

Modeling and Simulation of the Cardiovascular System – Michel Kana, PhD

SS2010

Task is to model each equation in a single subsystem and put all subsystems together in a Simulink model.

Conservation of Mass at Pulmonary Arteries

$$\frac{dP_{pa}}{dt} = \frac{1}{C_{pa}} (F_{o,r} - F_{pa}) \quad (A1.1)$$

Balance of Forces at Pulmonary Arteries

$$\frac{dF_{pa}}{dt} = \frac{1}{L_{pa}} (P_{pa} - P_{pp} - R_{pa} \times F_{pa}) \quad (A1.2)$$

Conservation of Mass at Pulmonary Peripheral Circulation

$$\frac{dP_{pp}}{dt} = \frac{1}{C_{pp}} (F_{pa} - \frac{P_{pp} - P_{pv}}{R_{pp}}) \quad (A1.3)$$

Conservation of Mass at Pulmonary Veins

$$\frac{dP_{pv}}{dt} = \frac{1}{C_{pv}} \left(\frac{P_{pp} - P_{pv}}{R_{pp}} - \frac{P_{pv} - P_{la}}{R_{pv}} \right) \quad (A1.4)$$

Conservation of Mass at Systemic Arteries

$$\frac{dP_{sa}}{dt} = \frac{1}{C_{sa}} (F_{o,l} - F_{sa}) \quad (A1.5)$$

Balance of Forces at Systemic Arteries

$$\frac{dF_{sa}}{dt} = \frac{1}{L_{sa}} (P_{sa} - P_{sp} - R_{sa} \times F_{sa}) \quad (A1.6)$$

Conservation of Mass at Peripheral Systemic Circulation

$$\frac{dP_{sp}}{dt} = \frac{1}{C_{hp} + C_{bp} + C_{mp} + C_{sp} + C_{ep}} \left(F_{sa} - \frac{P_{sp} - P_{hv}}{R_{hp}} - \frac{P_{sp} - P_{bv}}{R_{bp}} - \frac{P_{sp} - P_{mv}}{R_{mp}} - \frac{P_{sp} - P_{sv}}{R_{sp}} - \frac{P_{sp} - P_{ev}}{R_{ep}} \right) \quad (A1.7)$$

Conservation of Mass at Heart Veins

$$\frac{dP_{hv}}{dt} = \frac{1}{C_{hv}} \left(\frac{P_{sp} - P_{hv}}{R_{hp}} - \frac{P_{hv} - P_{ra}}{R_{hv}} \right) \quad (A1.8)$$

Conservation of Mass at Brain Veins

$$\frac{dP_{bv}}{dt} = \frac{1}{C_{bv}} \left(\frac{P_{sp} - P_{bv}}{R_{bp}} - \frac{P_{bv} - P_{ra}}{R_{bv}} \right) \quad (A1.9)$$

Conservation of Mass at Muscle Veins

$$\frac{dP_{mv}}{dt} = \frac{1}{C_{mv}} \left(\frac{P_{sp} - P_{mv}}{R_{mp}} - \frac{P_{mv} - P_{ra}}{R_{mv}} - \frac{dV_{u,mv}}{dt} \right) \quad (A1.10)$$

Conservation of Mass at Splanchnic Veins

$$\frac{dP_{sv}}{dt} = \frac{1}{C_{sv}} \left(\frac{P_{sp} - P_{sv}}{R_{sp}} - \frac{P_{sv} - P_{ra}}{R_{sv}} - \frac{dV_{u,sv}}{dt} \right) \quad (A1.11)$$

