# Quick Permutation Test: feature filtering of n-gram data

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#### Introduction

N-grams (k-tuples) are vectors of n characters derived from input sequence(s). They may form continuous sub-sequences or be discontinuous. Another important n-gram parameter is its position. Instead of just counting n-grams, one may want to count how many n-grams occur at a given position in multiple (e.g. related) sequences.

	P1	P2	P3	P4	P5	P6
S1	2	2	1	3	3	4
<b>S</b> 2	2	1	1	2	4	4
S3	4	2	2	4	1	2
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P1_1	P2_1	P3_1	P4_1	P5_1	P6_1	P1_2	P2_2	P3_2	P4_2	P5_2	P6_2	P1_3
0	0	1	0	0	0	1	1	0	0	0	0	0
0	1	1	0	0	0	1	0	0	1	0	0	0
0	0	0	0	1	0	0	1	1	0	0	1	0

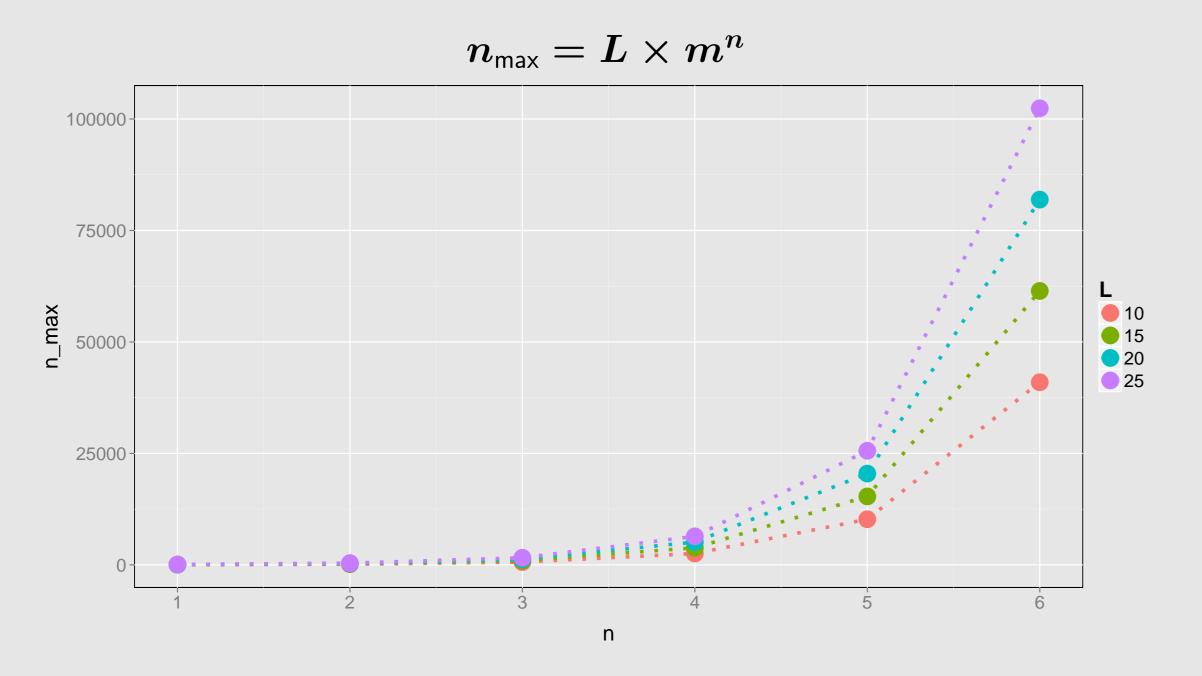
A fraction of possible unigrams with position information.

Originally developed for natural language processing, n-grams are also used in proteomics, genomics and transcriptomics.

### Curse of dimensionality

Even when we limit ourselves to only continuous positioned n-grams, feature space growths rapidly with the number of elements in n-gram (n) and length of the sequence (L).

Number of possible positioned n-grams:



## Feature selecting permutation tests

Model and statistic independent permutation tests can be used to filter features obtained through counting n-grams.

During a permutation test class labels are randomly exchanged during computation of significance statistic. p-values are defined as:

p-value 
$$= \frac{N_{T_P > T_R}}{N}$$

where  $N_{T_P>T_R}$  is number of times when  $T_P$  (permuted test statistic) was more extreme than  $T_R$  (test statistic for non-permuted data). Permutation tests are computationally expensive (especially precise estimation of low p-values, because the number of permutations is inversely proportional to the interval between p-values).

