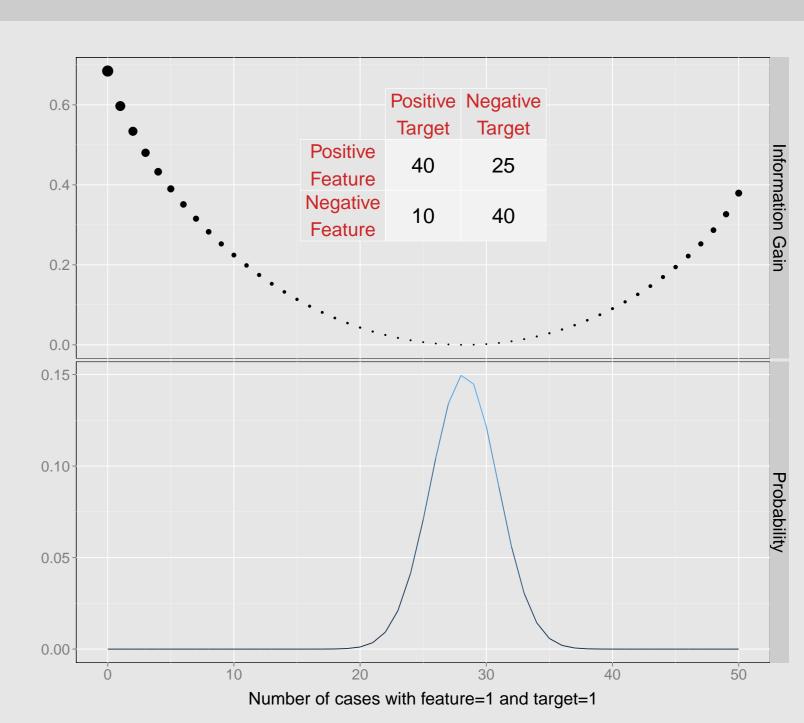
The cost of performing QuiPT is equal to computing a test statistic and probability of occurrence for  $n_{1,1} + n_{0,1}$  contingency tables.

Suppose we consider 6-grams build on sequences of length 25 build of four characters. Then there are around 100,000 n-grams (features) to test. This means that for Benjamini-Hochberg procedure, we need to calculate p-values with accuracy of  $0.05 \times 10^{-5}$ . This requires at least 2 million permutations. Each permutation, apart from reshuffling labels, requires computation of a test statistic. Since n-gram features are very sparse vectors, QuiPT needs to evaluate only few contingency tables.

The relative difference in speed between QuiPT and normal permutation tests depends on several factors, as a number of permutations and input data. For example, for simulation scheme presented below, QuiPT was on average 93 times faster than normal permutation test with  ${\bf 10}^5$  permutations.

