# Study of low-frequency quasi-periodic oscillations in GRS 1739–278 during 2014 outburst

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### ABSTRACT

We detected a type-C LF QPO at 0.3-0.7 Hz in NuSTAR and Swift-XRT observations of the black hole candidate GRS 1739–278 during the hard-intermediate state of its 2014 outburst, and type-B QPO in 1.7-5.2 Hz range during the soft-intermediate state. We traced the evolution of spectro-timing properties of the source during NuSTAR observation. As QPO frequency increases, the source spectrum becomes softer, with increasing power-law index and decreasing cut-off energy.

We performed an extended analysis of rapid X-ray variability in terms of power spectrum, cospectrum, coherence and phase-lags. In the power spectrum a prominent QPO and its second harmonic are clearly seen. The fluxes in soft and hard X-ray bands are coherent, however coherence drops with the separation of the energy bands. Phase-lags are generally positive (hard) in the 0.1–3 Hz frequency range, and negative below 0.1 Hz. Measurements of the inner disk radius obtained with the spectral models accounting for the metric around black hole and QPO frequency together with the relativistic precession model points towards very massive black hole.

**Key words:** X-rays: individual (GRS 1739–278) – X-rays: binaries – accretion, accretion disks – stars: black holes

# 1 INTRODUCTION

A study of X-ray variability in accreting astrophysical sources provides a broad view on processes that take a place in such systems. This works both on a long timescales - i.e. days and weeks - when one speaks about state changes through outbursts of transients sources (see e.g. Homan and Belloni 2005; Heil et al. 2015), and on short - all the way down to milliseconds - when the subject under consideration are a quasi-periodic oscillations (QPOs) and broad band stochastic noise. By simultaneous usage of spectral and timing data one can better constrain geometry of accretion flow around compact objects and infer on which processes are responsible for generation of observed spectro-timing features in a self-consistent way.

Some aspects of the spectro-timing evolution of X-ray transients (usually black-hole candidates, BHC) during outbursts can be explained in the frame of the two-temperature accretion flow model (Eardley et al. 1975; Shapiro et al. 1976; Narayan and Yi 1995), in which it is proposed that the accretion flow in a system consists of the geometrically

thin cold disk and geometrically thick hot flow (corona). It is strongly suggested from the observations that this geometrically thick hot flow is responsible for production of strong variability. As an example, using frequency-resolved spectroscopy Churazov et al. (2001) shown that variable part of the emission from the BHC system Cyg X-1 has a hard power-law shaped spectrum, which is thought to be produced by Comptonization of soft photons onto hot electrons in the corona, while stable part of the emission has a spectrum which is consistent with the cold classical  $\alpha$ -disc spectrum (Shakura and Sunyaev 1973). It is also well known that total variability power of BHC and neutron star binaries is greater in the hard state (when the spectrum is dominated by the emission produced in the hot flow) than in the soft state (when the spectrum can be described with optically thick  $\alpha$ -disk model) (Miyamoto et al. 1992; Revnivtsev et al. 2000; Homan et al. 2001; Churazov et al. 2001, e.t.c.). Lyubarskii (1997) proposed that observed strong variability (seen as a broad band noise in power spectra) is produced due to the stochastic variations of the angular momentum transport efficiency. In this propagating fluctuation model broad band noise of the luminosity is a product of noise signals from different radii of the accretion flow, each with its

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own characteristic time-scale (see, e.g. Arévalo and Uttley 2006; Ingram and van der Klis 2013). Therefore, the spectral shape of the broad band noise is determined by the physical and geometrical properties of the accretion flow, e.g. in particular in these works it was suggested that the broad noise dumping frequency is connected to the inner edge of the accretion flow.

Another feature, frequently observed in the X-ray binaries power spectra is different types of low and high frequency QPOs, manifesting itself as a narrow Lorentzian components. The low frequency QPOs are better studied, since they occur at moderate frequencies of 0.1..10 Hz. This QPOs are ubiquitous - they found in systems with neutron stars and black holes (Wijnands and van der Klis 1999), in cataclysmic variables (Mauche 2002) and even in active galactic nuclei (Gierliński et al. 2008). Few types of LF QPOs are distinguished, based on the shape of power spectrum (see, e.g. Casella et al. 2005). Most importantly, their origin still remains unclear, although it is possible that different mechanisms are responsible for different types of QPO.

Type-C LF QPOs are typically found in X-ray black hole transients (yet they are known to be present in neutron star systems too) during initial rise and transition to disk dominated state - i.e. in low-hard state (LHS) and in hard intermediate state (HIMS), according to standard scheme (Grebenev et al. 1997; Tanaka and Shibazaki 1996; Remillard and McClintock 2006; Belloni 2010), although they are sometimes seen at higher frequencies (≈30 Hz) after transition to high soft state (HSS). These QPOs are easy to detect and study, since they are prominent, having  $rms \approx 10\%$ (Casella et al. 2005). Different authors prescribe generation of these QPOs to various processes: Lense-Thirring precession of inner parts of the accretion disk (Stella and Vietri 1998; Ingram et al. 2009), oscillations of a standing shock (Molteni et al. 1996) and accretion rate modulation caused by different phenomena (Tagger and Pellat 1999; Cabanac et al. 2010) e.t.c. In some models, particularly in relativistic precession models (RPM), observed frequency is strongly dependent on the inner radius of the accretion disk, at which it transforms into geometrically thick optically thin hot flow

Recent advances in simulations of the reflected emission (Ross and Fabian 2005; García et al. 2014), arising due to the scattering and absorption of the hard photons in the cold accretion disk, led to the possibility to study geometry of the disk. For such a study to be made it is essential to obtain broadband X-ray spectrum with high energy resolution - reflected emission manifest itself by a presence of prominent, wide and asymmetric iron  $K_{\alpha}$  fluorescent emission line at 6.4 keV and Compton-hump at 20-30 keV. Now, adding information from X-ray timing analysis one can, in principle, constrain the location of a component, responsible for the variability - which is though to be a corona or a jet base. This task presents a challenge, that can be solved only by a telescope that posses both possibility to measure a broadband spectrum with good resolution and have a corresponding timing capabilities. NuSTAR (Harrison et al. 2013), launched in 2013, is the best available instrument for such studies. XMM-Newton and NICER can be used too, although their energy range reaching only up to  $\sim 12 \text{ keV}$ limits their capability to measure hard tails and Comptonhump contribution. Nevertheless there are some great results obtained with these instruments, e.g. measurement of the Fe  $K\alpha$  line profile variation with QPO phase by Ingram et al. (2016).

In this article we report on first detection of type-C QPOs in HIMS of Galactic black-hole candidate GRS 1739–278 and present a detailed study of properties of the X-ray variability, along with spectral evolution with NuSTAR and Swift-XRT.

### 2 GRS 1739-278

GRS 1739-278 is a typical X-ray nova, discovered during outburst in 1996 (Paul et al. 1996) by SIGMA (Paul et al. 1991) telescope onboard GRANAT space observatory. Using ROSAT observation Greiner et al. (1996) inferred distance of 6-8.5 kpc from the estimated absorption, indicating that the source may belong to Galactic bulge. It should be noted that Greiner et al. (1996) used X-ray halo size to assess obscuration column density, and mean extinction per parsec value from (Allen 1973) to estimate distance to the source. While his  $N_{\rm H}$  estimation appears to be quite precise it is larger than the new measurements of the line of sight absorption in the Galaxy towards the source (Dickey and Lockman 1990; Kalberla et al. 2005; Marshall et al. 2006; Schultheis et al. 2014). It follows that the source either has intrinsic obscuration or additional line of sight obscuration and the distance to the source can not be constrained from  $N_{\rm H}$ . Nevertheless in this work we will assume that the distance to GRS 1739-278 is 8 kpc, given that the source is projected on to the Galactic Bulge.

