



student			
nuid*	first_name	last_name	university_email

course_registration	
course_id*	nuid

course		
course_id*	course_name	instructor_id

instructor			
instructor_id*	first_name	last_name	university_email

Notes: primary key is noted with \*

The ERD and relational schema are shown above. For a table to satisfy BCNF, other than the table should be in the third normal form, it also should satisfy for any dependency  $A \rightarrow B$ ,  $A$  should be a super key.

In the requirement, we defined for courses, they are uniquely identified by `course_id`. For example, both John and Jodi can teach the "Database" course, but the `course_id` is completely different from each other. Another example is if John teaches "Database" course in 2 consecutive semesters, the assigned `course_id` is completely different for different semesters. So, to sum up, `course_id` is always unique and never repeated.

So, we can see the schema satisfy the requirement. For the student table,  $nuid \rightarrow first\_name$ ,  $nuid \rightarrow last\_name$ ,  $nuid \rightarrow university\_email$ . For the course table,  $course\_id \rightarrow course\_name$ ,  $course\_id \rightarrow instructor\_id$ . For the instructor table,  $instructor\_id \rightarrow first\_name$ ,  $instructor\_id \rightarrow last\_name$ ,  $instructor\_id \rightarrow university\_email$ . Because for any dependency  $A \rightarrow B$ ,  $A$  is a super key, so it is proved to be BCNF.