Conservation of Mass at Extrasplanchnic Veins

$$P_{ev} = \frac{1}{C_{ev}} \left[\begin{array}{l} V_{tot} - C_{sa}P_{sa} - (C_{hp} + C_{bp} + C_{mp} + C_{sp} + C_{ep})P_{sp} \\ -C_{bv}P_{bv} - C_{hv}P_{hv} - C_{mv}P_{mv} - C_{sv}P_{sv} \\ -C_{ra}P_{ra} - V_{rv} - C_{pa}P_{pa} - C_{pp}P_{pp} - C_{pv}P_{pv} \\ -C_{la}P_{la} - V_{lv} - V_u \end{array} \right] \quad (A1.12)$$

$$V_u = \left[\begin{array}{l} V_{u,sa} + V_{u,hp} + V_{u,bp} + V_{u,mp} + V_{u,sp} + V_{u,ep} \\ +V_{u,hv} + V_{u,bv} + V_{u,mv} + V_{u,sv} + V_{u,ev} \\ +V_{u,ra} + V_{u,pa} + V_{u,pp} + V_{u,pv} + V_{u,la} \end{array} \right]$$

Conservation of Mass at Left Atrium

$$\frac{dP_{la}}{dt} = \frac{1}{C_{la}} \left(\frac{P_{pv} - P_{la}}{R_{pv}} - F_{i,l} \right) \quad (A1.13)$$

Blood flow entering left ventricle

$$F_{i,l} = \begin{cases} 0 & \text{if } P_{la} \leq P_{lv} \\ \frac{P_{la} - P_{lv}}{R_{la}} & \text{if } P_{la} > P_{lv} \end{cases} \quad (A1.14)$$

Conservation of Mass at left Ventricle

$$\frac{dV_{lv}}{dt} = F_{i,l} - F_{o,l} \quad (A1.15)$$

Cardiac Output From Left Ventricle

$$F_{o,l} = \begin{cases} 0 & \text{if } P_{\max,lv} \leq P_{sa} \\ \frac{P_{\max,lv} - P_{sa}}{R_{lv}} & \text{if } P_{\max,lv} > P_{sa} \end{cases} \quad (A1.16)$$

Viscous Resistance of Left Ventricle

$$R_{lv} = k_{R,lv} \times P_{\max,lv} \quad (A1.17)$$

Instantaneous Left Ventricle Pressure

$$P_{\max,lv}(t) = \varphi(t) \times E_{\max,lv} \times (V_{lv} - V_{u,lv}) + (1 - \varphi(t)) \times P_{o,lv} \times (e^{k_{E,lv} \times V_{lv}} - 1) \quad (A1.18)$$

$$\varphi(t) = \begin{cases} \sin^2 \left[\frac{\pi \times T(t)}{T_{sys}(t)} \times u \right] & 0 \leq u \leq \frac{T_{sys}}{T} \\ 0 & \frac{T_{sys}}{T} \leq u \leq 1 \end{cases}$$

$$u(t) = \text{frac}(\xi) = \text{abs}(\xi - \text{round}(\xi)) \quad (\text{A1.19})$$

$$\frac{d\xi}{dt} = \frac{1}{T(t)}$$

$$T_{sys} = T_{sys,0} - k_{sys} \times \frac{1}{T}$$

Conservation of Mass at Right Atrium

$$\frac{dP_{ra}}{dt} = \frac{1}{C_{ra}} \left(\frac{P_{hv} - P_{ra}}{R_{hv}} + \frac{P_{bv} - P_{ra}}{R_{bv}} + \frac{P_{mv} - P_{ra}}{R_{mv}} + \frac{P_{sv} - P_{ra}}{R_{sv}} + \frac{P_{ev} - P_{ra}}{R_{ev}} - F_{i,r} \right) \quad (\text{A1.20})$$

Blood flow entering right ventricle

$$F_{i,r} = \begin{cases} 0 & \text{if } P_{ra} \leq P_{rv} \\ \frac{P_{ra} - P_{rv}}{R_{ra}} & \text{if } P_{ra} > P_{rv} \end{cases} \quad (\text{A1.21})$$