Optical and radio emission were detected during the course of outburst (Hjellming et al. 1996; Marti et al. 1997). Borozdin et al. (1998) found spectral evolution throughout the outburst to be consistent with canonical model - outburst starts from LHS, then soft emission, associated with the optically thick disk starts to dominate, heralding transition to high soft state. Eventually, they observed very high state and detected a QPO at 5 Hz using RXTE data (Borozdin and Trudolyubov 2000; Wijnands et al. 2001).

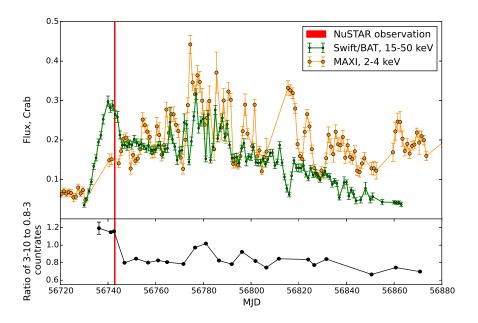
After some 18 year slumber GRS 1739–278 demonstrated another big outburst, rise of which was detected by Swift-BAT (Krimm et al. 2014) along with INTE-GRAL (Filippova et al. 2014). During this outburst extensive observing campaign by Swift-XRT were carried out, along with single long NuSTAR exposure. After this outburst the source remain active with repetitive mini-outbursts (Mereminskiy et al. 2017; Yan and Yu 2017).

## 3 OBSERVATIONS AND DATA REDUCTION

In order to characterize the overall outburst profile we used data of Swift-BAT  $transient\ monitor\ (Krimm\ et\ al.\ 2013)$  in hard X-rays (15–50 keV) as well as (2–4 keV) lightcurve from  $MAXI\ (Matsuoka\ et\ al.\ 2009)$ .

We used NuSTAR observation (ObsID: 80002018002) performed at March 26, 2014 (MJD 56742). We utilized nuproducts pipeline to extract photons from two-arcminute circular region, centered on the source and to produce lightcurves and spectra.

We also used public observations of Swift-XRT (target



**Figure 1.** Upper: green points denote Swift-BAT lightcurve of 2014 outburst in 15–50 keV range, orange circles correspond to MAXI fluxes in 2–4 keV. Red line show the time interval of NuSTAR observation. Lower: evolution of Swift-XRT spectral hardness during the outburst.

ID: 33203) performed regularly over the rise and peak of the outburst. Since the source was bright, all Swift-XRT observations were performed in windowed mode, allowing study of timing properties of the source. We performed standard analysis with xrtpipeline and barycentered data prior to lightcurve extraction. During several observations countrate was as high as 280 cts s<sup>-1</sup>, therefore we excluded one or few brightest columns depending on countrate, in order to suppress effects caused by photon pile-up. Photons with energies below 0.8 keV and above 10 keV were also filtered out. Long-term lightcurves and spectra were obtained from UK Swift Science Data Centre at the University of Leicester (Evans et al. 2009).

# 4 ANALYSIS

### 4.1 Outburst

First detection of the source by Swift-BAT (Krimm et al. 2014) occurred at March 9, 2014 (MJD 56725, we will refer to this date as  $\tau_0$ ). Outburst profile in hard X-rays (15–50 keV) featured fast rise with tenfold intensity increase over ten days, nearly flat-top peak ( $\tau_0+10..+15$  days) followed by abrupt flux decrease by 30% over the course of two days. After this, the source demonstrated gradual decline interrupted by flaring activity at  $\tau_0+50..+70$  days. At  $\tau_0\approx+86$  days a sharp dip occurred in the Swift-BAT lightcurve. After the cease of the outburst source remained active with flux about 5–15 mCrab.

Adding data from MAXI to the Swift-BAT hard X-ray lightcurve gives us another insight on the outburst evolution as shown in Fig. 1 - comparing fluxes in soft and hard bands (for 2–4 keV band we took a 1.67 counts s<sup>-1</sup> as a reference value for Crab, corresponding value for 15–50 keV band is 0.22 cts cm<sup>-2</sup> s<sup>-1</sup>) one can see that the soft component

obviously lags hard emission in the beginning of the outburst but then starts to grow and ends up dominating during the flaring period as well as during hard dip. Lower subplot of Fig. 1 shows evolution of hardness ratio (3–10 keV/0.8–3 keV) measured by Swift-XRT. Right after the peak of hard emission one can see the decline of hardness, also indicating appearance of the thermal component. Detailed analysis of the spectral evolution during the outburst will be presented in Bykov et al., (2018) in preparation.

Fortunately, NuSTAR observation triggered by Miller et al. (2015) were carried right at the transition between hard and soft states, thus giving us unique possibility to study processes that happens during HIMS.

### 4.2 NuSTAR observation

NuSTAR observed GRS 1739–278 for nearly 30 ks of net exposure right after the hard X-ray peak (at  $\tau_0 \approx +18$ , see Fig. 1). Earlier, Miller et al. (2015) shown that the average spectrum of this observation is well described by relativistic reflection models such as relxill (García et al. 2014; Dauser et al. 2014, 2016) with accretion disk that reaches remarkably close to the black hole innermost stable circular orbit (ISCO), with disk inner edge radius upper estimate being  $R_{\rm in} = 5^{+3}_{-4} \, GM/c^2$  (Miller et al. 2015). They also noted that no additional thermal component was needed in order to describe NuSTAR energy spectrum probably due to the low disk temperature and high absorption.

Given the 96.9 minute orbital period of NuSTAR, observation is divided in 13 intervals separated by Earth occultations, as shown in Fig. 2. We denoted these intervals with roman numerals, from I to XIII. From the lightcurve it is clear, that the source flux increased throughout observation from  $\approx 145$  up to  $\approx 170$  counts per second. The spectrum also altered, with hardness (defined as ratio of

# 4 I. A. Mereminskiy et al.

countrates  $R_{3-10\,keV}/R_{10-78\,keV}$ ) had been growing monotonically from 2.7 to 3.1.

### 4.2.1 Continuum evolution

To get better view on the evolution of continuum emission we fitted all individual interval spectra using XSPEC package (Arnaud 1996) with absorbed xillver (García et al. 2013) model (const\*phabs\*xillver). This model describes reflection of incident radiation from ionized slab of matter. The spectrum of incident radiation are assumed to be power-law with exponential cutoff. We picked xillver model over the relxill for separate intervals analysis because we wanted to describe the changes in the continuum emission making no assumptions on the system geometry.

Spectra from two NuSTAR modules of each interval were fitted simultaneously with free cross-calibration constant between modules. Before fitting, spectra were grouped in order to have at least 100 counts per bin, channels above  $60~\mathrm{keV}$  were ignored. We choose to fix interstellar absorption at  $N_H = 2.15 \times 10^{22} \text{ cm}^{-2}$  as was found by joint XMM-Newton/NuSTAR observation during the low luminosity state (Fuerst et al. 2016). Element abundances were taken from Wilms et al. (2000) and cross-sections from Verner et al. (1996). Relative iron abundance were fixed at  $A_{Fe} = 1$ , ionization parameter at  $\xi = 3.2$  and inclination at 35 degrees, in consistency with Miller et al. (2015) results obtained with different spectral models. Although in xillver there is no relativistic broadening of Fe K $\alpha$  emission line no significant residuals in 5-8 keV region are seen, mainly because of limited statistics in per interval spectra. Resulting fits are of satisfactory quality with  $\chi^2_{red.} \approx 1.05$ .

Examination of the best-fit parameters (see Fig.3) confirms that the spectrum softens during the observation and the cut-off energy decreases.

