

A Restaurant's Future

MICHELLE LI

github.com/michellekli/visitor-forecasting



Photo by [Helena Lopes](#) from [Pexels](#)

2-6% profit margins (Jong, 2017)



Photo by [Daria Shevtsova](#) from [Pexels](#)

\$25 billion/year food waste (Amin, 2018)

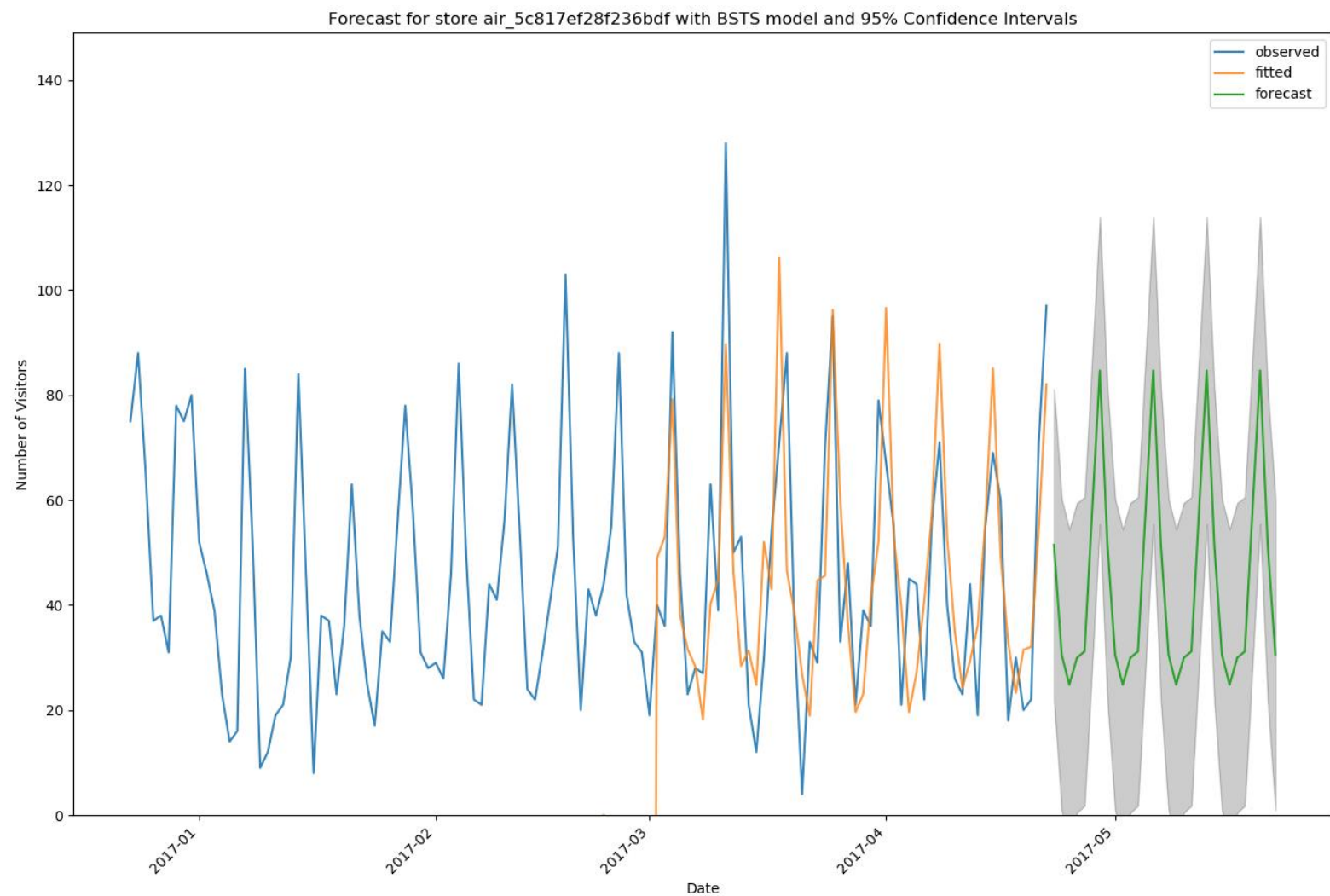


Photo by [Elle Hughes](#) from [Pexels](#)

\$150,000/year to staff turnover (Lachapelle, 2018)

