

# Modelling and simulation

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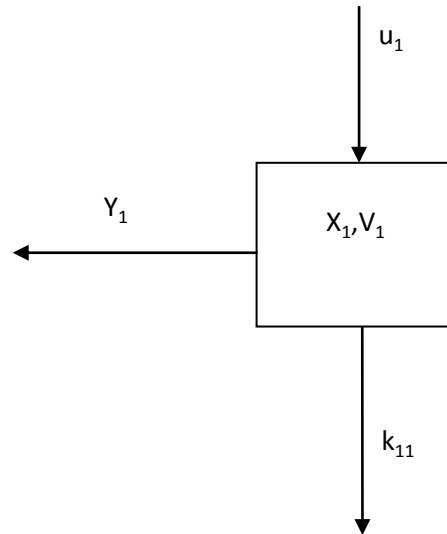
Practice: Daniela Müllerová



# Sensitivity analysis of model

- Sensitivity analysis aims to find an optimal experiment, which could provide the best measurement of a physiological process.
- Sensitivity analysis ensures that the quality of the measured data is sufficient to identify the model parameters.
- Sensitivity analysis can be carried out by direct differentiation of model output (eg, drug concentration or amount), with respect to the parameter of interest.

# 1-compartmental model



Differential equations

$$\dot{X}_1 = -k_{11} \cdot X_1 + u_1$$
$$Y_1 = \frac{1}{V_1} \cdot X_1$$

State space notation

$$X = [X_1] \quad Y = [Y_1] \quad U = [u]$$
$$A = [-k_{11}]$$
$$B = [1]$$
$$C = \left[ \frac{1}{V_1} \right]$$

# 1-compartmental model

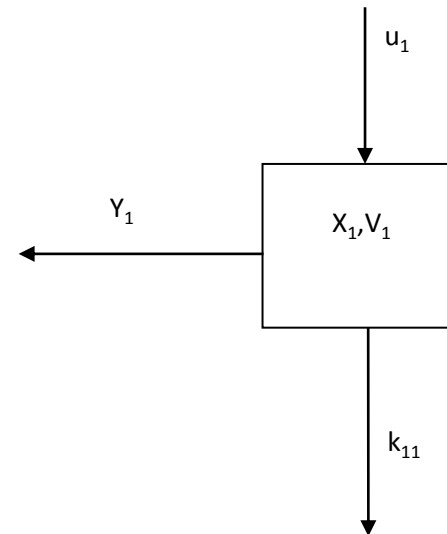
Sensitivity equations

$$\dot{\lambda} = A \cdot \lambda + H \cdot X$$
$$\eta = C \cdot \lambda + V \cdot X$$

Sensitivity matrix

$$H_1 = \frac{\partial A}{\partial k_{11}} = [-1]$$
$$H_2 = \frac{\partial A}{\partial V_1} = [0]$$

$$V_1 = \frac{\partial C}{\partial k_{11}} = [0]$$
$$V_2 = \frac{\partial C}{\partial V_1} = \left[-\frac{1}{V_1^2}\right]$$



**$K_{11}$ :**

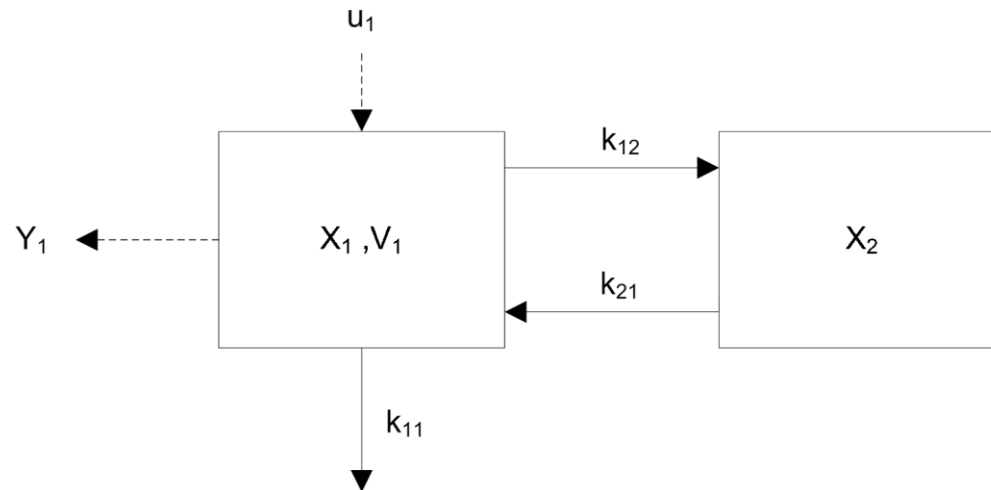
$$\dot{\lambda} = -k_{11} \cdot \lambda - x_1$$
$$\eta = \frac{\lambda}{V_1}$$

**$V_1$ :**

$$\dot{\lambda} = -k_{11} \cdot \lambda$$
$$\eta = \frac{\lambda}{V_1} - \frac{x_1}{V_1^2}$$

# Practice 2 - assignment

- 2-compartmental model



# Practice 2 - assignment

- Compose sensitivity analysis
  - ☐ Define differential equations of the model
  - ☐ Define matrix A, B, C, D
  - ☐ Define sensitivity equations
  - ☐ Define sensitivity matrix
- Compose model in Simulink
  - ☐ Model parameters ( $k_{12}=0.7$  mg/h,  $k_{11}=0.8$  mg/h,  $k_{21}=0.9$  mg/h,  $V_1=5$ l,  $u(0)=200$  mg)
  - ☐ Including sensitivity of model parameters

# Practice 2 – desired output

- Model file \*.mdl with correctly described blocks
- Short paper in \*.pdf containing
  - Block diagram of the model
  - Definition equation model
  - Matrices A, B, C, D
  - Sensitivity equations
  - Sensitivity matrix
  - Graphical output of the simulation – sensitivity analysis for state X and output Y with respect model parameters, outputs of model (amount, concentration).