# 4.2.2 Constrains on movement of the inner parts of accretion disk

Spectra of single intervals have not enough statistics to constrain change of Fe-line profile and, hence, to determine whether the disk inner boundary is moving during observation. To increase statistics, we split whole observation into three major pieces, with first made by intervals **I-IV**, second by **V-IX** and third by **X-XIII** and extracted 4–78 keV spectra. We chose to group them in order to have at least 100 counts per bin and then we fitted them (excluding data between 5–10 keV) with simple phabs\*cutoffpl model, using, once again,  $N_H = 2.15 \times 10^{22}$  cm<sup>-2</sup>.

Now, plotting the ratio of this fit to initial spectra (see Fig. 4) one can see that both strong features - i.e. Fe-line complex at 5–9 keV and Compton hump around 30 keV are seemingly stable. Additionally, we estimated the equivalent width of Fe K $\alpha$  emission line in this three parts - we approximated 4–78 keV spectra with 10–30 keV range being ignored (to neglect the Compton-hump contribution) with model consisting of absorbed cut-off powerlaw and gaussian. Equivalent width of the gaussian component is around 0.175 keV and remains constant along the observation within error margins, although it is possible that the quality of data is not enough to trace the real change. Therefore we can

conclude, that there is no drastic change in position of inner disk boundary between parts of observation.

# 4.2.3 Broadband average spectrum

There is a 1.3 ks part of Swift-XRT snapshot (ObsId: 00033203003) that coincides with NuSTAR observation. Extension of an energy range to 0.8–78 keV allows one to search for thermal emission associated with the cold inner disk with  $kT \sim 0.1...0.4$  keV (such as were found in other BHCs, see (Miller et al. 2006a,b; Parker et al. 2015, e.t.c)).

We extracted Swift-XRT spectrum using only zero-grade events, grouped it to has at least 30 counts per bin and added 3% systematic error. Similar grouping were applied to NuSTAR data.

Since the average spectrum has much better statistics we applied more sophisticated relxillp spectral model that describes reflection of emission, produced by point source located on the rotation axis above the Kerr black hole, from the relativistic accretion disk. We used latest available version of relxillp package (v1.0.2). Jet foundation are often thought to be responsible for this type of "lamp-post" geometry. Among the parameters of a model several are of a particular interest, namely h - height of a point source above the black hole illuminating the accretion disk and  $R_{in}$  - disks inner radius. We selected this model for several reasons - first, Miller et al. (2015) found that it matches NuSTAR data well. Also, during the 1996 outburst source was detected at radiowaves, possibly indicating jet activity. For spectral fitting we used migrad minimizer from MINUIT package (James and Roos 1975), and in order to estimate errors we employed a large MCMC chain.

Interestingly, instead of surplus thermal component we found a lack of the soft emission - usage of  $N_H = 2.15 \times 10^{22}$  cm<sup>-2</sup>, measured in the low state (Fürst et al. 2016) led to worse fits with systematic negative residuals below few keV. Therefore, we left  $N_H$  free during the fit. Obtained value of  $2.64 \times 10^{22}$  cm<sup>-2</sup> is higher than one measured by Fürst et al. (2016). This can be possibly accounted to a presence of disk outflow, caused by severe X-ray irradiation.

Obtained upper limit on the accretion disk truncation radius -  $R_{in} < 9GM/c^2$  (90% confidence limit) is similar to the value from Miller et al. (2015), height of the source above the accretion disk is in agreement too (see Tab. 1 for obtained parameters). Some discrepancy seen in the parameters of accretion disk - e.g. inclination, ionization parameter and Fe-abundance, it can be caused by a broader energy range used in this study. As it can be seen from Fig. 5 there are no significant residuals in lower-energy part of the spectrum, therefore thermal emission from accretion disk is too weak or too cold to detect.

Total unabsorbed flux in 0.1–100 keV band is about  $1.4\times10^{-8}~{\rm erg~s^{-1}~cm^{-2}}$  which translates to a luminosity of  $1.1\times10^{38}~{\rm erg~s^{-1}}$  for the 8 kpc distance. Typical luminosity at which BHCs change from LHS to HIMS is about  $0.1L_{Edd}=1.2\times10^{37}(M/M_{\odot})~{\rm erg~s^{-1}},$  although we should note that there is significant scatter in this value. Therefore one can put a rough lower estimate on the black-hole mass as 9  $M_{\odot}$ , which is reasonable.

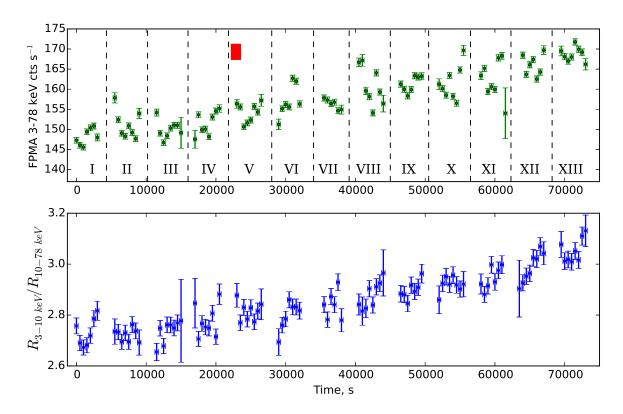


Figure 2. Upper panel: countrate of NuSTAR FPMA in 3–78 keV band. We enumerated intervals of uninterrupted observations with roman numerals. Red square shows time of simultaneous Swift-XRT observation (ObsId: 00033203003, second part). Bottom panel: evolution of hardness during observation

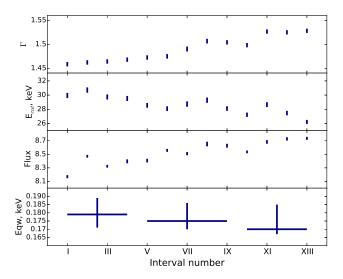


Figure 3. Parameters of continuum emission in intervals. From upper to lower: xillver powerlaw slope, cutoff energy and flux in 3–60 keV band  $\times$  erg s<sup>-1</sup> cm<sup>-2</sup> (see sec.4.2.1). On the botom panel we present Fe  $K\alpha$  line equivalent width obtained with phabs×(cutoffpl + gauss) model (see sec.4.2.2).

# 5 TIMING ANALYSIS

Variability properties of different types of X-ray binary systems are usually described in terms of the power spectrum. The power spectrum of the BHC systems in LHS/HIMS

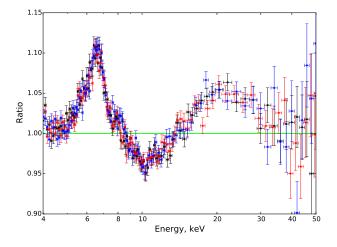


Figure 4. Ratio of NuSTAR FMPA spectra to phabs\*cutoffpl model. In black - data from intervals I-IV, in red from V-IX and in blue from X-XIII.

state can be described typically as a combination of a band-limited noise and one or few narrow Lorentzian functions, representing QPOs (see, e.g., Terrell 1972; Belloni and Hasinger 1990; Homan and Belloni 2005). Properties of these components and correlations between them, in principle, may be used to discriminate between different models of the formation of the X-ray emission in BHC systems.