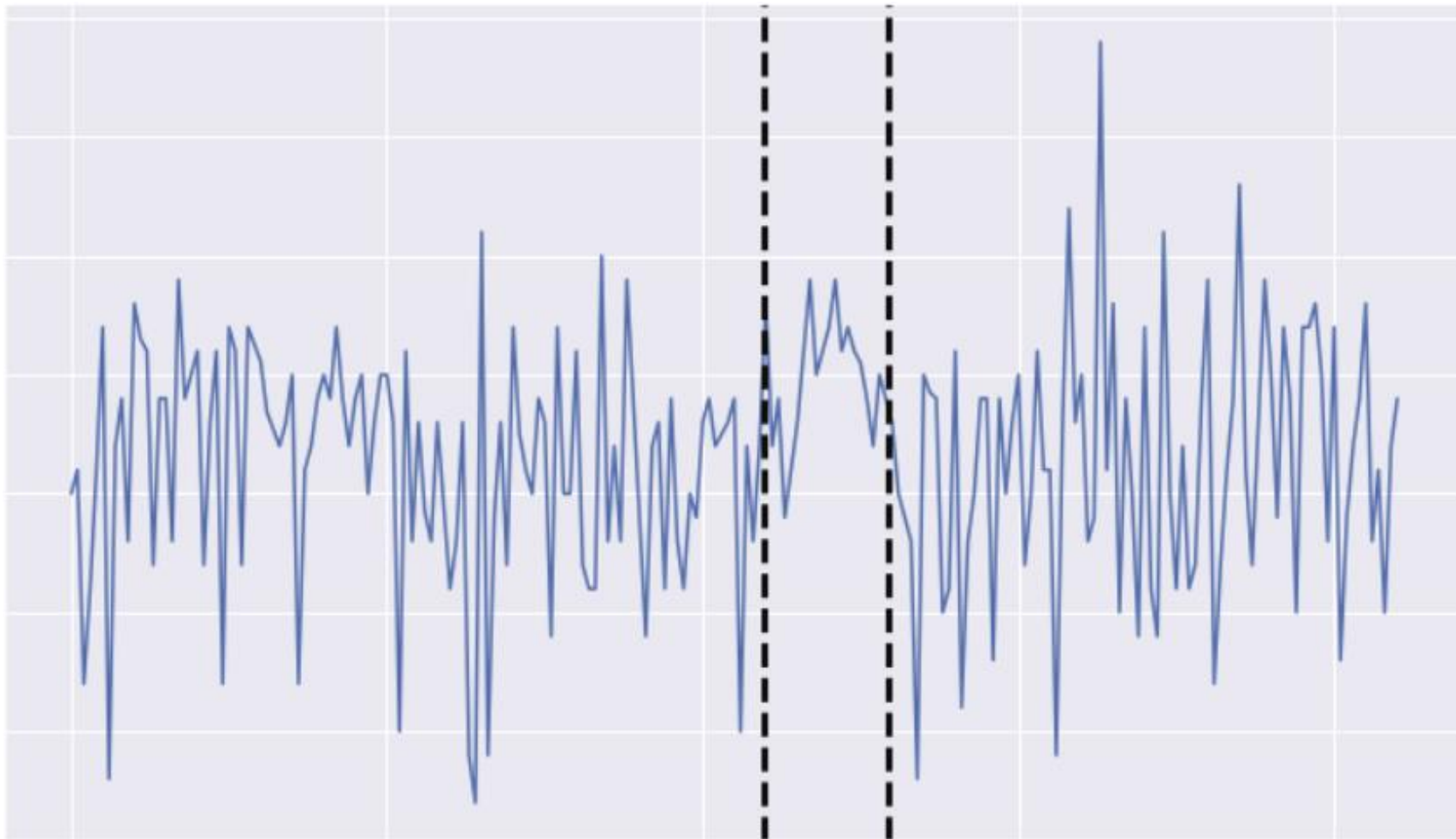


SEE THE
FUTURE



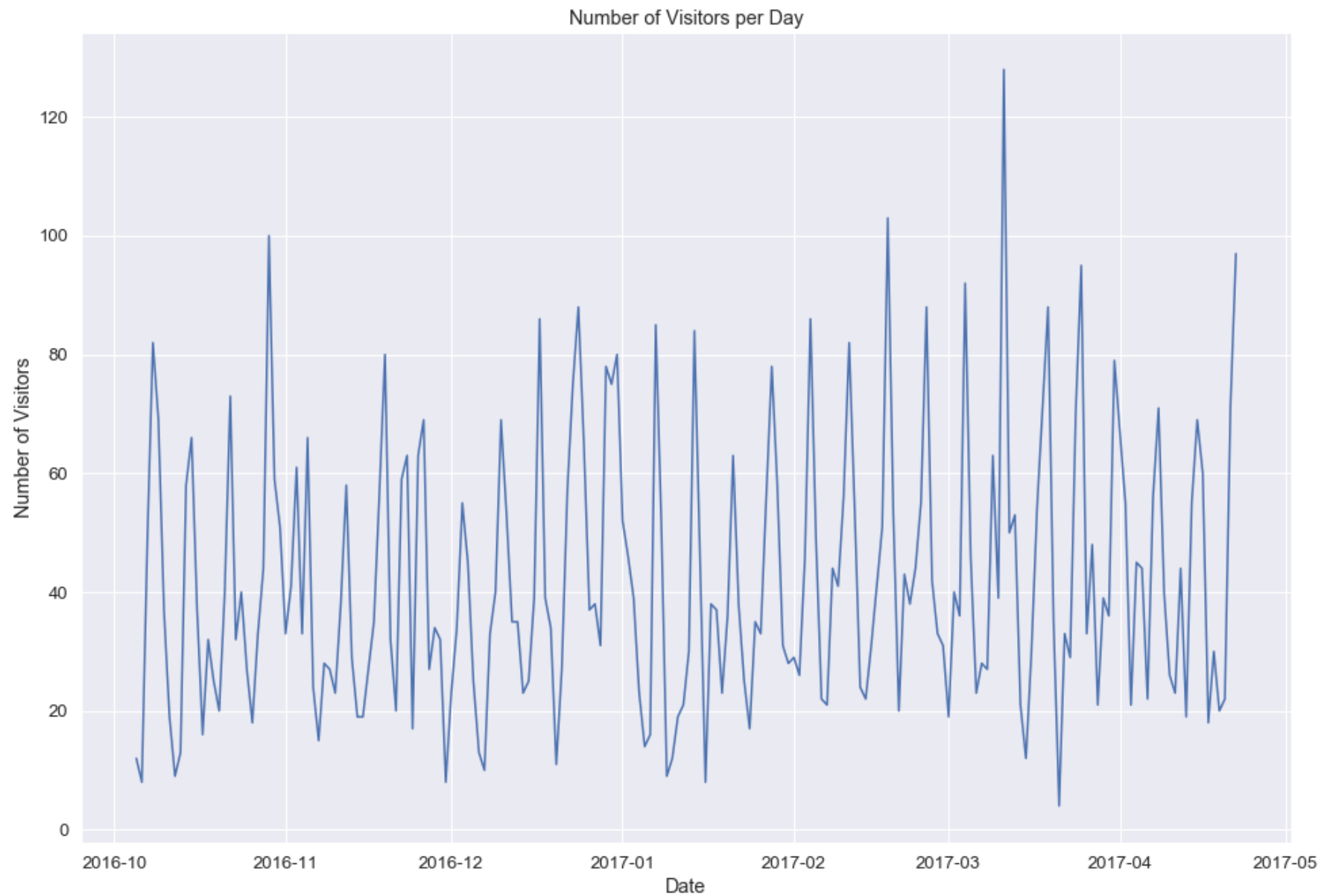
	visit_date	forecast	95_lower	95_upper
127	2017-04-29	84.681772	55.419824	113.943720
128	2017-04-30	51.479521	21.810771	81.148271
129	2017-05-01	30.561021	0.932295	60.189746
130	2017-05-02	24.827111	-4.756797	54.411018
131	2017-05-03	29.949439	0.441101	59.457776
132	2017-05-04	31.172617	1.798376	60.546858
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145	2017-05-17	29.949439	0.441101	59.457776
146	2017-05-18	31.172617	1.798376	60.546858

The Data

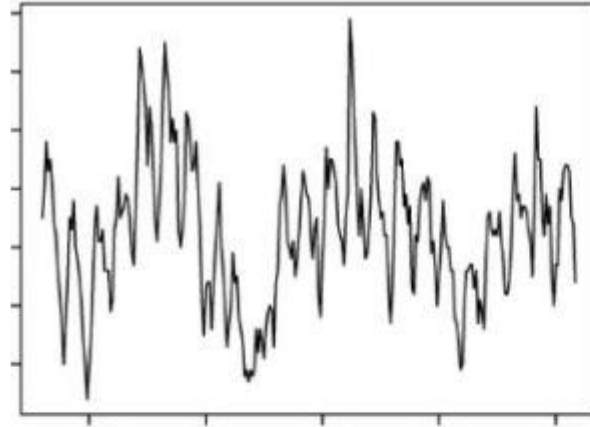


Structural Stability

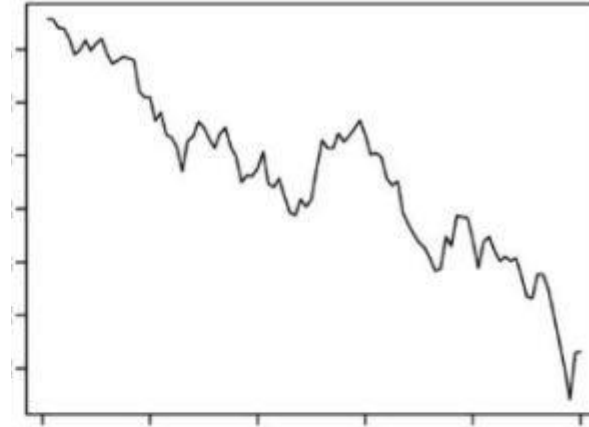
- ❖ Bottom-up segmentation
- ❖ Python library: ruptures



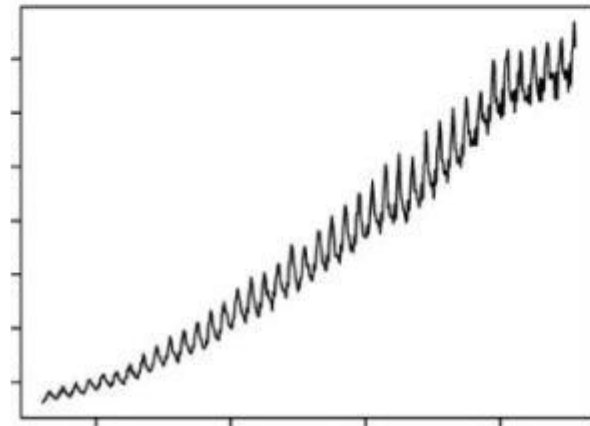
seasonality



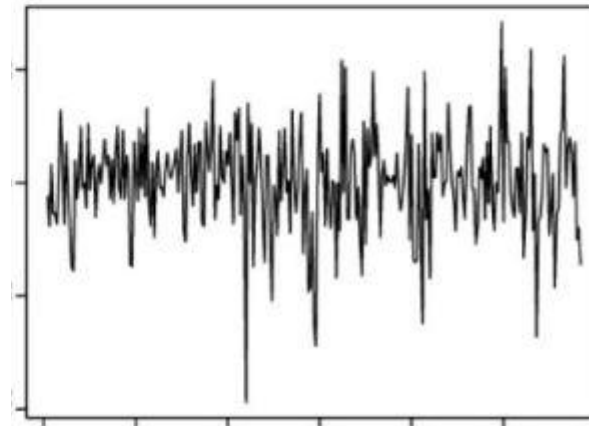
trend



seasonality and trend

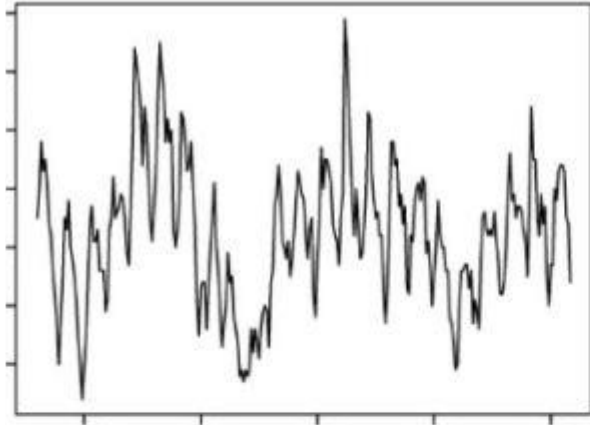


neither (stationary)

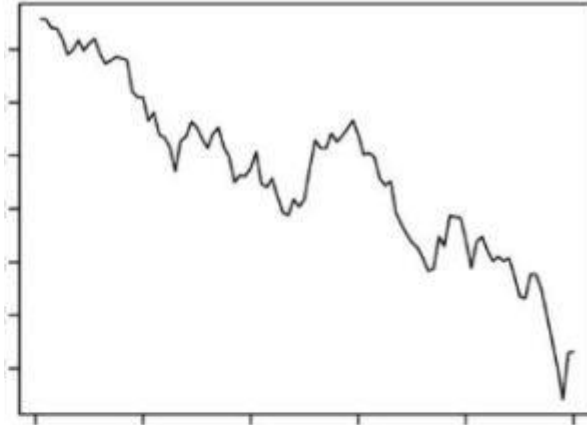


Source: (Seth, 2018)

