

## Laboratory 03

### Finite Element method for the diffusion-reaction equation in 3D

#### **Exercise 1.**

Let  $\Omega = (0, 1)^3$ , be the unit cube and let us consider the following diffusion-reaction problem:

$$\begin{cases} -\nabla \cdot (\mu \nabla u) + \sigma u = f & \mathbf{x} \in \Omega, \\ u = 0 & \text{on } \partial\Omega, \end{cases} \quad \begin{array}{l} (1a) \\ (1b) \end{array}$$

where  $\mathbf{x} = (x, y, z)^T$ ,  $\sigma(\mathbf{x}) = 1$ ,  $f(\mathbf{x}) = 1$  and

$$\mu(\mathbf{x}) = \begin{cases} 100 & \text{if } x < \frac{1}{2}, \\ 1 & \text{if } x \geq \frac{1}{2}. \end{cases}$$

**1.1.** Starting from the code of previous laboratories, implement a finite element solver for problem (1). The solver should read the mesh from file. Use the mesh `mesh/mesh-cube-10.msh` (four differently refined meshes are provided in the folder `mesh`).

**1.2.** Compute the solution on the mesh `mesh/mesh-cube-40.msh` (i.e.  $N + 1 = 40$ ), with linear finite elements.