Although the power spectra analysis is by far the most

Table 1. Best-fit parameters of phabs\*relxilllp model

Parameter	Value		
$N_H, 10^{22} cm^{-2}$	$2.64^{+0.05}_{-0.03}$		
$h, GM/c^2$	$22.3_{-4.3}^{+0.6}$		
$a, cJ/GM^2$	$0.73^{+0.26}_{-0.23}$		
incl, deg	$22.1_{-2.0}^{+2.9}$		
$R_{in}, ISCO$	$1.05^{+1.73}_{-0.02}$		
$\Gamma$	$1.40^{+0.01}_{-0.01}$		
$\log \xi$	$3.52^{+0.05}_{-0.07}$		
$A_{Fe}$	$3.0^{+0.6}_{-0.3}$		
$E_{cut}, keV$	$26.3_{-0.5}^{+0.3}$		
$R_{refl}$	$0.42^{+0.03}_{-0.03}$		
$N_{FMPA}, \times 10^{-2}$	$1.49^{+0.09}_{-0.03}$		
$C_{FMPB}$	$1.017^{+0.002}_{-0.001}$		
$C_{Swift-XRT}$	$1.04^{+0.01}_{-0.01}$		
$\chi^2_{red}$ .	1.1=		
	= 3366.21/3062  d.o.f		

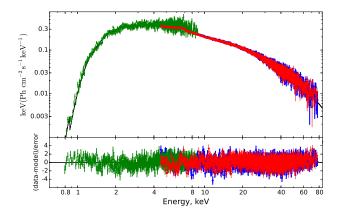


Figure 5. Fit of composite Swift-XRT/NuSTAR spectrum by phabs\*relxilllp model. Green, red and blue points correspond to Swift-XRT, NuSTAR FPMA and FPMB, correspondingly.

popular method for the study of a physical properties of the accretion flow, more sophisticated methods, such as a coherence function or phase-lag were successfully applied as well. In particular, using a measured time-lag between the soft and hard emission, which has a complex behavior with the frequency, Nowak et al. (1999a) constrained a geometrical size of the accretion flow.

In the following section we present results of the analysis of the GRS 1739-278 timing properties and their evolution during the 2014 outburst.

### 5.1 Power spectrum

As it was mentioned above, we splited NuSTAR observation of GRS 1739–278 into 13 continuous intervals separated with  $\sim 0.7$  hr gaps when the source was occulted by Earth. The continuous intervals have a duration about 3 ks (Table 2). Since NuSTAR detectors operate in the photon counting mode, data can be reduced to the lightcurve with the time resolution up to 2  $\mu$ s. For our analysis we extracted lightcurves with the 0.01 s temporal resolution in several

energy bands (3–78, 3–5, 5–8, 8–15, 15–78 keV), which allows us to examine a frequency range of  $\sim 3 \times 10^{-3}$ –50 Hz. This frequency band usually contains low frequency QPOs and a broad band noise (Wijnands and van der Klis 1999). We produced a power spectrum for each interval of the NuSTAR observation using lightcurves in the 3–78 keV energy band. All power spectra have a similar form: a plateau ( $P(f) \propto const$ ) on the low frequencies, transforming at the frequency of  $\approx 0.1$  Hz in to the power law with the slope of  $\rho \approx -1.6..-2.0$  and to the Poisson noise plateau at the frequencies above few Hz. A prominent QPO at the frequencies of 0.3–0.7 Hz and its second harmonic are present as well. Typical power spectrum (with subtracted Poisson noise, see text below) of a single interval is shown in Fig. 6.

In order to quantatively characterize properties of the broad band noise and QPOs we approximate each obtained power spectra with the following analytical function:

$$P(f) = n(1 + (f/f_{lb})^{4})^{\alpha} + \frac{s_{1}}{(f - f_{QPO})^{2} + (f_{QPO}/Q_{m})^{2}} + \frac{s_{2}}{(f - 2f_{QPO})^{2} + (2f_{QPO}/Q_{m})^{2}} + P_{poiss}$$

$$(1)$$

where  $f_{\rm lb}$  is a broad noise break frequency;  $f_{\rm QPO}$  and  $Q_{\rm m}$  -centroid of the QPO and its quality correspondingly (quality of the QPO characterize the broadness of the QPO peak and therefore the stability of the Quasi Periodic process);  $P_{\rm poiss}$  represents mean power of the variations caused by the counting statistics and dumped by the dead-time. In this function first component represents plateau with the break, second two components describe QPO main harmonics and its overtone, last component represents Poisson noise. We take that the quality of the second harmonic of QPO is equal to the QPO quality. In following we will mention this models as standard.

In order to determine properly all parameters one have to know the shape and normalization of the Poission noise component, which depend on the countrate and dead-time and in principle can be described with analytical functions (see, e.g., Vikhlinin et al. 1994; Zhang et al. 1995). NuSTAR detectors are subject to a non-paralyzing dead-time with the characteristic timescale of  $\tau \approx 2.5$  ms (Bachetti et al. 2015). In our case effects from dead-time already can be observed in power spectra at frequencies above 20 Hz. Bachetti et al. (2015) noted that the NuSTAR dead-time has a complex dependence on the energy of registered photons, and therefore it is hard to create an analytical model for the power spectrum of Poisson noise. To avoid this problem they proposed to use a cross-spectrum (or shortly cospectrum) for analysis of NuSTAR data instead of the power spectrum. Authors determine the cospectrum as a real part of the cross product of Fourier function of light-curves obtained from two NuSTAR detectors

$$P(f) \approx \langle re(F_{\text{FPMA}}^*(f)F_{\text{FPMB}}(f)) \rangle$$
 (2)

where P(f) is the estimation of the studied source intrinsic variability power spectrum,  $F_{\text{FPMA}[B]}$  is Fourier function of a light curve from FPMA[B] modules, asterisk \* - stands for complex conjugation. This method is based on the following assumptions: signals produced by an observed source on two detectors are identical and have no time lag

and therefore their Fourier functions are also identical and have zero phase shift; in contrast, signals independent for two detectors (like counting statistics) have random phase shifts. As a sequence for independent signals the average real part of the cross product tends to zero due to the random phase shift, i.e. Poisson noise is eliminated.

Huppenkothen and Bachetti (2017) shown that the cospectrum value in each frequency bin is distributed with the Laplace probability density function (PDF), if it is derived from two normally distributed random independent series (see, e.g., eq. 14 in Huppenkothen and Bachetti 2017):

$$p(C_j|0,\sigma_x\sigma_y) = \frac{1}{\sigma_x\sigma_y} exp\left(\frac{-|C_j|}{\sigma_x\sigma_y}\right)$$
 (3)

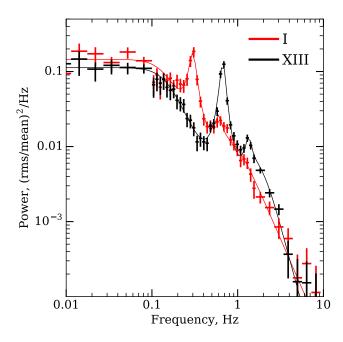
where  $C_j$  is the cospectrum of two uncoherent series measured in the j-th frequency channel and  $\sigma_x$ ,  $\sigma_y$  are second momenta of the initial normal distributions which were combined to produce Laplace distribution. These values  $(\sigma_x, \sigma_y)$ are equal to the square of the power spectra in corresponding frequency channel for each time series). If signals used for the cospectrum estimation have identical power spectra then  $\sigma_x = \sigma_y \approx |F_{\text{FPMA}}|$ . We, therefore, see that to determine proper likelihood function which can be used to approximate cospectra with analytical functions, one still has to know Poisson noise level. It is also worth noting, that source countrate and total countrate are usually slightly differs for two NuSTAR modules making amplitudes of counting-statistic and dead-time not equal. Taking all this arguments into consideration we decided to use standard power spectrum analysis to estimate properties of the source intrinsic variability.

Since we used relatively large time binning (10 ms) to extract lightcurves from NuSTAR data and considered variability at frequencies below 10 Hz (where signal to noise ratio is sufficient), we assumed that the only effect from the dead-time is lowering of the constant Poisson noise level on the factor  $(1 - 2\nu\tau_{\rm d})$ , where  $\nu$  is total count rate for detector and  $\tau_{\rm d}$  is a dead time (Vikhlinin et al. 1994; Zhang et al. 1995). As the dead-time is not constant with the energy, we determined a modified Poisson level for each extracted data-set separately.