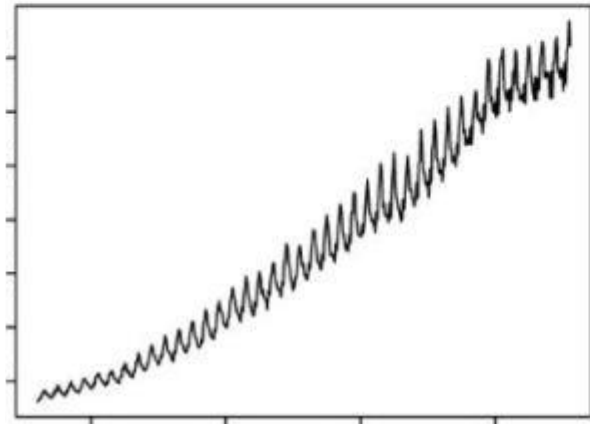
seasonality



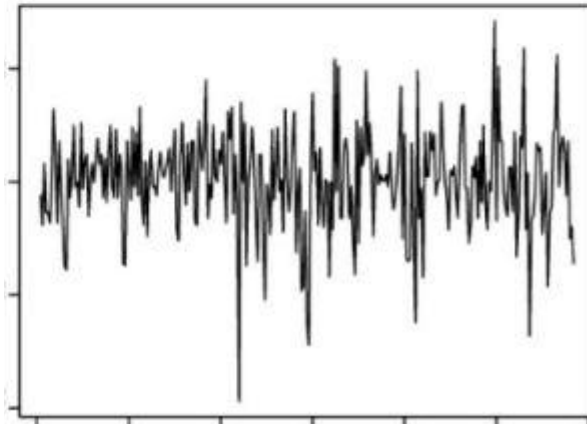
trend



seasonality and trend



neither (stationary)

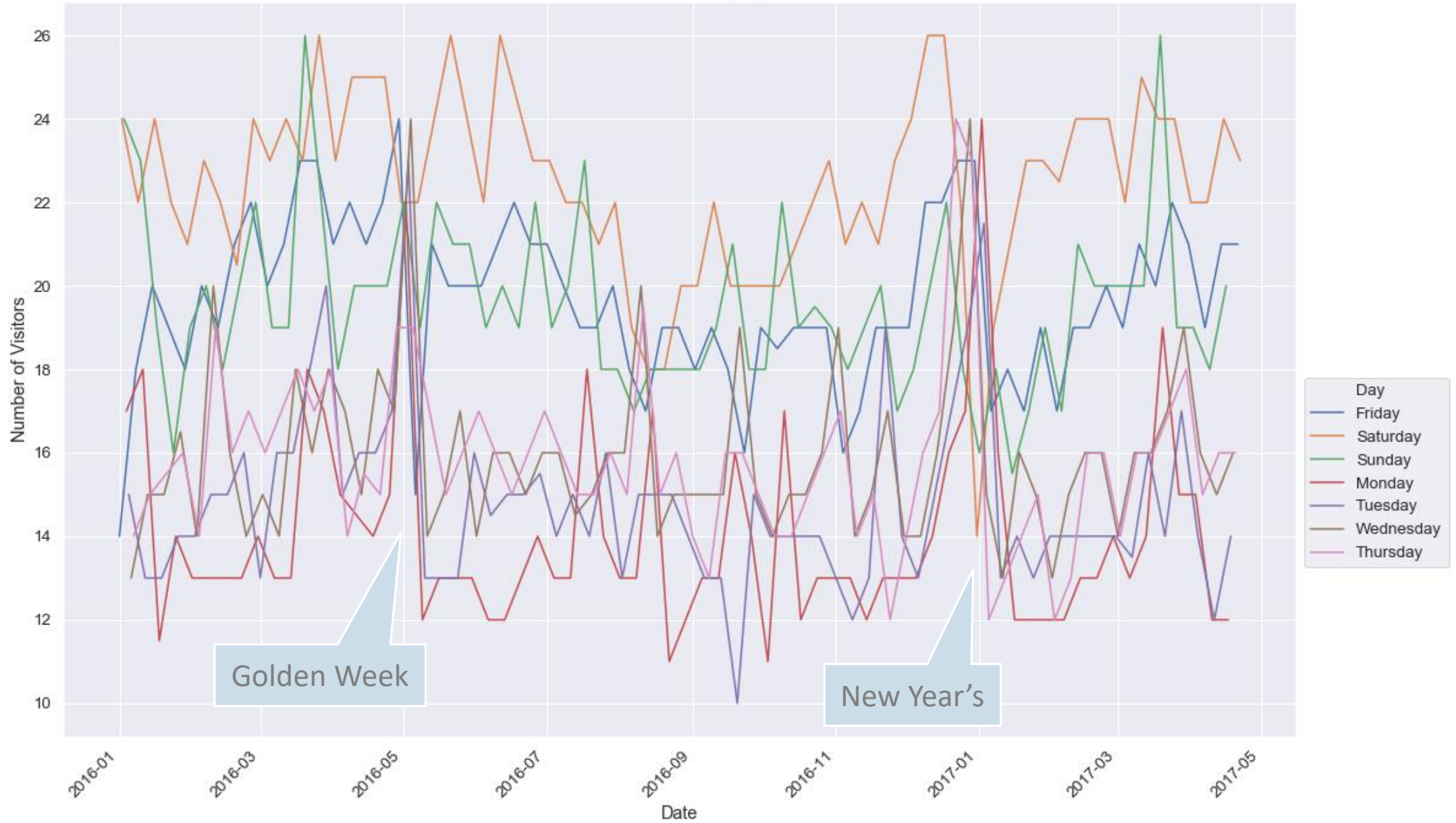


?