#### Distribution of Information Gain for given contingency table

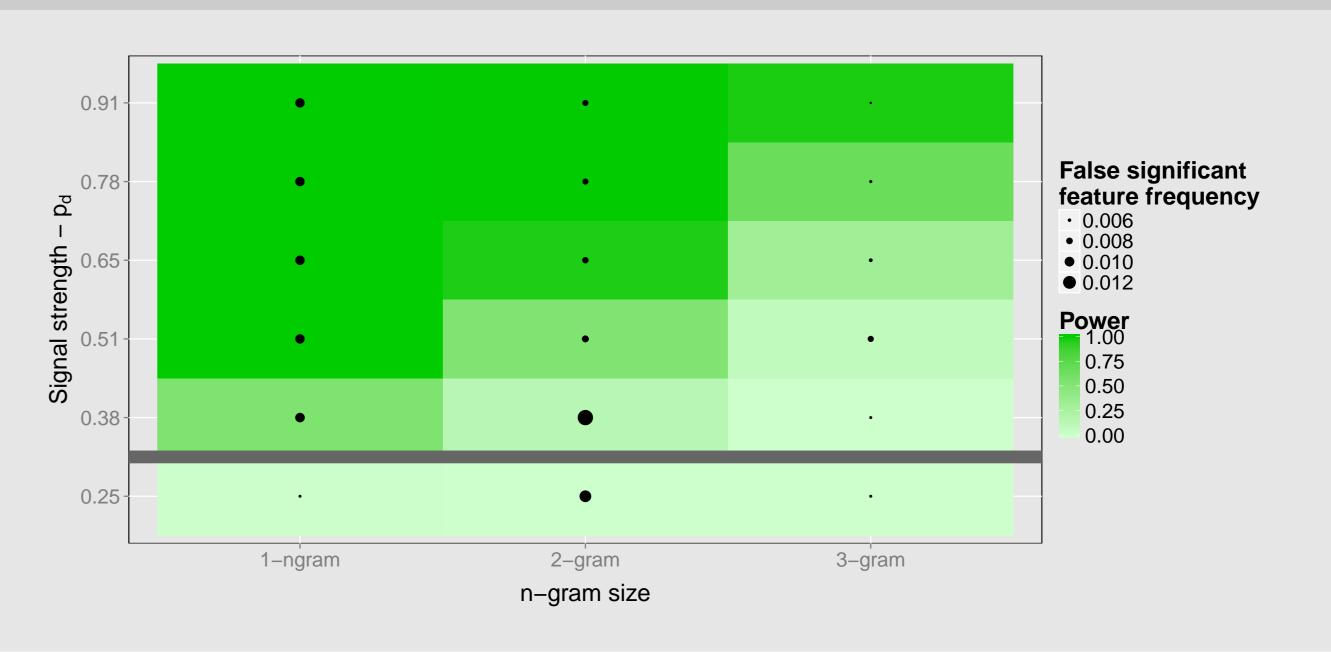
Given constraint on  $n_{1,1}+n_{0,1}$ , probability distribution on contingency tables, which permutations might produce, can be computed exactly.



# Simulation scheme - genomics

- 1. Random 4000 sequences (20 nucleotides each). The half of the sequences has label 0.
- 2. Choose a single position between 3 and 18 (to avoid border cases)
- 3. Resample nucleotides at chosen position. The dominant nucletoide has probability of occurrence  $p_d=0.25$ . Other nucleotides have probability of occurrence  $p_o=(1-p_d)/3$ .
- 4. Perform QuiPT (Information Gain as test statistic) and choose significant features (with p-value < 0.001).
- 5. Iterate steps 1-4 over other values of  $p_d$  0.38, 0.51, 0.65, 0.78, 0.91.
- 6. Repeat steps 1-5 200 times.

#### Power and False discoveries



# Summary

Quick permutation test is a powerful and quick equivalent of permutation test in binary feature-binary target testing scenario. It is especially useful when very precise p-values are required and features are sparse vectors.

#### **Avaibility**

QuiPT is a part of **biogram** R package devoted to the analysis of n-grams extracted from biological sequences: http://cran.r-project.org/web/packages/biogram/

# Bibliography

Fang, Y.-C., Lai, P.-T., Dai, H.-J., and Hsu, W.-L. (2011). Meinfotext 2.0: gene methylation and cancer relation extraction from biomedical literature. *BMC Bioinformatics*, 12(1):471.

Guo, S.-H., Deng, E.-Z., Xu, L.-Q., Ding, H., Lin, H., Chen, W., and Chou, K.-C. (2014). inuc-pseknc: a sequence-based predictor for predicting nucleosome positioning in genomes with pseudo k-tuple nucleotide composition. *Bioinformatics*, 30(11):1522–1529.

Lehmann, E. (1986). *Testing statistical hypotheses*. Wiley series in probability and mathematical statistics: Probability and mathematical statistics. Wiley.

Wang, Y., Liu, L., Chen, L., Chen, T., and Sun, F. (2014). Comparison of metatranscriptomic samples based on jitalic¿tuple frequencies. *PLoS ONE*, 9(1):e84348.