We did not consider were any high frequency QPOs, since the typical HF QPO (centroid frequency 100-400 Hz, amplitude  $\approx 10\%$  and quality  $Q \approx 2-10$ ) is indiscernible over the Poisson noise with the obtained count-rate and duration of the observation.

We found that the QPO frequency evolves with time (Table 2 and Fig. 6). It correlates with the NuSTAR flux and photon index, similar to many other black hole and neutron star binary systems (see, e.g., Vignarca et al. 2003; Pottschmidt et al. 2003). The QPO amplitude remained stable during the first half of the observation, and started to grow in the second part.

We also inspected power spectra in soft (3–5 keV) and hard (15–78 keV) energy bands and found that the QPO amplitude is smaller in the soft band, while amplitude of its harmonic is larger. The ratio of the power in the QPO and its harmonic for hard and soft energy bands is presented in Fig. 7. It follows that the QPO profile in time domain, such as was found by Ingram and van der Klis (2015) in GRS 1915+105, differs in the hard and soft X-ray bands.



**Figure 6.** Power spectrum of the GRS 1739–278 obtained with NuSTAR data at the beginning (red crosses) and at the end (black crosses) of the observation. Poisson noise is subtracted.

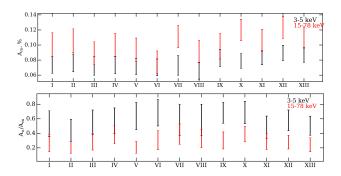


Figure 7. On top panel: amplitude of the QPO harmonic in % of mean countrate, on the bottom panel: ratio of the total power in the QPO and its second harmonic measured for the lightcurves obtained in 3–5 keV and 15–78 keV energy bands.

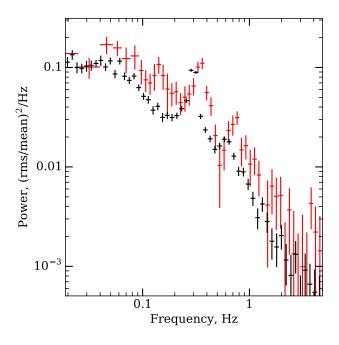
Following Ingram and van der Klis (2015) we tried to extract QPO profile by segregating the coherent part (Fourier signal with conserving phase shift relative to the signal on QPO frequency) between the QPO and its harmonics, however no significant coherence was detected above the noise level. It indicates that the QPO profile was not stable during the observation, in contrast with the result obtained by Ingram and van der Klis (2015) for GRS 1915+105 with RXTE observatory data.

In some intervals QPO subharmonics, centered approximately at 1/2 of the QPO centroid frequency, is clearly observed in the cospectra (see examples on Fig. 8, red crosses) (namely I, II, IV, V, VI sets). In order to observe QPO with better significance we stacked several cospectra, frequency of each cospectrum was scaled in such a way to conserve QPO centroid at 0.3 Hz. Obtained "tracked" cospectrum is pre-

Table 2. Evolution of the Fourier and energy spectrum properties through the NuSTAR observation in the 3-78 keV energy band.

Interval	$T_{start},$ MJD	Expo,	$^{\mathrm{f_{br}},}$ $\times 10^{-2},\mathrm{Hz}$	$\begin{array}{c} f_{\mathrm{QPO}}, \\ \mathrm{Hz} \end{array}$	$Q_{\rm m}$	A <sub>m</sub> ,	A <sub>o</sub> , %	rms %	Γ	$E_{\rm cut},$ ${ m keV}$
I	56742.68	3386	$8.9_{-2.3}^{+2.2}  7.8_{-1.8}^{+2.0}  8.2_{-1.9}^{+2.4}$	$0.30 \pm 0.01$	$15^{+5}_{-3}$	$7.5^{+0.9}_{-1.0}$ $7.9^{+1.0}_{-0.9}$	$2.7^{+0.8}_{-0.9}$	$26 \pm 1$	$1.459 \pm 0.005$	$29.9 \pm 0.4$
II	56742.75	3388	$7.8^{+2.0}_{-1.8}$	$0.31 \pm 0.01$	$13 \pm 3$	$7.9^{+1.0}_{-0.9}$	$2.7^{+0.9}_{-0.9}$ $2.7^{+0.8}_{-0.9}$	$26 \pm 1$	$1.462 \pm 0.005$	$30.7 \pm 0.4$
III	56742.82	3392	$8.2^{+2.4}_{-1.9}$	$0.34 \pm 0.01$	$12^{+3}_{-2}$	$7.7^{+0.9}_{-0.8}$	$3.9^{+0.9}_{-0.8}$	$26 \pm 1$	$1.464\pm0.005$	$29.7 \pm 0.4$
IV	56742.88	3389	$8.3^{+2.0}_{-1.0}$	$0.35 \pm 0.01$	$15^{+4}_{-3}$	$7.6 \pm 0.9$	$3.2^{+0.7}_{-0.8}$	$26 \pm 1$	$1.468\pm0.005$	$29.5^{+0.4}_{-0.3}$
V	56742.95	3389	$6.9^{+1.6}_{-1.4}$	$0.39 \pm 0.01$	$13^{+4}_{-3}$	$7.4 \pm 0.8$	$4.3^{+0.8}_{-0.9}$	$26 \pm 1$	$1.473\pm0.005$	$28.6 \pm 0.3$
VI	56743.02	3136	$7.5^{+1.9}_{-1.5}$	$0.41 \pm 0.01$	$17^{+5}_{-3}$	$6.9_{-0.8}^{+0.9}$	$4.3^{+0.8}_{-0.9}$ $3.8^{+0.7}_{-0.8}$	$26 \pm 1$	$1.475\pm0.005$	$28.1 \pm 0.3$
VII	56743.09	2771	$\begin{array}{c} -1.6 \\ 6.9 + 1.6 \\ -1.4 \\ 7.5 + 1.9 \\ 7.5 - 1.5 \\ 9.7 + 2.7 \\ 9.8 + 1.4 \\ 5.8 + 1.5 \end{array}$	$0.43 \pm 0.01$	$17_{-3}^{+5}  12_{-2}^{+3}  11_{-2}^{+3}$	$7.4 \pm 0.9$	$3.6 \pm 0.9$	$26^{+2}_{-1}$	$1.500\pm0.005$	$28.7 \pm 0.4$
VIII	56743.15	3387	$5.8^{+1.4}_{-1.5}$	$0.46 \pm 0.01$	$11^{+3}_{-2}$	$7.9 \pm 0.9$	$4.2^{+0.9}_{-0.8}$	$27 \pm 2$	$1.507\pm0.005$	$29.3 \pm 0.4$
IX	56743.22	3392	$7.1^{+1.6}_{-1.4}$	$0.50 \pm 0.01$	$12^{+4}_{-2}$	$7.9 \pm 0.8$	$4.3 \pm 0.8$	$26 \pm 1$	$1.504\pm0.005$	$28.1 \pm 0.3$
X	56743.29	3390	$7.0_{-1.6}^{+1.7}$	$0.53 \pm 0.01$	$13^{+3}_{-2}$	$8.7 \pm 0.7$	$4.5^{+0.7}_{-0.8}$	$25 \pm 1$	$1.498\pm0.005$	$27.2 \pm 0.3$
XI	56743.35	3382	$(6.7 \pm 1.5)$	$0.57 \pm 0.01$	$13 \pm 3$	$9.1^{+0.8}_{-0.7}$	$4.0 \pm 0.8$	$25 \pm 1$	$1.527^{+0.004}_{-0.005}$	$28.7 \pm 0.3$
XII	56743.42	3386	$6.7^{+1.8}_{-1.4}$	$0.63 \pm 0.01$	$14^{+3}_{-2}$	$9.5^{+0.8}_{-0.7}$	$4.4 \pm 0.7$	$26^{+2}_{-1}$	$1.525 \pm 0.004$	$27.5 \pm 0.3$
XIII	56743.49	3391	$6.7_{-1.4}^{+1.8} \\ 7.5_{-1.5}^{+1.7}$	$0.67 \pm 0.01$	$15\pm3$	$9.6 \pm 0.7$	$4.2\pm0.8$	$25^{+2}_{-1}$	$1.528\pm0.004$	$26.2 \pm 0.3$

