



## ML in Action Graph Coverage

Walter Cazzola

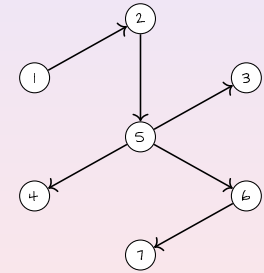
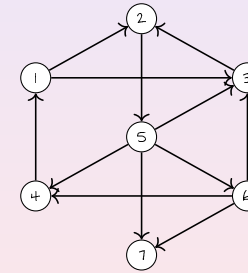
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## Depth First Search (DFS) Problem Definition

### Depth First Search

- is an algorithm for traversing Graph starting from a given node and exploring as far as possible along each branch before backtracking.



### Note,

- DFS depends on how out edges are ordered (in the case above they are sorted by value).
- we focus on acyclic direct Graphs

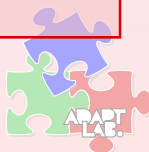


## Depth First Search (DFS) Abstract Datatypes

To solve the problem we need:

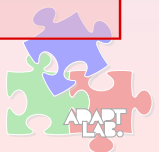
- a tree datatype to represent the result of the visit
- a graph datatype to support the obvious needing

```
module type GraphADT =
sig
  type 'a graph
  val empty : unit -> 'a graph
  val add_node : 'a -> 'a graph -> 'a graph
  val add_arc : 'a -> 'a -> 'a graph -> 'a graph
  val adjacents : 'a -> 'a graph -> 'a list
  val node_is_in_graph : 'a -> 'a graph -> bool
  val is_empty : 'a graph -> bool
  exception TheGraphIsEmpty
  exception TheNodeIsNotInGraph
end;;
```



## Depth First Search (DFS) Graph Implementation

```
module Graph : GraphADT =
struct
  type 'a graph = Graph of ( 'a list ) * ( ( 'a * 'a ) list )
  let empty() = Graph([], [])
  let is_empty = function
    Graph(nodes, _) -> (nodes = [])
  exception TheGraphIsEmpty
  exception TheNodeIsNotInGraph
  (* checks if an element belongs to the list *)
  let rec is_in_list ?(res=false) x = function
    [] -> res
  | h::tl -> is_in_list ~res: (res || (x=h)) x tl
  (* checks if a node is in the graph *)
  let node_is_in_graph n = function
    Graph(nodes, _) -> is_in_list n nodes
  ...
end
```





## Depth First Search (DFS)

### Graph Implementation (Follows)

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DFS

problem def  
abstract DT  
concrete DT  
aux stuff  
dfs  
result  
References

```
(* adds an element to a list if not present *)
let rec add_in_list ?(res=[]) x = function
  [] -> List.rev x::res
| h::tl when (h=x) -> List.rev_append tl (h::res)
| h::tl -> add_in_list ~res: (h::res) x tl

(* operations to add new nodes and arcs (with their nodes) to the graph, respectively *)
let add_node n = function
  Graph( [], [] ) -> Graph( [n], [] )
| Graph( nodes, arcs ) -> Graph( (add_in_list n nodes), arcs )

let add_arc s d = function
  Graph(nodes, arcs) ->
    Graph( (add_in_list d (add_in_list s nodes)), (add_in_list (s,d) arcs) )

(* returns the nodes adjacent to the given node *)
let adjacents n =
  let adjacents n l = List.map snd (List.filter (fun x -> ((fst x) = n)) l)
in function
  Graph(_, arcs) -> adjacents n arcs
```



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## Depth First Search (DFS)

### Ancillary Operations on Graphs

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abstract DT  
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result  
References

```
open Graph

(* transforms a list of arcs in a graph *)
let arcs_to_graph arcs =
  let rec arcs_to_graph g = function
    [] -> g
  | (s,d)::tl -> arcs_to_graph (add_arc s d g) tl
  in arcs_to_graph (empty()) arcs

(* extract a tree out of acyclic graph with the given node as the root *)
let graph_to_tree g root =
  let rec make_tree n = function
    [] -> Leaf(n)
  | adj_to_n -> Tree(n, (make_forest adj_to_n))
  and make_forest = function
    [] -> []
  | hd::tl -> (make_tree hd (adjacents hd g))::(make_forest tl)
  in make_tree root (adjacents root g)
```



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## Depth First Search (DFS)

### DFS Implementation

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DFS

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```
open Graph

let dfs g v =
  let rec dfs g v g' = function
    [] -> g'
  | hd::tl when (node_is_in_graph hd g') -> dfs g v g' tl
  | hd::tl -> dfs g v (add_arc v hd (dfs g hd (add_node hd g')) (adjacents hd g)) tl
  in
    if (is_empty g) then raise TheGraphIsEmpty
    else if not (node_is_in_graph v g) then raise TheNodeIsNotInGraph
    else graph_to_tree (dfs g v (add_node v (empty())) (adjacents v g)) v
```



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## Depth First Search (DFS)

### DFS in Action

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```
[18:08]cazzola@surture:~/lp/ml>ocaml
# #use "tree.ml";;
type 'a tree = Leaf of 'a | Tree of ('a * 'a tree list)
# #use "GraphADT.ml";;
module type GraphADT =
sig
  type 'a graph
  val empty : unit -> 'a graph
  val add_node : 'a -> 'a graph -> 'a graph
  val add_arc : 'a -> 'a -> 'a graph -> 'a graph
  val adjacents : 'a -> 'a graph -> 'a list
  val node_is_in_graph : 'a -> 'a graph -> bool
  val is_empty : 'a graph -> bool
  exception TheGraphIsEmpty
  exception TheNodeIsNotInGraph
end
# #use "Graph.ml" ;;
module Graph : GraphADT
# #use "aux.ml" ;;
val arcs_to_graph : ('a * 'a) list -> 'a Graph.graph = <fun>
val graph_to_tree : 'a Graph.graph -> 'a -> 'a tree = <fun>
# #use "dfs.ml" ;;
val dfs : 'a Graph.graph -> 'a -> 'a tree = <fun>
# let g1 = arcs_to_graph [(1,2);(1,3);(4,1);(5,4);(3,2);(3,5);(5,3);(5,6);(5,7);(6,7);(6,3);(6,4)] ;;
val g1 : int Graph.graph = <abstr>
# let g7 = arcs_to_graph [(("C", "Scala"), ("Lisp", "Erlang")); ("Algol", "C++"); ("C", "Java"); ("Lisp", "Python"); ("Pascal", "Modula 2"); ("C", "C++"); ("Java", "Scala"); ("Lisp", "ML"); ("Lisp", "Scala"); ("Lisp", "Python"); ("Lisp", "Erlang"); ("ML", "OCaML")];;
val g7 : string Graph.graph = <abstr>
# dfs g1 1 ;;
- : int tree = Tree (1, [Tree (2, [Tree (5, [Leaf 4; Leaf 3; Tree (6, [Leaf 7])])])])
# dfs g7 "Algol" ;;
- : string tree = Tree ("Algol", [Tree ("Pascal", [Leaf "Modula 2"]);
  Tree ("C", [Tree ("Java", [Leaf "Scala"]); Leaf "C++"]); Leaf "Python"])
# dfs g7 "Lisp" ;;
- : string tree = Tree ("Lisp", [Tree ("ML", [Leaf "OCaML"]); Leaf "Scala"; Leaf "Python"; Leaf "Erlang"])
```



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## References

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References

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