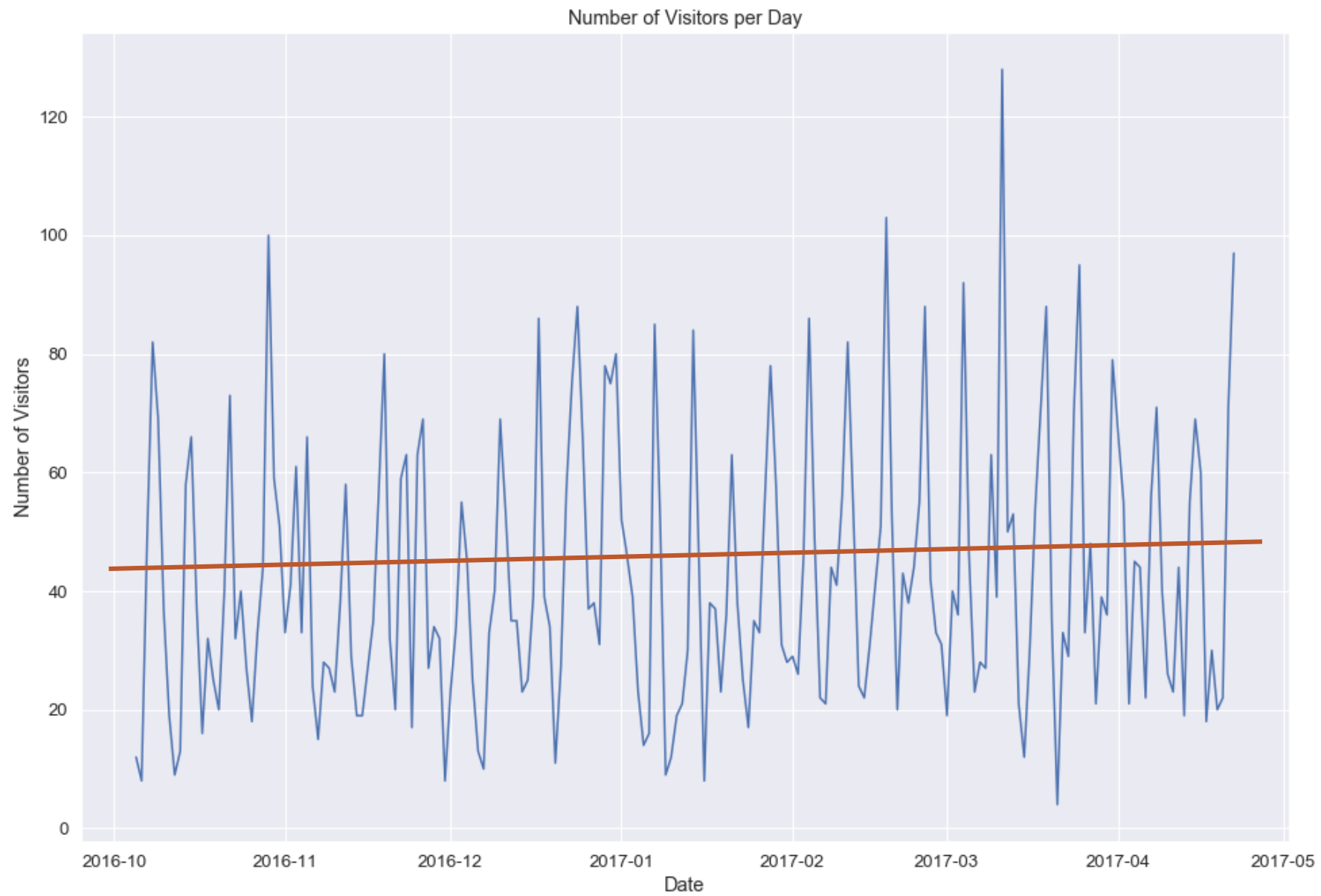


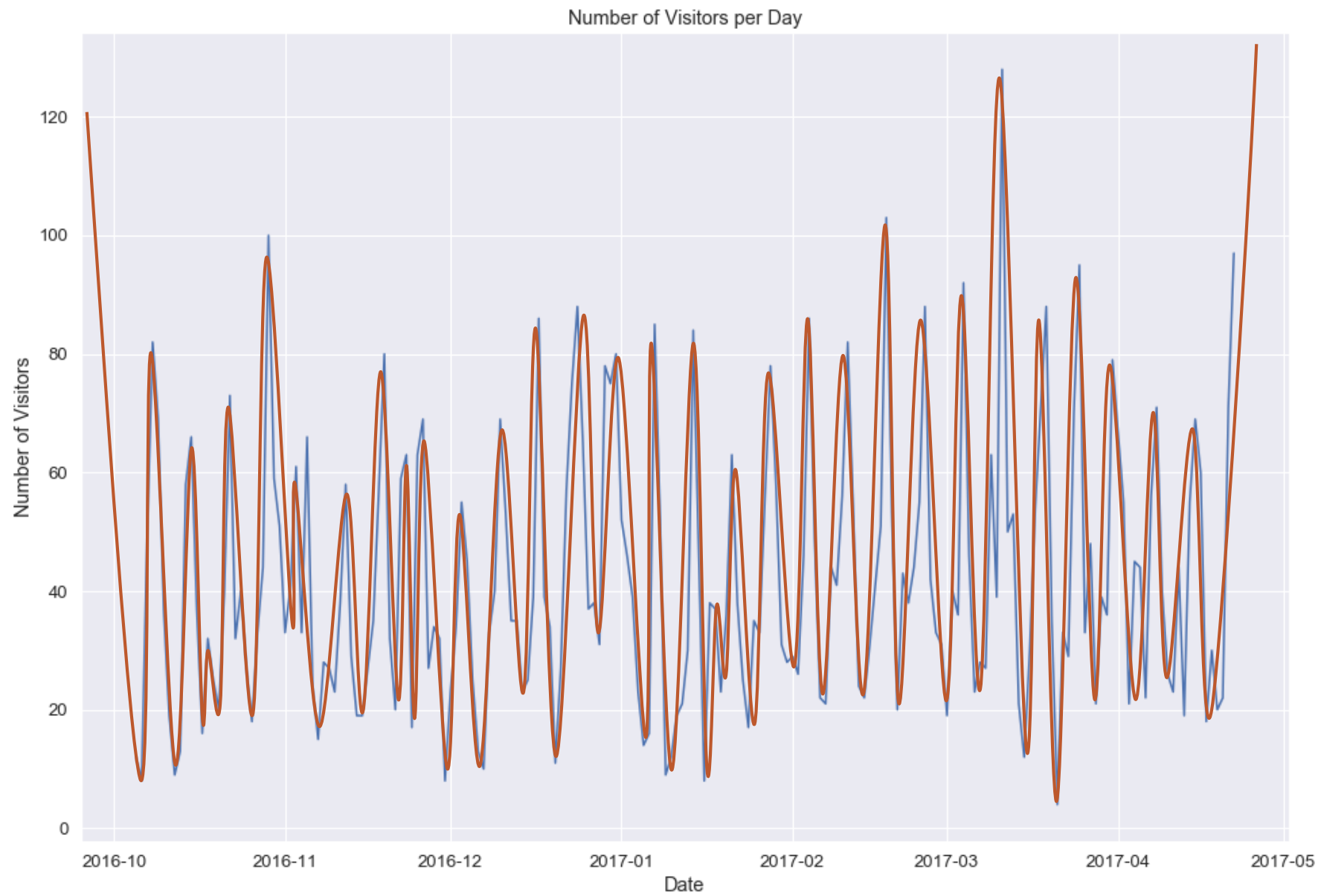
Source: (Seth, 2018)

Median Visitors by Day



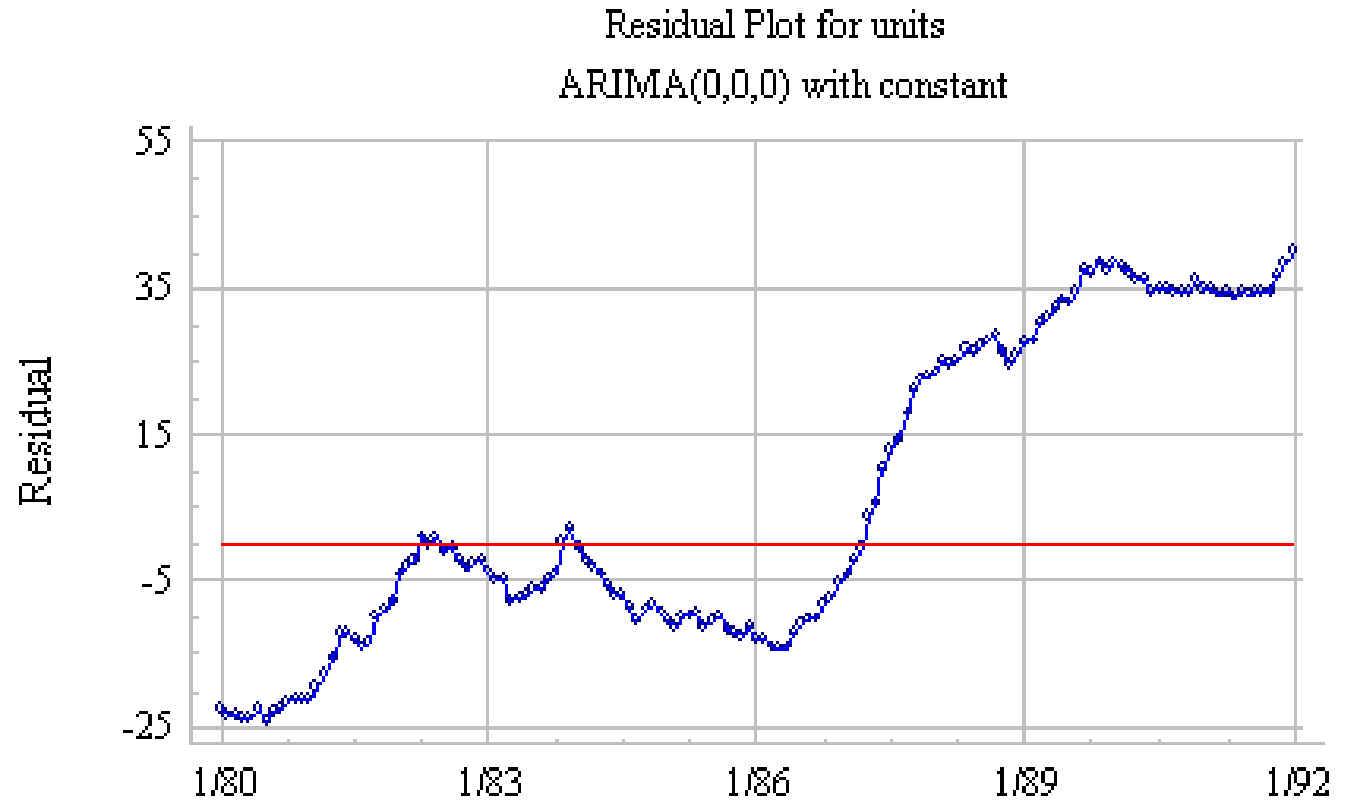
Model Selection





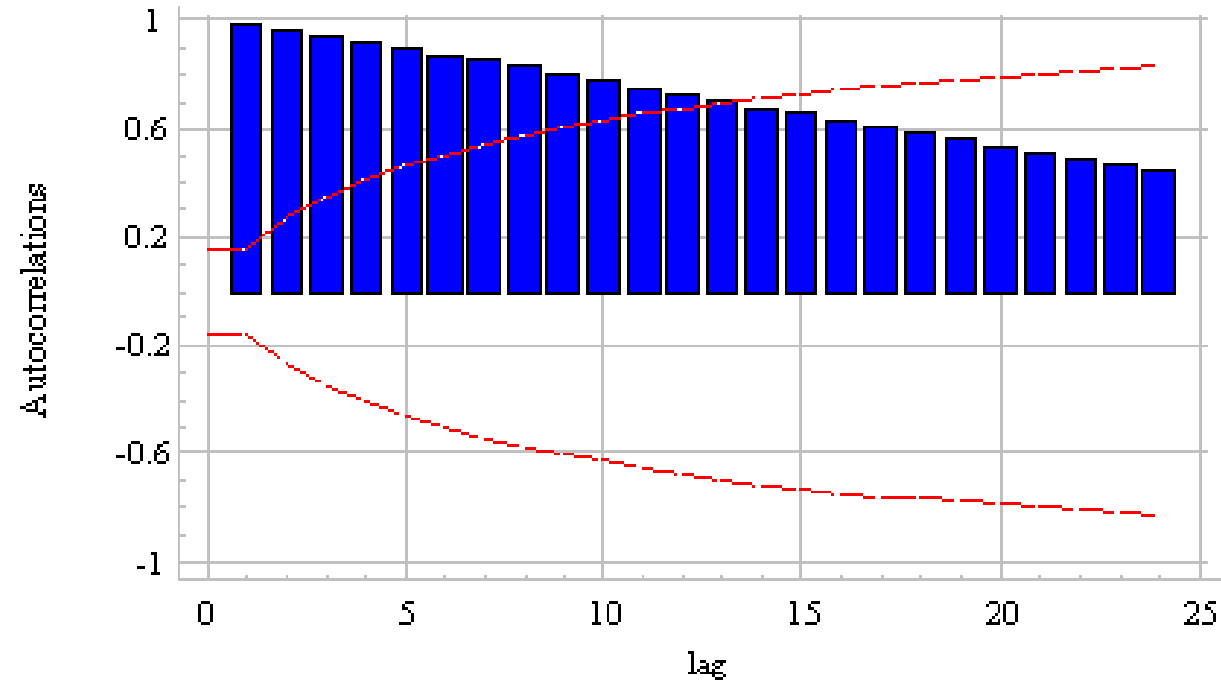
ARIMA(p,d,q)