In Table  $f_{\rm br}$  is broad band noise break frequency,  $f_{\rm QPO}$  is QPO centroid frequency,  $Q_{\rm m}$  is QPO main harmonic quality (ratio of its centroid frequency to its width),  $A_{\rm m}$  - total power in the QPO main harmonic in % of mean countrate,  $A_{\rm m}$  is total power in the QPO second harmonic in % of mean countrate, rms - total amplitude of variations in the % of mean countrate,  $\Gamma$  - powerlaw photon index,  $E_{\rm cut}$  - powerlaw cutoff energy. Parameters  $\Gamma$  and  $E_{\rm cut}$  were obtained from spectra of individual intervals with *xillver* model (see sec.4.2.1).



**Figure 8.** Cross-spectrum of the observations, obtained by scaling frequency to conserve QPO position. Black crosses obtained from the all intervals, while red crosses are from interval IV in which QPO subharmonics was most prominent.

sented on Fig. 8. The subharmonics seems to roam around the 1/2 QPO frequency, therefore we were not able to obtain it with a large significance on the tracked cospectrum.

It should be noted that the changes in the QPO centroid position during the interval may contribute to the observed quality factor Q. We can estimate the derivative of the QPO centroid position with time (by approximating  $f_{\rm QPO}(time)$ 

with the straight line), which appears to be  $\dot{f}_{\rm QPO} \approx 5.0$  $6.5 \times 10^{-6}$  Hz s<sup>-1</sup>. During an interval with the duration  $\tau = 3000 \text{ s}$  observed QPO drift will broaden the perfect periodic signal located at  $f_{\rm QPO}=0.3~{\rm Hz}$  up to the quality factor  $Q \approx f_{\rm QPO}/(f_{\rm QPO}\tau) \approx 17$ , which is of order of the Q estimations obtained from the observations with standard model (described with eq.1). In order to better estimate the QPO quality factor, we split each of the 13 intervals in sets of 82 s long time-series. After that, for each of 13 intervals, we fitted obtained power spectra simultaneously with new model in which we assume that QPO frequency linearly growing with time. The model has the same form as standard with  $f_{\rm QPO}$ substituted with  $f'_{\rm QPO} = f_{\rm QPO} + (t - t_{\rm mid}) \dot{f}_{\rm QPO}$ , where  $\dot{f}_{\rm QPO}$  is the free parameter and  $t_i^{\rm mid}$ ,  $f_{\rm QPO}$  are the middle time of the *i*-th 82 s interval and QPO centroid frequency measured with standard model correspondingly. Inside each data set we obtained the QPO centroid changing speed consistent with the estimation obtained from the general trend ( $\approx 2$ - $9 \times 10^{-6} \text{ Hz s}^{-1}$ ), nevertheless the median quality factor, obtained in this model appears to be  $\sim 14.3$  - i.e. compatible with the previous estimations made with standard model (see Table 2). It should be noted that the estimation of the QPO quality factor is restricted by the width of fast Fourier transform frequency bins, which is 1/T, where T - is a duration of separate series used for fitting, in our case T = 82 s, and QPO width is limited at 1/T = 0.012 Hz (we can not discriminate Q > 25).

From the shape of the energy and Fourier spectrum we concluded that the system is in the hard intermediate state and observed low frequency QPO (LF QPO) is of type C.

# 5.2 Coherence

Vaughan and Nowak (1997)(hereafter VN97) suggested to use the coherence between different energy bands in order to obtain additional information from the source variability.

The coherence measure the similarity between two signals and can be computed with the following expression:

$$C(f) = \frac{|\langle F_{s}(f)^{*}F_{h}(f)\rangle|^{2} - n^{2}}{P_{s}(f)P_{h}(f)}$$
(4)

where  $F_h(f)$  and  $F_s(f)$  are Fourier function of the observed time series in hard and soft bands, correspondingly,  $P_s(f)$  and  $P_h(f)$  is estimation of their power density spectra (derived, for example, with the Equation 2),  $n^2$  - product of the power in the uncorrelated noise components divided by the number of used series (which mostly determined by Poisson statistics noise, see VN97). Since the coherence is estimated as a mean product of the Fourier functions it should be computed for the number of independent time series, therefore we separated each of the available uninterrupted time intervals on several shorter parts, 82 s long each.

Different models of the XRBs variability generation suggest that signals in two energy bands can be partially independent, while the shape of the power spectra is conserved. It appears that in many sources the coherence between soft and hard X-ray bands is close to unity (Nowak et al. 1999a; Wijnands and van der Klis 1999), however there were also indications on complex picture of the coherence in particular state of some systems (dip in the coherence at 0.03 Hz frequency, observed in GRS1915+105, Ji et al. 2003), (decreasing of the coherence between particular energy bandse in GX 339-4, Vaughan and Nowak 1997). See also discussion in the VN97 for the theoretical prediction on the coherence for different models.

Following VN97, we estimated the coherence of GRS 1739-278 light-curves obtained in different soft and hard energy bands. Since we use NuSTAR data (covering 3-79 keV energy band) we adopted following energy bands for our analysis: 3-5 keV, 5-8 keV, 8-15 keV and 15-78 keV. This partition of the NuSTAR energy band pursues the following idea: the energy spectrum of GRS 1739–278 can be described with two major components - powerlaw continuum and reflection features i.e. the fluorescent Fe K $\alpha$  line and the Compton hump. In the 5-8 kev band there is a contribution of the prominent Fe K $\alpha$  line, with the equivalent width of 0.2 keV it provides about 5% of the flux in this band. In the 8-15 keV energy band we expect only the power law component to be present. Compton hump, another reflection feature, is confined in the 15–78 kev energy band.

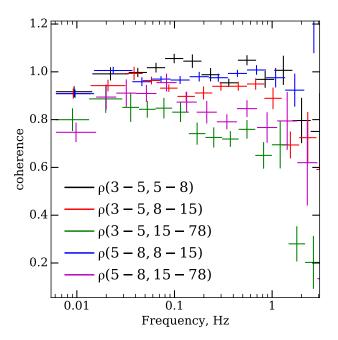
As it was mentioned above the NuSTAR detectors have a complex dead-time depending on the energy, the coherence computed from one detector is subject to the dead-time cross-talk effects (i.e. capturing of the photon in particular energy band prevents registration of any next photon arriving during the dead-time, see e.g.?). Such cross-talk makes more coherent random processes, independent in different energy channels. In order to eliminate these effects in coherence estimation we follow the recipe suggested by Bachetti et al. (2015) for the cospectrum estimation. As explained in (Bachetti et al. 2015) we can take advantage of the presence of two detectors modules, signals from which are processed independently. That means that the photon registered by one of the modules do not prevent registration of the photon arriving during the dead-time in another module. Therefore, for the numerator in Eq 4 (cross product of the Fourier functions of the light-curves obtained in different energy bands) we use light-curves obtained from different modules - e.g. lightcurve obtained in soft band on FPMA with one obtained in hard band on FPMB and vice versa.

To obtain proper estimation on the coherence it is also important to have the correct estimation of the intrinsic variability power spectrum (denumenator in Eq. 4). We use in this work model independent approach, with the cospectrum used for the power spectrum estimation (another approach would be to use Poisson noise subtracted power spectrum or analytical function fitted to the power spectrum in the previous section).