Conservation of Mass at Right Ventricle

$$\frac{dV_{rv}}{dt} = F_{i,r} - F_{o,r} \quad (\text{A1.22})$$

Cardiac Output From Right Ventricle

$$F_{o,r} = \begin{cases} 0 & \text{if } P_{\max,rv} \leq P_{pa} \\ \frac{P_{\max,rv} - P_{pa}}{R_{rv}} & \text{if } P_{\max,rv} > P_{pa} \end{cases} \quad (\text{A1.23})$$

Viscous Resistance of Right Ventricle

$$R_{rv} = k_{R,rv} \times P_{\max,rv} \quad (\text{A1.24})$$

Instantaneous Right Ventricle Pressure

$$P_{\max,rv}(t) = \varphi(t) \times E_{\max,rv} \times (V_{rv} - V_{u,rv}) + (1 - \varphi(t)) \times P_{o,rv} \times (e^{k_{E,rv} \times V_{rv}} - 1) \quad (\text{A1.25})$$

Baroreceptors

$$f_{ab} = \frac{f_{ab,\min} + f_{ab,\max} \times e^{\frac{\tilde{P} - P_n}{k_{ab}}}}{1 + e^{\frac{\tilde{P} - P_n}{k_{ab}}}}$$

$$k_{ab} = \frac{f_{ab,\max} - f_{ab,\min}}{4 \times G_b} \quad (\text{A1.26})$$

$$\tau_{pb} \times \frac{d\tilde{P}}{dt} = P_{sa} + \tau_{zb} \times \frac{dP_{sa}}{dt} - \tilde{P}$$

$$\begin{aligned}\frac{df_{ac}}{dt} &= \frac{1}{\tau_c} \times (-f_{ac} + \varphi_{ac}) \\ \varphi_{ac} &= \frac{f_{ac,\max} + f_{ac,\min} \times e^{\frac{P_{asO_2} - P_{asO_{2n}}}{k_{ac}}}}{1 + e^{\frac{P_{asO_2} - P_{asO_{2n}}}{k_{ac}}}}\end{aligned}\quad (0.0.27)$$

$$\begin{aligned}\frac{df_{ap}}{dt} &= \frac{1}{\tau_p} \times (-f_{ap} + \varphi_{ap}) \\ \varphi_{ap} &= G_{ap} \times V_T\end{aligned}\quad (0.0.28)$$

$$\begin{aligned}f_{sp} &= \begin{cases} f_{es,\infty} + (f_{es,0} - f_{es,\infty}) \times e^{k_{es} \times (-W_{b,sp} \times f_{ab} + W_{c,sp} \times f_{ac} - W_{p,sp} \times f_{ap} - \theta_{sp})} & \text{if } f_{sp} < f_{es,\max} \\ f_{es,\max} & \text{if } f_{sp} \geq f_{es,\max} \end{cases} \\ f_{sh} &= \begin{cases} f_{es,\infty} + (f_{es,0} - f_{es,\infty}) \times e^{k_{es} \times (-W_{b,sh} \times f_{ab} + W_{c,sh} \times f_{ac} - \theta_{sh})} & \text{if } f_{sh} < f_{es,\max} \\ f_{es,\max} & \text{if } f_{sh} \geq f_{es,\max} \end{cases}\end{aligned}\quad (0.0.29)$$

$$f_v = \frac{f_{ev,0} + f_{ev,\infty} \times e^{\frac{f_{ab} - f_{ab,0}}{k_{ev}}}}{1 + e^{\frac{f_{ab} - f_{ab,0}}{k_{ev}}}} + W_{c,v} \times f_{ac} - W_{p,v} \times f_{ap} - \theta_v \quad (0.0.30)$$

$$R_{sp}(t) = \Delta R_{sp}(t) + R_{sp,0}$$

$$\frac{d\Delta R_{sp}}{dt} = \frac{1}{\tau_{R_{sp}}} \times (-\Delta R_{sp} + \sigma_{R_{sp}})$$

$$\sigma_{R_{sp}} = \begin{cases} G_{R_{sp}} \times \ln[f_{sp}(t - D_{R_{sp}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases}$$