- AutoRegressive (p)
- Integrated (d)
- Moving Average (q)

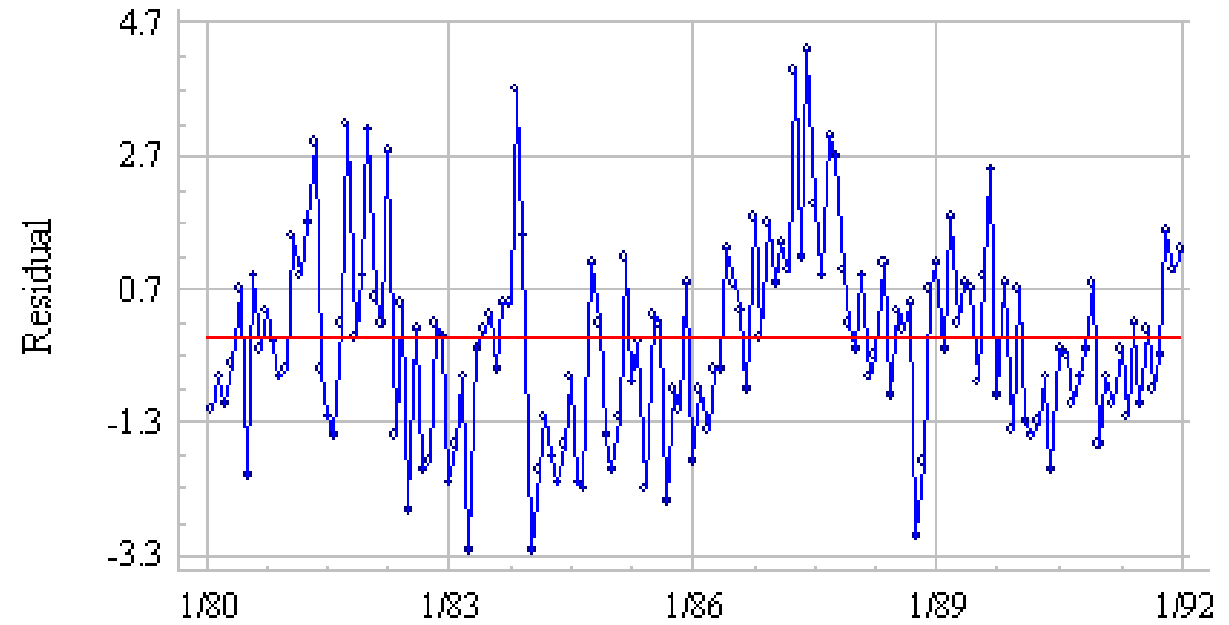


Source: (Nau, Identifying the order of differencing in an ARIMA model, n.d.)

Residual Autocorrelations for units
ARIMA(0,0,0) with constant



Residual Plot for units
ARIMA(0,1,0) with constant



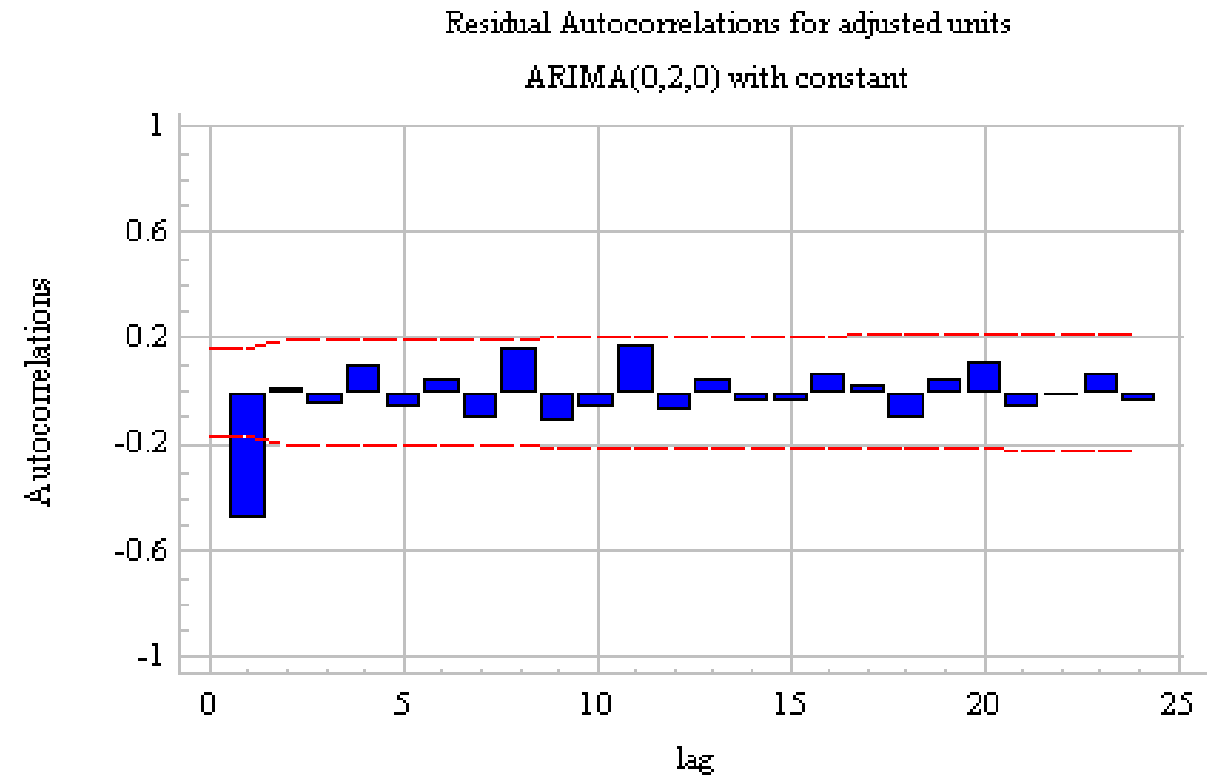
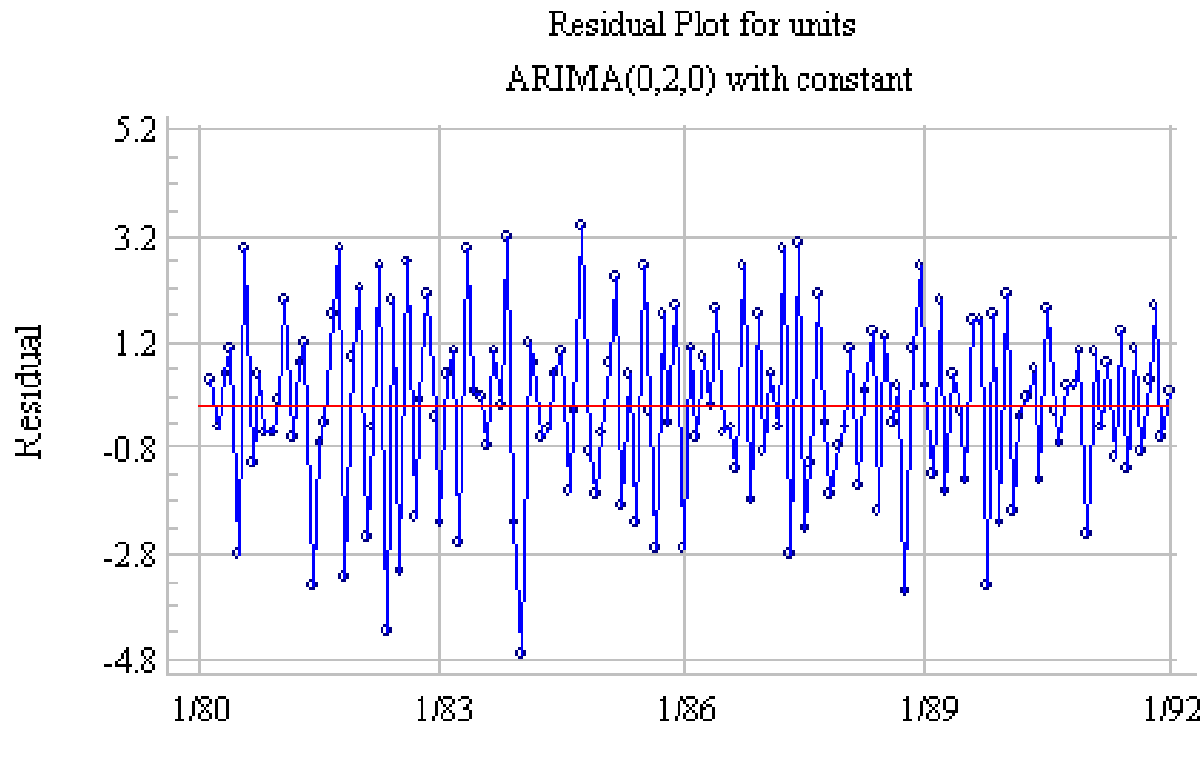
Source: (Nau, Identifying the order of differencing in an ARIMA model, n.d.)