The  $n^2$  component was computed as it is suggested by VN97. We estimated Poisson noise level as a mean power in the 5–15 Hz range, in this frequency band Poisson noise dominating over the source intrinsic variability, while its shape already not affected by the dead-time effects (the spectrum is flat below 15 Hz).

By using the cospectrum for the intrinsic variability power spectrum estimation we introduce one drawback. As was discussed in the previous section cospectrum can be described with Laplace statistics, which have non-zero probability density in the vicinity of zero and positive mean value. Therefore, if insufficient number of samples are used to calculate the mean of the cospectrum than the enormous statistical errors would be introduce in the coherence (since the cospectrum is used in the denominator in its estimation). The number of the samples is limited by the total duration of the observation and the condition that the shape of the cospectrum should not changing significantly in used samples (otherwise artificial dispersion would be introduced in the cospectrum distribution). The last criterion appears to be more strict one, since the QPO and break frequencies are changed by a factor of two during the observation. In order to increase statistical significance of the estimated cospectrum we use the following property found to be inherent for the XRBs intrinsic variability. Wijnands and van der Klis (1999) shown that primary features of the power spectrum of the XRBs in low-hard and high intermediate states are evolving simultaneously, i.e. the break frequency of the flat top broad band noise and the QPO centroid frequency are connected with the relation  $f_b \approx 0.3 f_{\rm QPO}$ . Bearing in mind this property of the power spectrum and small scatter in the  $f_{\rm b}/f_{\rm QPO}$  in our data, we stacked all 13 separate intervals of the observation, scaling their frequencies to preserve QPO position. We assumed that the coherence in each tracked frequency channel is preserved along the observation and scaled in the similar way.

The coherence between hard and soft energy bands at frequencies up to  $\sim 3$  Hz is presented in Fig. 9. We found that the coherence in the adjacent energy bands is close to unity, with mean values in 0.01–1 Hz frequency band being 1.0  $\pm$  0.05. However for the 3–5 and 15–78 keV energy bands the coherence is significantly lower (Fig. 9). It is on the nearly constant level of  $\approx 0.85$  in the (0.005–0.1) Hz frequency band and drops down above this frequency. Analogous behavior was observed in GX 339–4 (VN97), in this work authors also discussed possible mechanisms which could lead to such loss of coherence between different energy bands. Two main possibilities discussed by VN97 were a) nonlinear transfer function between soft and hard bands and b) contribution of several coherent (within



**Figure 9.** Coherence between lightcurves extracted in different energy bands: black, red, green, blue and magenta are for (3–5, 5–8), (3–5, 8–15), (3–5, 15–78), (5–8, 8–15) and (5–8, 15–78) correspondingly.

two energy bands) but independent processes in each energy band. Both this scenarios can take place along with the model of propagating fluctuations, considered in this work. First one would have require nonlinear process in the formation of the soft and hard emission, and the second require spatial separation of the soft and hard emission regions along the accretion flow.

# 5.3 Phase lags

From the definition of the coherence (see eq. 4) it follows that signals have roughly constant phase shifts between their Fourier functions in each frequency bin where they are coherent. Following VN97 to estimate the phase lag one have to calculate mean of the product of the Fourier function obtained in one energy band to the conjugated Fourier function estimated in second energy band, the phase of the obtained complex value would be the phase lag.

$$\delta\phi(f) = \arctan\left(\frac{Im(\langle F_{\rm s}(f)F_{\rm h}^*(f)\rangle)}{Re(\langle F_{\rm s}(f)F_{\rm h}^*(f)\rangle)}\right)$$
 (5)

Where Im and Re are stated for the imaginary and real part of the complex value correspondingly and  $\delta\phi(f)$  if the frequency dependent phase lag. For the uncertainty estimation we used approach proposed by Uttley et al. (2014), therefore  $\Delta\delta\phi\approx\arctan\left(\Delta C(f)/C(f)\right)$ , where C(f) - estimation of the coherence, and  $\Delta C(f)$  is the coherence uncertainty estimation.

The phase lags observed for different systems had features, which correlated with the power spectrum and those which had not obvious counterpart in it. Therefore, bearing in mind property of the linear evolution of all frequencies of the power spectra discussed in previous section, we computed the phase lag spectrum with two approaches - with and without the QPO centroid frequency tracing (see right and left panels of Fig.10, correspondingly). Obtained phase lags appears to be surprisingly similar, however those calculated with the traced QPO frequency are seem to have larger amplitude on the lower frequencies, which may indicate that phase lags are indeed evolves in a similar way with the power spectrum. It appears that in the 0.1–3 Hz frequency band positive (hard) lag is present while at frequencies below 0.1 Hz there are indication of the negative (soft) lag. Observed phase lag corresponds to the delay times between soft and hard photons  $\sim 0.1~\rm s$  for frequencies above 0.1 Hz and  $-0.1..-1~\rm s$  for frequencies below 0.1 Hz.

The phase lag in different BHC system was being investigated by many authors (see, e.g. Vaughan and Nowak 1997; Malzac et al. 2003; Reig et al. 2006; Gandhi et al. 2010; Böck et al. 2011; Muñoz-Darias et al. 2011; Cassatella et al. 2012; Méndez et al. 2013; Yan et al. 2017; De Marco et al. 2017; Zhang et al. 2017; van den Eijnden et al. 2017; Reig et al. 2018). It was found that for stellar mass black holes the phase lag in the frequency range occupied by the flat-top noise and LF QPOs is usually hard and can be described with the power law  $\Delta \phi/(2\pi f) = \Delta \tau \propto$  $f^{-0.7}$  with thin wide dips pikes at the QPO and its harmonics frequencies. Zhang et al. (2017) shown that the phase lag at the QPO frequency and its second harmonic in GX 339-4 BHC evolves with this frequency.

First example of  $\Delta \tau \propto f^{-0.7}$  behavior was found by Miyamoto and Kitamoto (1989) in Cyg X-1 and later investigated with the better resolution based on the RXTE observatory data by Nowak et al. (1999a). Miyamoto and Kitamoto (1989) tried to explain observed lags with the clumpy flow model, which previously was used to explain an observed shape of the flat-top noise Fourier spectrum. Nowak et al. (1999b) considered two models, promising to explain observed hard lags and their dependence on frequency - i.e. phase lags are formed due to Comptonization in the extended corona or they formed due to the propagation of the perturbations in the advection flow. They found that it is hard to explain observed phase lags with both models, with first demanding very extended corona ( $\sim 150R_{\rm g}$  and second - very slow matter propagation speed in it. Later Kotov et al. (2001) considered their result and, on the basis on the amplitude and energy dependence of the hard lag, derived that it can not be caused by the reverberation and is most preferably due to the perturbation propagation in the corona on the viscous time scales (see also Arévalo and Uttley 2006, on simulations results). It is worth mentioning, that proposed models are generally can explain hard lags but fail in explaining soft lags, which were later found in many source both on low and high frequencies (below and above flat-top noise break frequency) to mention a few (Gandhi et al. 2010; Cassatella et al. 2012; Yan et al. 2017; van den Eijnden et al. 2017). However, it was demonstrated that the soft lags are possible in the propagation fluctuation model if outward movement of the disk surface

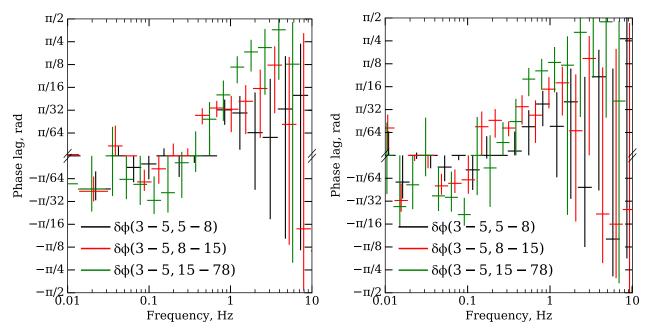


Figure 10. Phase lag between the soft (3–5 keV) and hard (5–8; 8–15; 15–78 keV) energy bands in GRS 1739–278. On the left panel phase lag spectrum obtained from *NuSTAR* observations by stacking all data, on the right panel same spectrum with tracked frequency (frequency for each separate light-curve segment was scaled such a way to conserve QPO centroid at 0.3 Hz).