## QuiPT algorithm

If probability that target equals 1 is  $\boldsymbol{p}$  and probability that feature equals 1 is  $\boldsymbol{q}$  and feature and target are independent then each of them has the following probabilities

$$P(Target, Feature) = (1, 1)) = p \cdot q$$
 $P(Target, Feature) = (1, 0)) = p \cdot (1 - q)$ 
 $P(Target, Feature) = (0, 1)) = (1 - p) \cdot q$ 
 $P(Target, Feature) = (0, 0)) = (1 - p) \cdot (1 - q)$ 

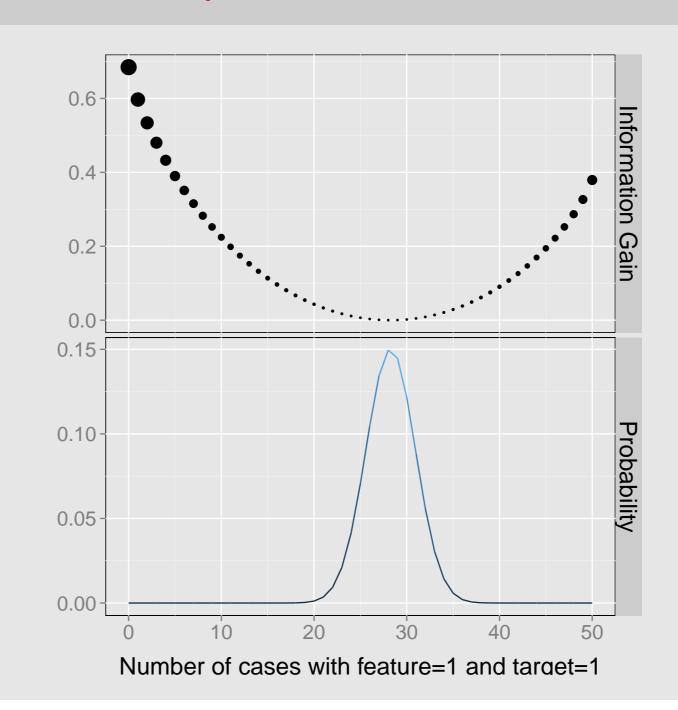
Therefore another view is that we get a contingency table that needs to be tested for independance.

#### Independence test

 $\mathsf{F}(\mathsf{n}_{1,1},n_{1,0},n_{0,1},n_{0,0}) = \binom{n}{n_{1,1}} (p \cdot q)^{n_{1,1}} \binom{n-n_{1,1}}{n_{1,0}} (p \cdot (1-q))^{n_{1,0}} \\ \binom{n-n_{1,1}-n_{1,0}}{n_{0,1}} ((1-p) \cdot q)^{n_{0,1}} \binom{n-n_{1,1}-n_{1,0}-n_{0,1}}{n_{0,0}} ((1-p) \cdot (1-q))^{n_{0,0}} \\ \mathsf{This} \ \mathsf{distribution} \ \mathsf{comes} \ \mathsf{with} \ \mathsf{two} \ \mathsf{constraints} \colon n_{1,\cdot} = n_{1,1} + n_{1,0} \ \mathsf{and} \\ n_{\cdot,1} = n_{1,1} + n_{0,1}. \ \mathsf{Thus}, \ \mathsf{conditioning} \ \mathsf{on} \ n_{1,1}, \ \mathsf{we} \ \mathsf{get} \ \mathsf{hypergeometric} \\ \mathsf{distribution}.$ 

This is in fact exact two-sided Fisher's test. Information Gain is used here as a way of deciding which contingency tables are more extreme.