$$R_{mp}(t) = \Delta R_{mp}(t) + R_{mp,0}$$

$$\frac{d\Delta R_{mp}}{dt} = \frac{1}{\tau_{R_{mp}}} \times (-\Delta R_{mp} + \sigma_{R_{mp}})$$

$$\sigma_{R_{mp}} = \begin{cases} G_{R_{mp}} \times \ln[f_{sp}(t - D_{R_{mp}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases}$$

$$R_{ep}(t) = \Delta R_{ep}(t) + R_{ep,0}$$

$$\frac{d\Delta R_{ep}}{dt} = \frac{1}{\tau_{R_{ep}}} \times (-\Delta R_{ep} + \sigma_{R_{ep}})$$

$$\sigma_{R_{ep}} = \begin{cases} G_{R_{ep}} \times \ln[f_{sp}(t - D_{R_{ep}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases} \quad (0.0.31)$$

$$E_{\max,rv}(t) = \Delta E_{\max,rv}(t) + E_{\max,rv,0}$$

$$\frac{d\Delta E_{\max,rv}}{dt} = \frac{1}{\tau_{E_{\max,rv}}} \times (-\Delta E_{\max,rv} + \sigma_{E_{\max,rv}})$$

$$\sigma_{E_{\max,rv}} = \begin{cases} G_{E_{\max,rv}} \times \ln[f_{sh}(t - D_{E_{\max,rv}}) - f_{es,\min} + 1] & \text{if } f_{sh} \geq f_{es,\min} \\ 0 & \text{if } f_{sh} < f_{es,\min} \end{cases}$$

(0.0.32)

$$E_{\max,lv}(t) = \Delta E_{\max,lv}(t) + E_{\max,lv,0}$$

$$\frac{d\Delta E_{\max,lv}}{dt} = \frac{1}{\tau_{E_{\max,lv}}} \times (-\Delta E_{\max,lv} + \sigma_{E_{\max,lv}})$$

$$\sigma_{E_{\max,lv}} = \begin{cases} G_{E_{\max,lv}} \times \ln[f_{sh}(t - D_{E_{\max,lv}}) - f_{es,\min} + 1] & \text{if } f_{sh} \geq f_{es,\min} \\ 0 & \text{if } f_{sh} < f_{es,\min} \end{cases}$$

$$\begin{aligned}
 T(t) &= \Delta T_S(t) + \Delta T_V(t) + T_0 \\
 \frac{d\Delta T_S}{dt} &= \frac{1}{\tau_{T_S}} \times (-\Delta T_S + \sigma_{T_S}) \\
 \frac{d\Delta T_V}{dt} &= \frac{1}{\tau_{T_V}} \times (-\Delta T_V + \sigma_{T_V}) \\
 \sigma_{T_S} &= \begin{cases} G_{T_S} \times \ln[f_{sh}(t - D_{T_S}) - f_{es,\min} + 1] & \text{if } f_{sh} \geq f_{es,\min} \\ 0 & \text{if } f_{sh} < f_{es,\min} \end{cases} \\
 \sigma_{T_V} &= G_{T_V} \times f_v(t - D_{T_V})
 \end{aligned} \tag{0.0.33}$$

Unstressed Volume

$$\begin{aligned}
 V_{u,mv}(t) &= \Delta V_{u,mv}(t) + V_{u,mv,0} \\
 \frac{d\Delta V_{u,mv}}{dt} &= \frac{1}{\tau_{V_{u,mv}}} \times (-\Delta V_{u,mv} + \sigma_{V_{u,mv}}) \\
 \sigma_{V_{u,mv}} &= \begin{cases} G_{V_{u,mv}} \times \ln[f_{sp}(t - D_{V_{u,mv}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases} \\
 V_{u,sv}(t) &= \Delta V_{u,sv}(t) + V_{u,sv,0} \\
 \frac{d\Delta V_{u,sv}}{dt} &= \frac{1}{\tau_{V_{u,sv}}} \times (-\Delta V_{u,sv} + \sigma_{V_{u,sv}}) \\
 \sigma_{V_{u,sv}} &= \begin{cases} G_{V_{u,sv}} \times \ln[f_{sp}(t - D_{V_{u,sv}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases}
 \end{aligned}$$