Table 3. QPOs detected in Swift-XRT observations

Segment	$t_{mean}$	$f_{QPO}$ , Hz	QPO rms, %	Total rms, %	Туре
	days from $\tau_0$	• •			
03	17.9	$0.37 \pm 0.01$	$9 \pm 2$	$28 \pm 3$	С
04	21.9	$2.17 \pm 0.03$	$8^{+1}_{-2}$	$14^{+2}_{-1}$	В
05	26.8	$1.67^{+0.03}_{-0.04}$	$8\pm 1$	$17^{+6}_{-3}$	В
06	31.8	$5.05 \pm 0.09$	$4^{+2}_{-1}$	$11^{+2}_{-1}$	В
07	36.0	$2.52^{+0.07}_{-0.08}$	$7^{+1}_{-2}$	$15^{+\frac{3}{2}}_{-2}$	В
08	39.8	$5.10^{+0.16}_{-0.14}$	$5\pm 1$	$12^{+3}_{-2}$	В
09	46.6	$2.17^{+0.02}_{-0.04}$	$7^{+2}_{-1}$	$17^{+\frac{7}{4}}_{-3}$	В

density perturbations due to viscous evolution are also considered (Mushtukov et al. 2017). Reig et al. (2018) found that the mean time lag strongly correlates with photon index of power law continuum, with the time lag increasing with decreasing hardness. They proposed, that observed behavior can be explained with the Comptonization of soft photons by energetic electrons in a jet. van den Eijnden et al. (2017) found that the sign and amplitude of the phase lag at the QPO frequency depends on a system inclination.

Considering phase lags obtained in this work, in the frequency range, where phase lags are positive they can be described with  $\Delta\phi/f\propto f^{-0.7}$  relation, which breaks at  $\sim 0.1$  Hz, below which lags are negative. Unfortunately, due to insufficient signal to noise ratio, we can not determine, are there any specific features present at the QPO or its second harmonic centroid frequencies. Obtained phase lag dependence can be considered as quite standard for BHC.

# 5.4 Swift-XRT observations

We performed search for LF QPOs in first dozen of Swift-XRT observations of the GRS 1739–278. QPO is clearly detected in observations 3 to 9, with frequency varying from 0.37 Hz (during simultaneous observation with NuSTAR, see Fig. 2) up to 5.1 Hz (see Tab. 3). Last detection of QPO happened right before the onset of a strong flaring, at  $\tau_0 + 46.6$ .

We used the shape of power spectra in order to classify QPOs as belonging to type C or B (Casella et al. 2005). In all observations except for the observation 03, low frequency parts of power spectra can be described with weak red noise, which typically accompanies type-B QPOs. In order to reinforce classification we calculated rms for each detected QPO, along with total rms over 0.01–20 Hz band. Obtained  $rms_{total}$  are significantly lower for observations 04..09 than for 03. We, therefore, conclude that in observations 04..09 type-B QPOs were observed with frequencies ranging from  $\sim$ 2 Hz to 5 Hz. It follows, that four days after the NuS-TAR observation, the source already had transitioned from

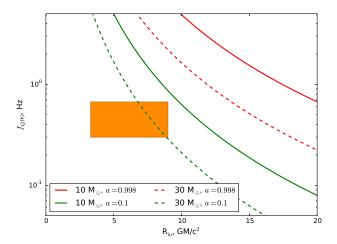


Figure 11. Expected QPO frequency for a black hole of a given mass and spin versus the disk inner radius from Ingram and Motta (2014). The orange square represents region containing observed QPOs.

HIMS to SIMS and resided in this state until 09 Swift-XRT observation.

# 6 DISCUSSION AND CONCLUSIONS

We had studied NuSTAR observation carried out during the transition between soft and hard state. We had studied the spectro-timing evolution of GRS 1739-278 during its hardintermediate state. We found a prominent type-C LF QPO in its power spectrum, its frequency show clear correlation with the parameters of continuum emission. As the QPO frequency increases from 0.3 to 0.7 Hz spectrum became softer: the power law index grows from 1.46 to 1.53 and cut-off energy decreases from 30 to 26 keV. Overall flux increases, too. Such behaviour was first observed in a number of systems by Di Matteo and Psaltis (1999) and now it is studied in greater details in many systems (see e.g. Vignarca et al. 2003; Stiele et al. 2013; Seifina et al. 2014; Fürst et al. 2016, and many more). Although the quality of the data prevented us from measuring a movement of the inner disk boundary, from the total broadband energy spectrum we found that an accretion disk is truncated at the radius smaller than 9  $GM/c^2$  (90% confidence limit) which is in agreement with an estimates by Miller et al. (2015). We used this combination of inner radius and QPO together with Lense-Thirring precession model of QPO origin (Ingram et al. 2009) in order to assess black hole mass. Following Ingram and Motta (2014) we calculated nodal frequencies (which is though to correspond to the QPO fundamental frequency) versus the inner radius for two values of the black hole mass ( $10M_{\odot}$  and  $30M_{\odot}$ ) and two values of the spin - a=0.1 and a=0.998(maximally rotating). As it can be seen from Fig. 11 observations are incompatible with the black hole mass  $10M_{\odot}$  and barely agrees with the slowly rotating massive black hole. This results, along with the measurements by Fürst et al. (2016), indicates that there are some tensions between the predictions of RPM and the truncation radii inferred from the spectral fitting.

We carried out an extensive study of the timing properties of GRS 1739–278. Along with the broadband noise and fundamental QPO, the second harmonic of the QPO is clearly seen. During several intervals from first half of the observation subharmonic is also observed. In all 13 intervals second QPO harmonic is more prominent in soft band (3–5 keV), with ratio of its amplitude to that of fundamental QPO being  $0.565\pm0.02$  in 3–5 keV band versus  $0.275\pm0.02$  in 15–78 keV. We also measured the velocity of the QPO drift and found it to be  $\approx 6.0\times10^{-6}~{\rm Hz~s^{-1}}$ .

We searched for similar QPO in Swift-XRT observations of GRS 1739–278 performed after NuSTAR exposure and found that all other detected QPOs are probably of type B, thus the source transitioned to soft-intermediate state few days after NuSTAR observation.

Coherence measured between adjacent energy ranges in 0.01-1 Hz was found to be nearly unity, while for the softest used energy band (3–5 keV) and the hardest energy band (15–78 keV) coherence turned out to be lower, with plateau breaking at 0.1 Hz . In the frame of the propagating fluctuations model it can be explained with the nonlinear process of the formation of soft and hard emission or with the separation of zones producing soft and hard emission along the accretion flow.

Phase lag found to be of order of +0.1 s (hard) in the 0.1–3 Hz frequency range and -1...-0.1 s (soft) below 0.1 Hz. van den Eijnden et al. (2017) shown that the sign of the phase lag at the type-C QPO centroid frequency depends on a system inclination, however this difference is explicit only when the QPO centroid frequency is above  $\sim 3$  Hz, therefore we were not able to restrict GRS 1739–278 system inclination.

We also may use (?) diagram, demonstrating observed dependence between the QPO and flat-top break frequency for the different objects. On this diagram massive objects are located in the bottom left corner, having smaller QPO and break frequencies.

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