

课堂练习3

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1、用简单字母置换产生的密文仍然保持明文的统计特征。为打乱密文的统计结构，可采取如下的加密方法，它是排斥加加密算法的扩展。将英语的26个字母按字母表映射成为0, 1, 2, 3, ..., 25，并记此映射为 I ，即 $I(A) = 0, I(B) = 1, \dots, I(Z) = 25$ 。令 X 和 Y 为两个英文字母，令 $X + Y = I^{-1}([I(X) + I(Y)] \bmod 26)$

其中 I^{-1} 为 I 的反函数，即 $I^{-1}(0) = A, I^{-1}(1) = B, \dots, I^{-1}(25) = Z$ 。令 $X = X_1 X_2 \dots X_l$ 和 $Y = Y_1 Y_2 \dots Y_l$ 为长度相等英文字母串，令 $X + Y = (X_1 + Y_1) \dots (X_l + Y_l)$

令密钥 K 为任意英文字母串，并记 K 的长度为 l 。（密钥 K 可长可短，而且同一字母可出现多次。）令明文 $M = M_1 M_2 \dots M_k$ ，这里除 M_k 外所有 M_i 均为由 l 个字母组成的片段，而 M_k 的长度 m 满足 $0 < m \leq l$ 。令 K_m 为 K 的前 m 个英文字母。定义加密算法 E 如下： $E(K, M) = C_1 C_2 \dots C_k$

其中 $C_i = K + M_i, i = 1, 2, \dots, k-1, C_k = K_m + M_k$

(a) 给出解密算法 D

```
1  #include <iostream>
2  using namespace std;
3  string m = "Methods of making messages unintelligible to adversaries have
   been necessary. Substitution is the simplest method that replaces a
   character in the plaintext with a fixed different character in the
   ciphertext. This method preserves the letter frequency in the plaintext and
   so one can search for the plaintext from a given ciphertext by comparing
   the frequency of each letter against the known common frequency in the
   underlying language.";
4  string k = "BLACKHAT";
5  //为了简化算法，翻译后不区分大小写
6  int getnum(char a) { if (a < 'a') return a - 'A'; else return a - 'a'; }
7  char getch(int a) { return a + 'a'; }
8  int main()
9  {
10     int len = k.length();
11     int lenm = m.length();
12     string cipher = "";
13     for (int i = 0, j=0; i < lenm; i += 1, j++)
14     {
15         if (j == len) j = 0;
16         while (m[i] == ' ' || m[i] == '.')
17             //跳过空格和句号
18             cipher += m[i];
19             i++;
20     }
21     if (i == lenm) break; //全部翻译完毕
22     cipher += getch((getnum(m[i]) + getnum(k[j])) % 26);
23 }
24 cout << cipher << endl;
25 }
```

(b) 令 $K=BLACKHAT$ 。将下列明文翻译成密文：

Methods of making messages unintelligible to adversaries have been necessary. Substitution is the simplest method that replaces a character in the plaintext with a fixed different character in the ciphertext. This method preserves the letter frequency in the plaintext and so one can search for the plaintext from a given ciphertext by comparing the frequency of each letter against the known common frequency in the underlying language.

翻译结果:

```
nptjyks hg xamsug ffdscqls notnvoslbhtbno ao tegetchrbfd hcfl bxf
y ngmlslbcy. ueismjeuvsvn bt ehg cpmimpsv wltapo tjka rxqwaeoz a
vilrcmaek jy tjo wltjytgha wbus a hseew etfhoyegu nhcbhcmfc ip do
e vjahgbaequ. ehkc temizd rblsxsgau doe efetgb mrxfepmf ig use r
vhigupxv kud lp zng mhn lflrer mok use rvhigupxv pyof b rixou cbq
setdlxm cj cqwwakjyg vrl fkfbugxjy hg paer semupr cqhigte tjo rnh
xy cqwtog gceselnvz tn vrl ugeprnipnz mlniehgx.
```