$$\begin{aligned}
 V_{u,ev}(t) &= \Delta V_{u,ev}(t) + V_{u,ev,0} \\
 \frac{d\Delta V_{u,ev}}{dt} &= \frac{1}{\tau_{V_{u,ev}}} \times (-\Delta V_{u,ev} + \sigma_{V_{u,ev}}) \\
 \sigma_{V_{u,ev}} &= \begin{cases} G_{V_{u,ev}} \times \ln[f_{sp}(t - D_{V_{u,ev}}) - f_{es,\min} + 1] & \text{if } f_{sp} \geq f_{es,\min} \\ 0 & \text{if } f_{sp} < f_{es,\min} \end{cases}
 \end{aligned} \tag{0.0.34}$$

Ventricle Pressure

$$\begin{aligned}
P_{lv} &= P_{\max,lv} - R_{lv} \times F_{o,l} \\
P_{rv} &= P_{\max,rv} - R_{rv} \times F_{o,r}
\end{aligned}
\tag{0.0.35}$$

Table 1. *Parameters characterizing the vascular system in the basal condition*

Compliance, ml/mmHg	Unstressed Volume, ml	Hydraulic Resistance, mmHg · s · ml ⁻¹	Inertance, mmHg · s ² · ml ⁻¹
$C_{sa} = 0.28$	$V_{u,sa} = 0$	$R_{sa} = 0.06$	$L_{sa} = 0.22 \times 10^{-3}$
$C_{sp} = 2.05$	$V_{u,sp} = 274.4$	$R_{sp} = 3.307$	
$C_{ep} = 0.668$	$V_{u,ep} = 134.64$	$R_{ep} = 3.52$	
$C_{mp} = 0.525$	$V_{u,mp} = 105.8$	$R_{mp} = 4.48$	
$C_{bp} = 0.358$	$V_{u,bp} = 72.13$	$R_{bp} = 6.57$	$L_{pa} = 0.18 \times 10^{-3}$
$C_{hp} = 0.119$	$V_{u,hp} = 24$	$R_{hp} = 19.71$	
$C_{sv} = 61.11$	$V_{u,sv} = 1,121$	$R_{sv} = 0.038$	
$C_{ev} = 20$	$V_{u,ev} = 550$	$R_{ev} = 0.04$	
$C_{mv} = 15.71$	$V_{u,mv} = 432.14$	$R_{mv} = 0.05$	
$C_{bv} = 10.71$	$V_{u,bv} = 294.64$	$R_{bv} = 0.075$	
$C_{hv} = 3.57$	$V_{u,hv} = 98.21$	$R_{hv} = 0.224$	
$C_{pa} = 0.76$	$V_{u,pa} = 0$	$R_{pa} = 0.023$	
$C_{pp} = 5.80$	$V_{u,pp} = 123$	$R_{pp} = 0.0894$	
$C_{pv} = 25.37$	$V_{u,pv} = 120$	$R_{pv} = 0.0056$	

C, compliance; V_u , unstressed volume; R , hydraulic resistance; L , inertance; sa, systemic arterial; sp, splanchnic peripheral; ep, extra-splanchnic peripheral; mp, skeletal muscle peripheral; bp, brain peripheral; hp, coronary peripheral; sv, splanchnic venous; ev, extra-splanchnic venous; mv, skeletal muscle venous; bv, brain venous; hv, coronary venous; pa, pulmonary arterial; pp, pulmonary peripheral; pv, pulmonary venous. Total blood volume (V_{tot}) is 5,300 ml.