Integrated (d)

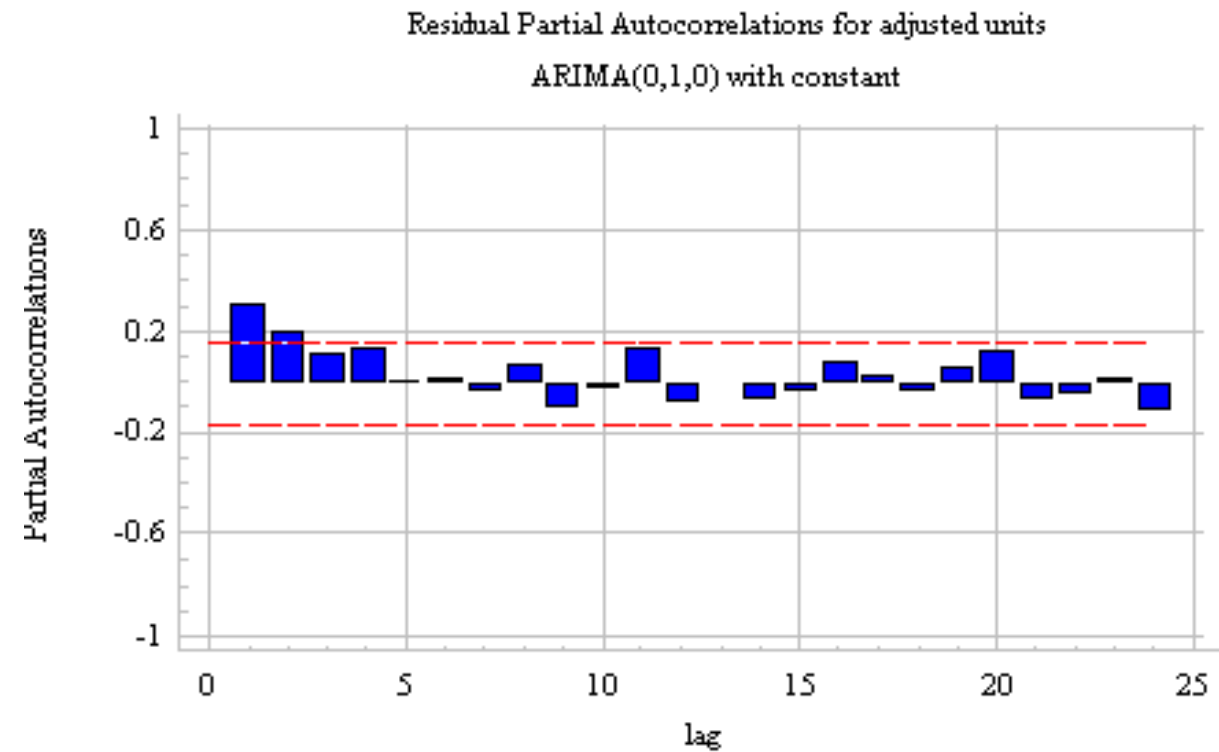
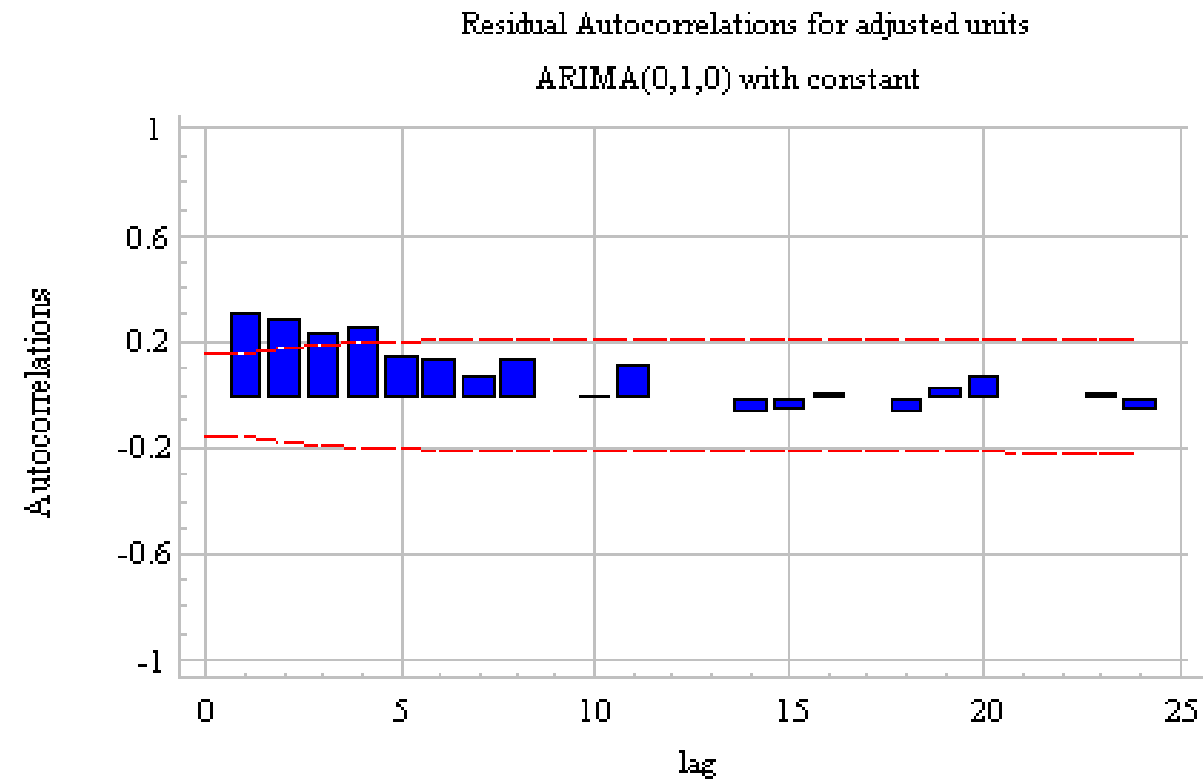
- ❖ Very slow linear decay in autocorrelation function (ACF) plot
- ❖ statsmodels.graphics.tsaplots: plot_acf, plot_pacf

Over Differencing

- Residuals change in sign from one observation to the next



Source: (Nau, Identifying the order of differencing in an ARIMA model, n.d.)



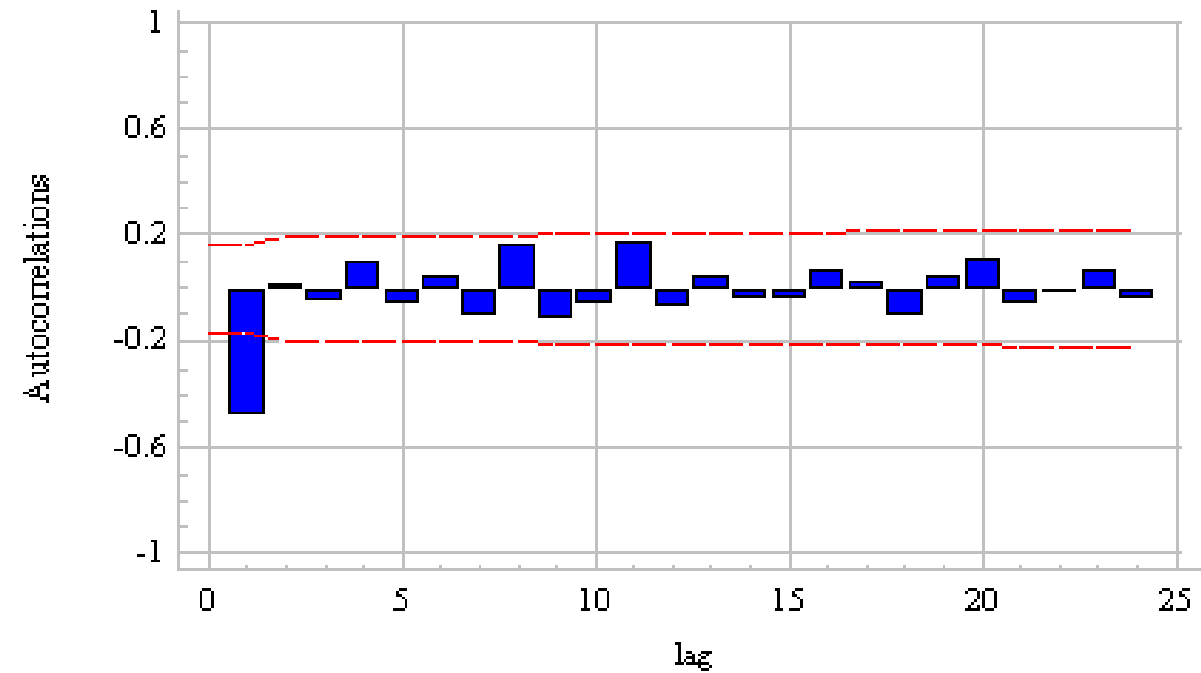
Source: (Nau, Identifying the numbers of AR or MA terms in an ARIMA model, n.d.)

