

Polymorphism

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Polymorphism introduction

Polymorphism in ML

parametric
weak typed
Type Inserence

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References

Polymorphism in ML Polymorphic functions and types, type inference, ...

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Polymorphism

It permits to handle values of different data types by using a uniform interface.

- A function that can evaluate to or Be applied to values of different types is known as a polymorphic function.
- A data type that can appear to be of a generalized type is designated as a polymorphic data type.

OCaML/ML natively supports polymorphism

```
let compose f g x = f (g x);
```

```
[15:34]cazzola@surtur:~/lp/ml>ocaml
# #use "compose.ml";;
val compose : ('a -> 'b) -> ('c -> 'a) -> 'c -> 'b = <fun>
# compose char_of_int int_of_char ;;
- : char -> char = <fun>
# compose (not) (not) ;;
- : bool -> bool = <fun>
# compose (fun x -> x+1) int_of_char ;;
- : char -> int = <fun>
```



Polymorphism Polymorphism Taxonomy

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Ad Hoc Polymorphism

- the function/method denotes different implementations depending on a range of types and their combination:
- it is supported in many languages by overloading.

Parametric Polymorphism

- all the code is written without mention of any specific type and thus can be used transparently with any number of new types;
- it is widely supported in statically typed functional programming languages or in object-orientation by generics or templates.

Subtype Polymorphism

- the code employs the idea of subtypes to restrict the range of types that can be used in a particular case of parametric polymorphism;
- in OO languages is realized by inheritance and sub-classing



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OCaML supports parametric polymorphism.

- compose implements fog without any type Binding;
- its (polymorphic) type is

$$(\alpha \to \beta) * (\gamma \to \alpha) * \gamma \to \beta$$

- α, β and γ are type variables denoted by 'a, 'b and 'c respectively;
- the type is inferred from time to time; in compose' the possible values for α and β are restricted to **char** and **int**

```
[17:13]cazzola@surtur:-/lp/ml>ocaml
# let compose f g x = f (g x);;
val compose : ('a -> 'b) -> ('c -> 'a) -> 'c -> 'b = <fun>
# let compose' = compose (fun c -> int.of.char c) ;;
val compose' : ('_a -> char) -> '_a -> int = <fun>
```

compose' is weak-typed ('_a).





Polymorphism Weak Typed

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Nothing that is the result of the application of a function to an argument can be polymorphic

Polymorphis introduction taxonomy - if we don't know yet exactly what is its type, then it's a weak type.

Polymorphism in Ml The type 'a -> 'a means:

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- for all type 'a, this is the type 'a -> 'a.

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Whereas, the type '_a -> '_a means:

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- there exist one and only one type '_a such that this is the type '_a -> '_a.

Shall we say that what is potentially polymorphic turns to monomorphic in practice when the compiler deals with its polymorphic form

```
# let a = ref [];;
val a : '_a list ref = {contents = []}
# let b = !:!a ;;
val b : int list = [1]
# a;;
- : int list ref = {contents = []}
```



Polymorphism Type Inference

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let rec map f l = match l with h::l1 -> f h::map f l1

| _ -> [];;

Let us calculate the type of map

- I. [], [] is a zerary function []: $\rightarrow \alpha$ list $\forall \alpha$;
- **2.** h::l1, :: is a Binary operator ::: $\alpha \times \alpha$ list $\rightarrow \alpha$ list so the type of h is α and the type of l1 is α list;
- 3. the type of f is a function whose input has type α nothing can be said on the return type (denoted by β);
- **4**. so the second occurrence of :: should be $\beta \times \beta$ list $\to \beta$ list due to the type of f; that means
- 5. map f l1 should have type β list

and this is possible only if

b. the type of map is $(\alpha \to \beta) \times \alpha$ list $\to \beta$ list

#use "map.ml" ;; val map : ('a -> 'b) -> 'a list -> 'b list = <fun>





Polymorphism @ Work Polymorphic ADT: Stack

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Reference:

```
module Stack = struct
  type 'a stack = { mutable c : 'a list }
  exception EmptyStackException

let empty () = { c = [] }
  let push s x = s.c <- x :: s.c
  let pop s =
    match s.c with
    hd::tl -> s.c <- tl
    | [] -> raise EmptyStackException
end;;
```

```
[22:40]cazzola@surtur:~/lp/ml>ocaml
# #use "adtstack.ml"::
# let s = Stack.empty();;
val s : '_a Stack.stack = {c = []}
# Stack.push s 7::
- : unit = ()
# Stack.push s 25;;
- : unit = ()
# s ;;
- : int Stack.stack = {c = [25: 7]}
# let s1 = Stack.empty();;
val s1 : ' a Stack.stack = {c = []}
# Stack.push s1 "Hello";;
- : unit = ()
# Stack.push s1 "World";;
- : unit = ()
# s1::
- : string Stack.stack = {c = ["World"; "Hello"]}
```



Polymorphism @ Work Iterating on Collections

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Reference:

Count the occurrences

```
let rec count ?(tot=0) x = function
[] -> tot | h::ll -> if (h==x) then count -tot:(tot+1) x ll else count -tot:tot x ll

val count : ?tot:int -> 'a -> 'a list -> int = <fun>
# let il = [;;;3;5;;;;1;5;;5;7;3;;;] ;;
# count u cl;
- : int = 2
# count u il;
- : int = 3
```

Reducing a List

```
let rec remove x = function
[] -> [] | h::l1 -> if (h = x) then (remove x l1) else (h::(remove x l1))

val remove : 'a -> 'a list -> 'a list = <fun>
# remove 3 il;;
- : int list = [1; 2; 4; 2; 2; 1; 4; 5; 7; 2; 1]
# remove 1 cl;
```

- : char list = ['b'; 'c'] Herating on strings

```
let rec iter f ?(k = 0) s = if k < String.length s then ( f s.[k] ; iter f ~k:(k + 1) s ) ;;
```

val iter : (char -> 'a) -> ?k:int -> string -> unit = <fun>



Polymorphism @ Work Sorting (Quicksort)

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Note

- (>:) represents a Binary operator, you can use any sort of symbol
- to avoid to scan the list twice **List**.partition can be used instead of **List**.filter



Polymorphism @ Work Sorting (Selection Sort)

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```
let lmin (<:) 1 =
  let rec lmin m = function
    [] -> m
  | h::tl -> lmin (if (m <: h) then m else h) tl
  in lmin (List.hd l) (List.tl l)
let filter_out x l =
  let rec filter out acc x = function
    [] -> List.rev acc
  | h::tl when h=x -> List.rev_append tl acc
   h::tl -> filter_out (h::acc) x tl
  in filter_out [] x l
let selection (<:) l =</pre>
  let rec selection acc = function
    [] -> List.rev acc
  | l' -> let m = (lmin (<;) l') in selection (m::acc) (filter_out m l')
  in selection [] l
```

```
[10:56]cazzola@surtur:~/lp/ml> ocaml
# let ll = [-7;; ½5;-3;6; 17;-7];
val ll : int list = [-7; 1; 25; -3; 0; 15; 77; -7]
# #use "selection.ml";;
val lmin : ('a -> 'a -> bool) -> 'a list -> 'a = <fun>
val filter_out : 'a -> 'a list -> 'a list -> 'a list = <fun>
val selection : ('a -> 'a -> bool) -> 'a list -> 'a list = <fun>
# selection (<) ll ;
- : int list = [-7; -7; -3; 0; 1; 15; 25; 77]
# selection (>) ll ;;
- : int list = [77; 25; 15; 1; 0; -3; -7; -7]
```



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