Table 2. Basal values of parameters for reflex regulatory mechanisms

<i>Afferent baroreflex pathway (Eqs. 14–16)</i>			
$\tau_{z,b} = 6.37 \text{ s}$ $\tau_{p,b} = 2.076 \text{ s}$	$f_{ab,min} = 2.52 \text{ spikes/s}$ $f_{ab,max} = 47.78 \text{ spikes/s}$	$P_n = 92 \text{ mmHg}$ $k_{ab} = 11.76 \text{ mmHg}$	
<i>Afferent chemoreflex pathway (Eqs. 17 and 18)</i>			
$\tau_c = 2 \text{ s}$	$f_{ac,min} = 1.16 \text{ spikes/s}$ $f_{ac,max} = 17.07 \text{ spikes/s}$	$PO_{2n} = 45 \text{ mmHg}$ $k_{ac} = 29.27 \text{ mmHg}$	
<i>Afferent pulmonary stretch receptors pathway (Eqs. 19 and 20)</i>			
$\tau_p = 2 \text{ s}$		$G_{ap} = 23.29 \text{ l}^{-1} \cdot \text{spikes} \cdot \text{s}^{-1}$	
<i>Efferent sympathetic pathway (Eqs. 21 and 22)</i>			
$f_{es,\infty} = 2.1 \text{ spikes/s}$ $f_{es,0} = 16.11 \text{ spikes/s}$ $f_{es,min} = 2.66 \text{ spikes/s}$ $f_{es,max} = 60 \text{ spikes/s}$ $k_{es} = 0.0675 \text{ s}$	$W_{b,sp} = 1$ $W_{c,sp} = 5$ $W_{p,sp} = 0.34$	$W_{b,sh} = 1$ $W_{c,sh} = 1$	
<i>Efferent vagal pathway (Eq. 23)</i>			
$f_{ev,\infty} = 6.3 \text{ spikes/s}$ $f_{ev,0} = 3.2 \text{ spikes/s}$ $f_{ab,0} = 25 \text{ spikes/s}$ $k_{ev} = 7.06 \text{ spikes/s}$		$W_{c,v} = 0.2$ $W_{p,v} = 0.103$ $\theta_v = -0.68 \text{ spikes/s}$	
<i>CNS hypoxic response (Eqs. 24–27)</i>			
$\chi_{max,sp} = 13.32 \text{ spikes/s}$ $\chi_{max,sh} = 3.59 \text{ spikes/s}$ $\tau_{isc} = 30 \text{ s}$	$\chi_{min,sp} = 7.33 \text{ spikes/s}$ $\chi_{min,sh} = -49.38 \text{ spikes/s}$	$PO_{2n,sp} = 30 \text{ mmHg}$ $PO_{2n,sh} = 45 \text{ mmHg}$	$k_{isc,sp} = 2 \text{ mmHg}$ $k_{isc,sh} = 6 \text{ mmHg}$
<i>Ventilatory response (Eqs. 28 and 29)</i>			
$G_v = 0.125 \text{ l/v}$	$\tau_v = 3 \text{ s}$	$D_v = 6 \text{ s}$ $V_{Tn} = 0.583 \text{ liter}$	$f_{ac,n} = 3.6 \text{ spikes/s}$
<i>Reflex effectors (Eqs. 30–40)</i>			
$G_{E_{max,l_v}} = 0.475 \text{ mmHg} \cdot \text{ml}^{-1} \cdot \text{v}^{-1}$ $G_{E_{max,r_v}} = 0.282 \text{ mmHg} \cdot \text{ml}^{-1} \cdot \text{v}^{-1}$ $G_{R_{sp}} = 0.695 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1} \cdot \text{v}^{-1}$ $G_{R_{ep}} = 1.94 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1} \cdot \text{v}^{-1}$ $G_{R_{mp}} = 2.47 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1} \cdot \text{v}^{-1}$ $G_{V_{u,sv}} = -265.4 \text{ ml/v}$ $G_{V_{u,ev}} = -74.21 \text{ ml/v}$ $G_{V_{u,mv}} = -58.29 \text{ ml/v}$ $G_{T,s} = -0.13 \text{ s/v}$ $G_{T,v} = 0.09 \text{ s/v}$	$\tau_{E_{max,l_v}} = 8 \text{ s}$ $\tau_{E_{max,r_v}} = 8 \text{ s}$ $\tau_{R_{sp}} = 6 \text{ s}$ $\tau_{R_{ep}} = 6 \text{ s}$ $\tau_{R_{mp}} = 6 \text{ s}$ $\tau_{V_{u,sv}} = 20 \text{ s}$ $\tau_{V_{u,ev}} = 20 \text{ s}$ $\tau_{V_{u,mv}} = 20 \text{ s}$ $\tau_{T,s} = 2 \text{ s}$ $\tau_{T,v} = 1.5 \text{ s}$	$D_{E_{max,l_v}} = 2 \text{ s}$ $D_{E_{max,r_v}} = 2 \text{ s}$ $D_{R_{sp}} = 2 \text{ s}$ $D_{R_{ep}} = 2 \text{ s}$ $D_{R_{mp}} = 2 \text{ s}$ $D_{V_{u,sv}} = 5 \text{ s}$ $D_{V_{u,ev}} = 5 \text{ s}$ $D_{V_{u,mv}} = 5 \text{ s}$ $D_{T,s} = 2 \text{ s}$ $D_{T,v} = 0.2 \text{ s}$	$E_{max,l_v,0} = 2.392 \text{ mmHg/ml}$ $E_{max,r_v,0} = 1.412 \text{ mmHg/ml}$ $R_{sp,0} = 2.49 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1}$ $R_{ep,0} = 1.655 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1}$ $R_{mp,0} = 2.106 \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1}$ $V_{u,sv,0} = 1,435.4 \text{ ml}$ $V_{u,ev,0} = 640.73 \text{ ml}$ $V_{u,mv,0} = 503.26 \text{ ml}$ $T_0 = 0.58 \text{ s}$

