

ML in Action

Walter Cazzola

DFS

problem def. abstract DT concrete DT aux stuff dfs

References

ML in Action Graph Coverage

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Depth First Search (DFS) Problem Definition

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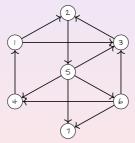
DFS

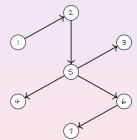
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References

Depth First Search

- is an algorithm for traversing graph starting from a given node and exploring as far as possible along each branch before backtracking





Note,

- DFS depends on how out edges are ordered (in the case above they are sorted by value).
- we focus on acyclic direct graphs



Depth First Search (DFS) Abstract Datatypes

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References

To solve the problem we need:

- a tree datatype to represent the result of the visit

```
type 'a tree = Leaf of 'a | Tree of ('a * 'a tree list);;
```

- a graph datatype to support the obvious needing

```
module type GraphADT =
    sig
    type 'a graph

val empty : unit -> 'a graph

val add_node : 'a -> 'a graph -> 'a graph
 val add_arc : 'a -> 'a -> 'a graph -> 'a graph
 val adjacents : 'a -> 'a graph -> 'a list
 val node_is_in_graph : 'a -> 'a graph -> bool
 val is_empty : 'a graph -> bool
    exception TheGraphIsEmpty
    exception TheNodeIsNotInGraph
end;;
```





Depth First Search (DFS) Graph Implementation

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```
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dfs
result
```

```
module Graph : GraphADT =
struct
   type 'a graph = Graph of ( 'a list ) * ( ( 'a * 'a ) list )
   let emptv() = Graph([], [])
   let is_empty = function
     Graph(nodes, _) -> (nodes = [])
   exception TheGraphIsEmpty
   exception TheNodeIsNotInGraph
   (* checks if an element belongs to the list *)
   let rec is_in_list ?(res=false) x = function
     [] -> res
    | h::tl -> is_in_list ~res: (res || (x=h)) x tl
   (* checks if a node is in the graph *)
   let node_is_in_graph n = function
     Graph(nodes, _) -> is_in_list n nodes
  end
```



Depth First Search (DFS) Graph Implementation (Follows)

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Zeference:

```
(* adds an element to a list if not present *)
let rec add_in_list ?(res=[]) x = function
  [] -> List.rev x::res
  h::tl when (h=x) -> List.rev_append tl (h::res)
  h::tl
                  -> add_in_list ~res: (h::res) x tl
(* operations to add new nodes and arcs (with their nodes) to the graph, respectively *)
let add node n = function
  Graph([], []) -> Graph([n], [])
 | Graph( nodes, arcs ) -> Graph( (add_in_list n nodes), arcs )
let add arc s d = function
  Graph(nodes, arcs) ->
     Graph( (add_in_list d (add_in_list s nodes)), (add_in_list (s.d) arcs) )
(* returns the nodes adjacent to the given node *)
let adjacents n =
  let adjacents n l = List.map snd (List.filter (fun x -> ((fst x) = n)) l)
in function
  Graph(_, arcs) -> adjacents n arcs
```





Depth First Search (DFS) Ancillary Operations on Graphs

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problem def. abstract DT

aux stuff

result

References

```
open Graph
(* transforms a list of arcs in a graph *)
let arcs_to_graph arcs =
  let rec arcs_to_graph g = function
              -> a
  | (s,d)::tl -> arcs_to_graph (add_arc s d g) tl
 in arcs_to_graph (empty()) arcs
(* extract a tree out of acyclic graph with the given node as the root *)
let graph_to_tree g root =
  let rec make tree n = function
    [] -> Leaf(n)
  | adj_to_n -> Tree(n, (make_forest adj_to_n))
  and make_forest = function
   [] <> []
  | hd::tl -> (make_tree hd (adjacents hd g))::(make_forest tl)
  in make_tree root (adjacents root g)
```





Depth First Search (DFS) DFS Implementation

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Reference:





Depth First Search (DFS) DFS in Action

[18:08]cazzola@surtur:~/lp/ml>ocaml

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Reservences

```
# #use "tree.ml"::
type 'a tree = Leaf of 'a | Tree of ('a * 'a tree list)
# #use "GraphADT.mli"::
module type GraphADT =
    type 'a graph
    val empty : unit -> 'a graph
    val add_node : 'a -> 'a graph -> 'a graph
    val add_arc : 'a -> 'a graph -> 'a graph
    val adjacents : 'a -> 'a graph -> 'a list
    val node_is_in_graph : 'a -> 'a graph -> bool
    val is empty : 'a graph -> bool
    exception TheGraphIsEmpty
    exception TheNodeIsNotInGraph
  end
# #use "Graph.ml" ;;
module Graph : GraphADT
# #use "aux.ml" ::
val arcs to graph : ('a * 'a) list -> 'a Graph.graph = <fun>
val graph_to_tree : 'a Graph.graph -> 'a -> 'a tree = <fun>
# #use "dfs.ml" ::
val dfs : 'a Graph.graph -> 'a -> 'a tree = <fun>
# let q1 = arcs_to_graph [(1,2);(1,3);(4,1);(5,4);(3,2);(2,5);(5,3);(5,6);(5,7);(6,7);(6,3);(6,4)];
val q1 : int Graph.graph = <abstr>
# let g7 = arcs_to_graph([("A
  ("Algol", "Python"): ("Pascal", "Modula 2"): ("C", "C++"): ("Java", "Scala"): ("Lisp", "ML"):
  ("Lisp", "Scala"); ("Lisp", "Python"); ("Lisp", "Erlang"); ("ML", "OCaML")]);;
val q7 : string Graph.graph = <abstr>
# dfs a1 1 ::
- : int tree = Tree (1, [Tree (2, [Tree (5, [Leaf 4; Leaf 3; Tree (6, [Leaf 7])])])])
# dfs q7 "
- : string tree = Tree ("Algol", [Tree ("Pascal", [Leaf "Modula 2"]):
   Tree ("C". [Tree ("Java". [Leaf "Scala"]): Leaf "C++"]): Leaf "Pvthon"])
# dfs a7
-: string tree = Tree ("Lisp", [Tree ("ML", [Leaf "OCaML"]): Leaf "Scala": Leaf "Python": Leaf "Erlang"]
```



References

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References

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