AutoRegressive (p)

- ❖ Partial ACF (PACF) shows sharper cutoff than ACF
- ❖ Select AR term as the number of significant spikes in PACF

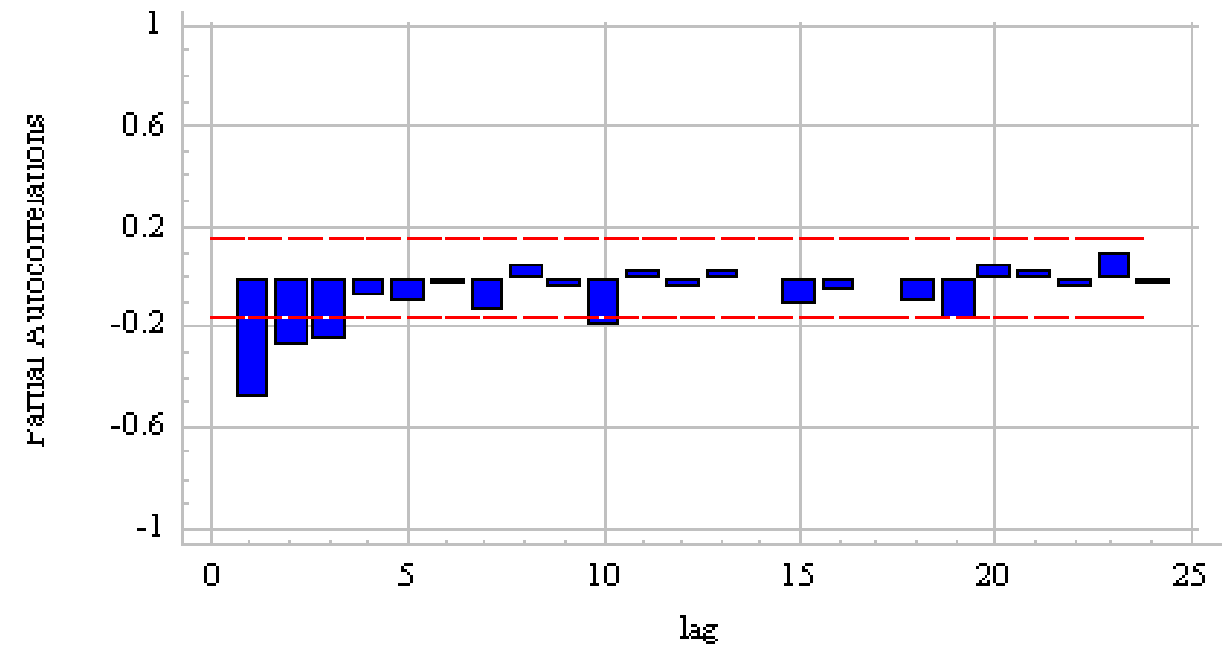
Residual Autocorrelations for adjusted units

ARIMA(0,2,0) with constant



Residual Partial Autocorrelations for adjusted units

ARIMA(0,2,0) with constant

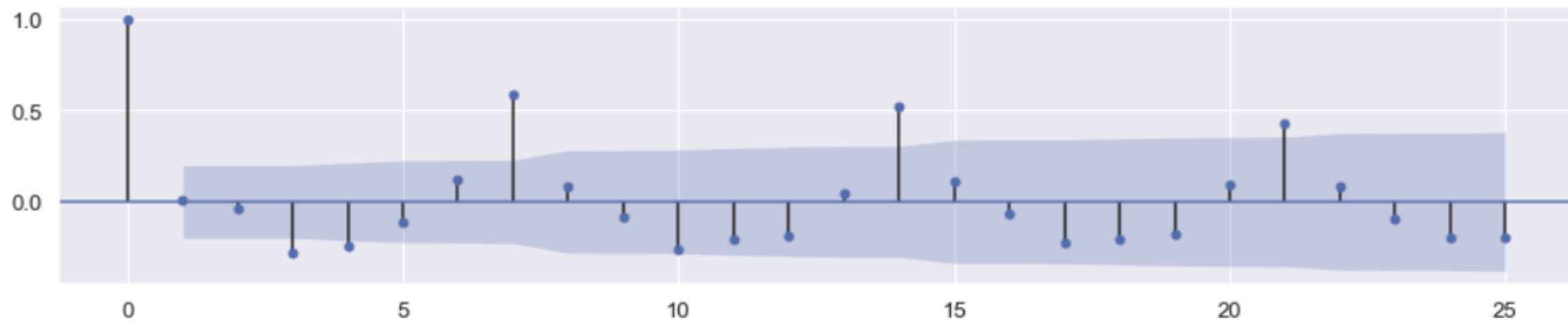


Source: (Nau, Identifying the numbers of AR or MA terms in an ARIMA model, n.d.)

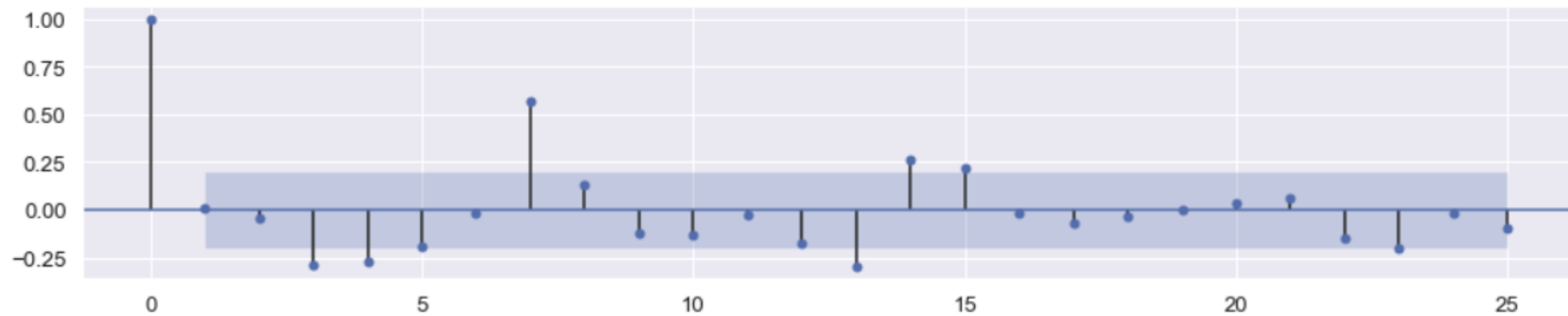
Moving Average (q)

- ❖ ACF shows sharper cutoff than PACF
- ❖ Select MA term as the number of significant spikes in ACF