#### Validation procedure

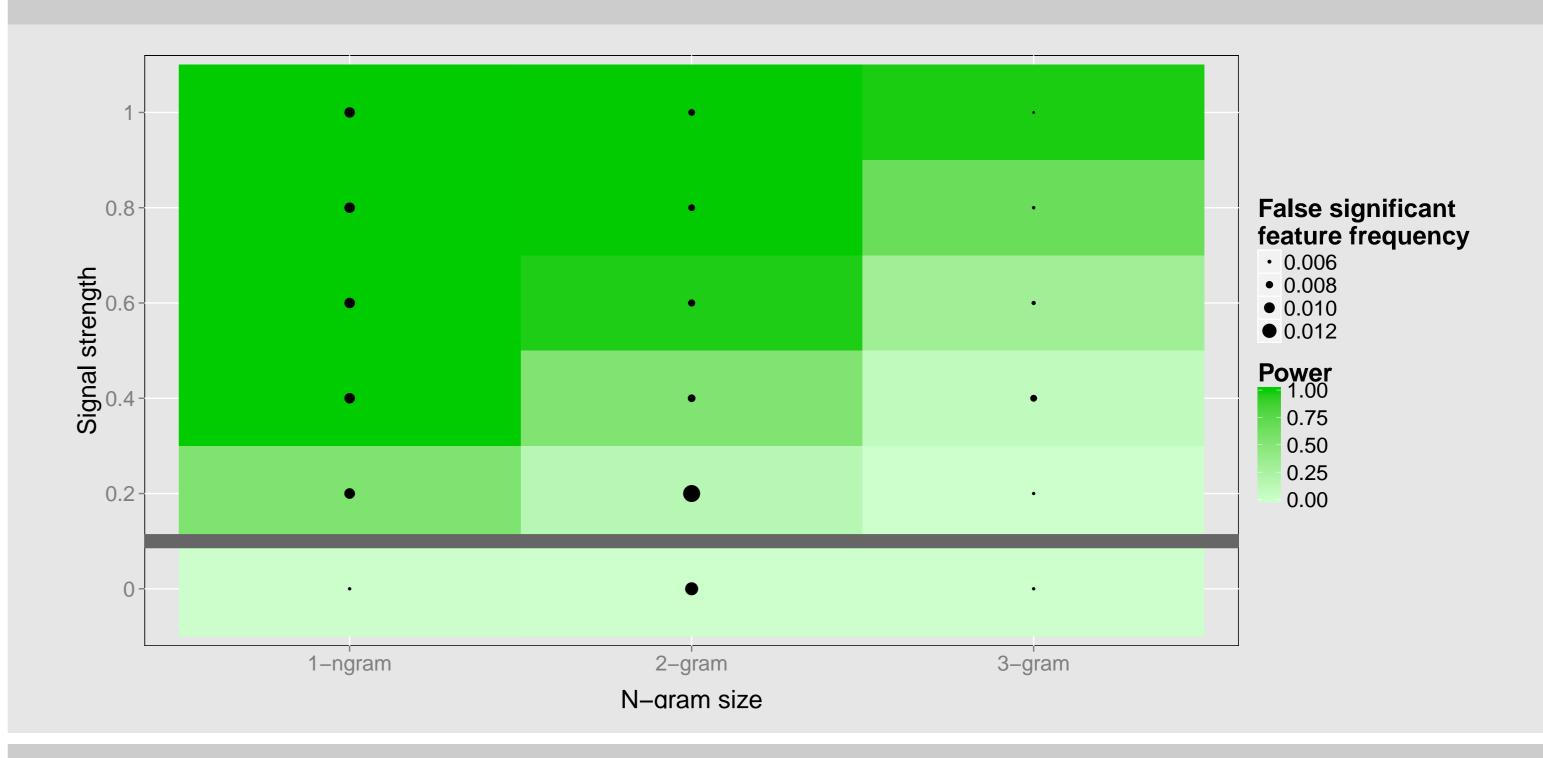


	Target	Feature	Freq
1	0	0	40
2	1	0	10
3	0	1	25
4	1	1	40

#### Simulation scheme

- 1. Random 4000 sequences (20 nucleotides each). The half of the sequences has label 0.
- 2. Choose a single position between 3 and 18 (to avoid border cases).
- 3. Resample nucleotides at chosen position. The dominant nucletoide has probability of occurrence  $p_d=0.25$ . Other nucleotides have probability of occurrence  $p_o=(1-p_d)/3$ .
- 4. Perform QuiPT (Information Gain) and choose significant features (with p-value < 0.001).
- 5. Iterate steps 1-4 over other values of  $p_d$  0.38, 0.51, 0.65, 0.78, 0.91.
- 6. Repeat steps 1-5 200 times.

### Power and False discoveries



### Summary

Quick permutation test is a powerful and quick equivalent of permutation test in binary feature-binary target testing scenario.

## Avaibility

biogram R package:
http://cran r-project.org/we

http://cran.r-project.org/web/packages/biogram/

### Bibliography