CNS, central nervous system; \dot{v} , ventilation; see APPENDIX for explanation of other symbols. $v = \text{spikes/s}$.

Table 2. *Parameters describing the right and left heart*

Left Heart	Right Heart
$C_{la} = 19.23 \text{ ml/mmHg}$	$C_{ra} = 31.25 \text{ ml/mmHg}$
$V_{u,la} = 25 \text{ ml}$	$V_{u,ra} = 25 \text{ ml}$
$R_{la} = 2.5 \cdot 10^{-3} \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1}$	$R_{ra} = 2.5 \cdot 10^{-3} \text{ mmHg} \cdot \text{s} \cdot \text{ml}^{-1}$
$P_{0,lv} = 1.5 \text{ mmHg}$	$P_{0,rv} = 1.5 \text{ mmHg}$
$k_{E,lv} = 0.014 \text{ ml}^{-1}$	$k_{E,rv} = 0.011 \text{ ml}^{-1}$
$V_{u,lv} = 16.77 \text{ ml}$	$V_{u,rv} = 40.8$
$E_{\max,lv} = 2.95 \text{ mmHg/ml}$	$E_{\max,rv} = 1.75 \text{ mmHg/ml}$
$k_{R,lv} = 3.75 \cdot 10^{-4} \text{ s/ml}$	$k_{R,rv} = 1.4 \cdot 10^{-3} \text{ s/ml}$

Basal heart period (T) is 0.833 s; k_{sys} and $T_{\text{sys},0}$, which describe duration of systole as function of heart rate, are 0.075 s² and 0.5 s, respectively. R , resistance of atrioventricular valve; k_E and P_0 , parameters describing end-diastolic pressure-volume function of ventricle; E_{\max} , slope of end-systolic relationship; k_R , parameter describing dependence of ventricle resistance on isometric pressure. Subscripts: la, left atrium; ra, right atrium; lv, left ventricle; rv, right ventricle.