Autocorrelation



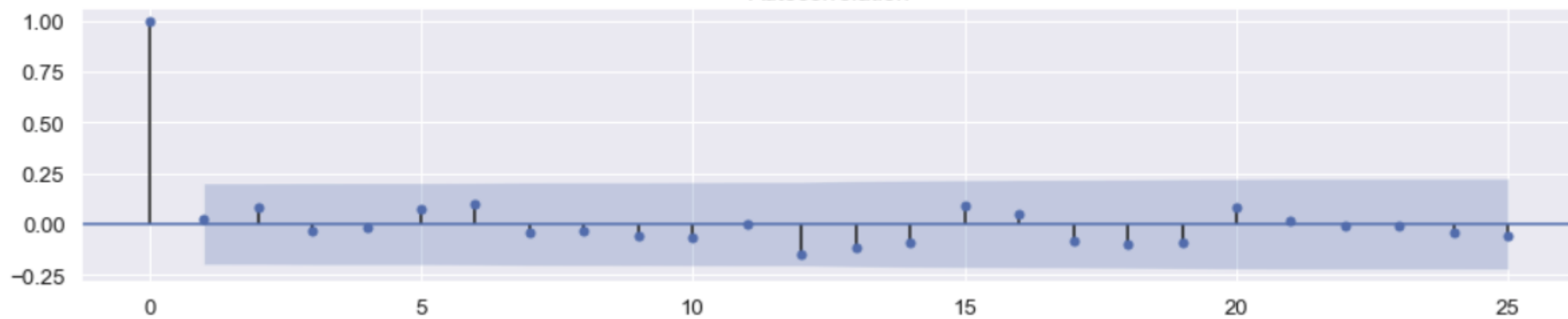
Partial Autocorrelation



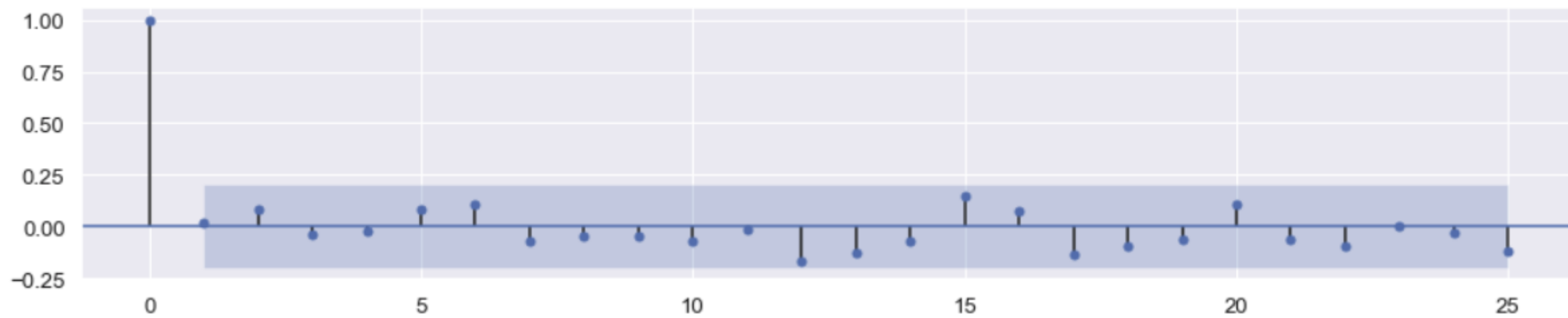
SARIMAX(p,d,q)(P,D,Q)m

- Seasonal AutoRegressive (P)
- Seasonal Integrated (D)
- Seasonal Moving Average (Q)
- Number of observations per seasonal cycle (m)
 - 7 – daily
 - 12 – monthly
 - 52 - weekly

Autocorrelation



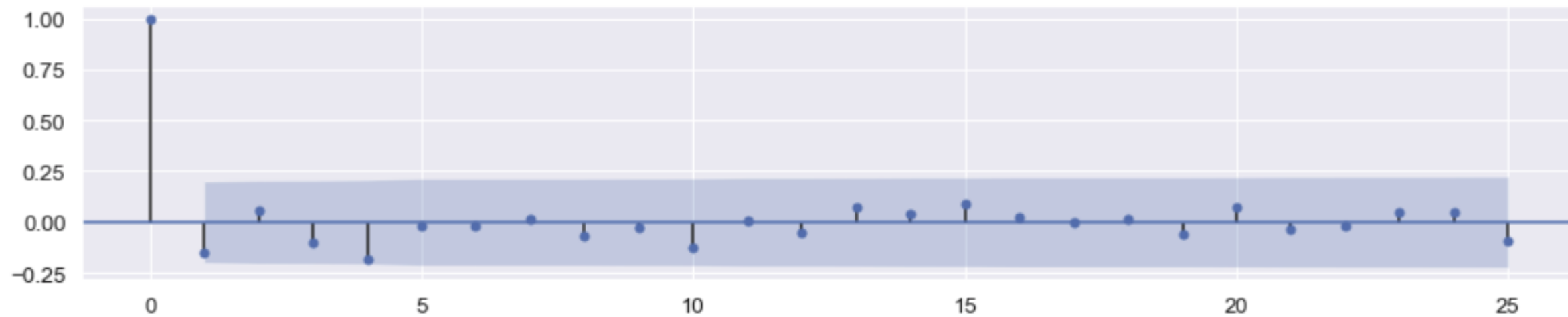
Partial Autocorrelation



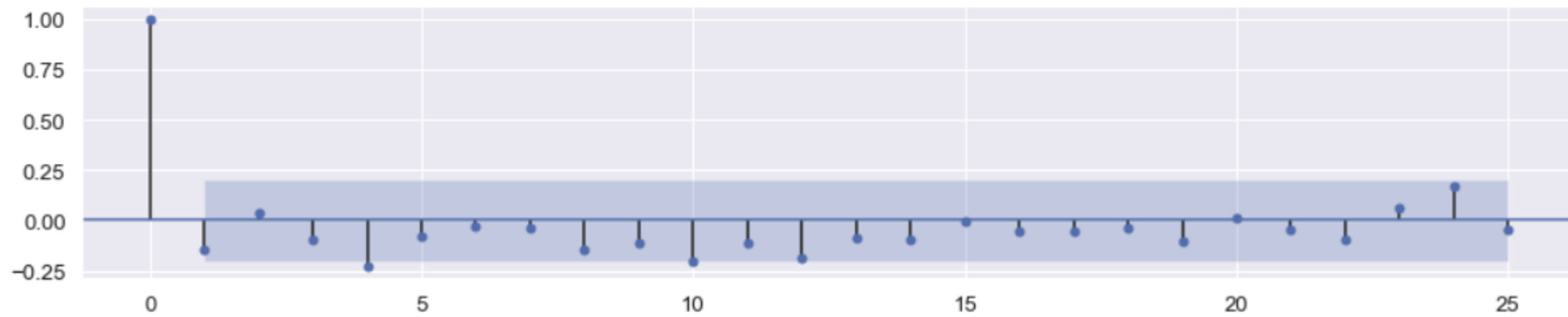
Bayesian Structural Time Series (BSTS)

- ☐ Trend
- ☐ Seasonality
- ☐ Auto-regression

Autocorrelation



Partial Autocorrelation



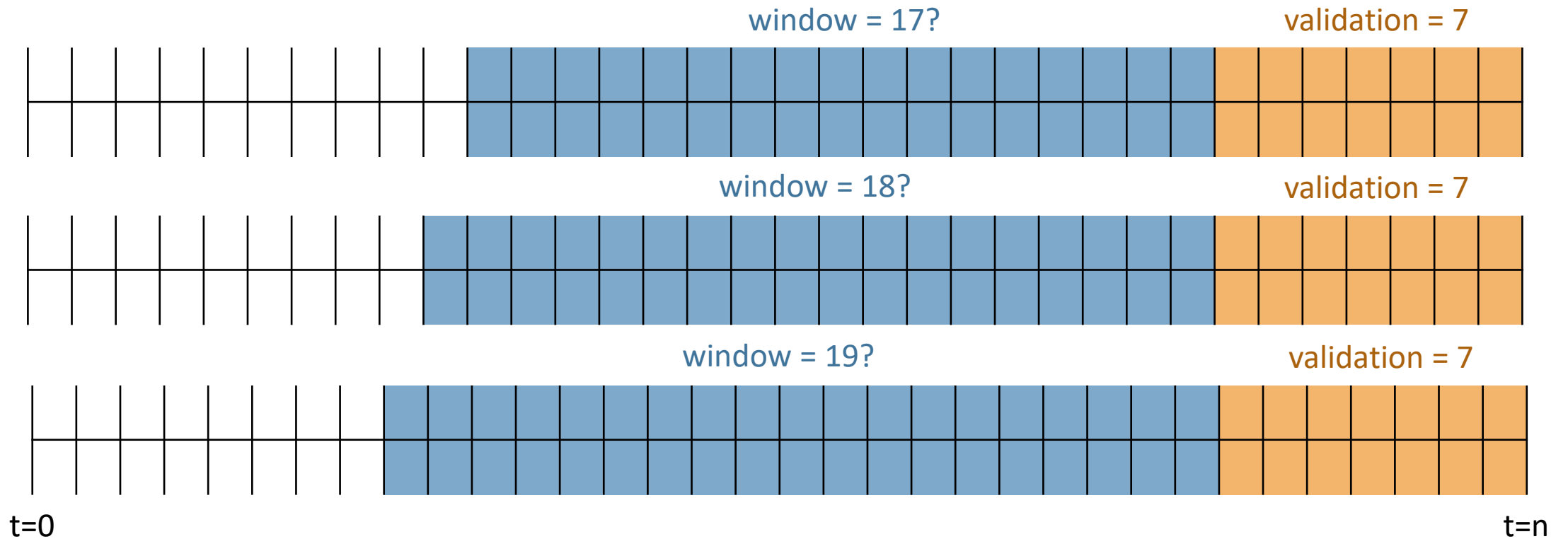
Forecasting 800+ Restaurants

- ❑ “pmdarima brings R’s beloved auto.arima to Python” (Smith, n.d.)
- ❑ Step-wise search for best model
 - ❑ Bias-corrected Akaike information criterion (AICc)

Model Tuning

Window Size

Validation size = forecast horizon



Model Evaluation

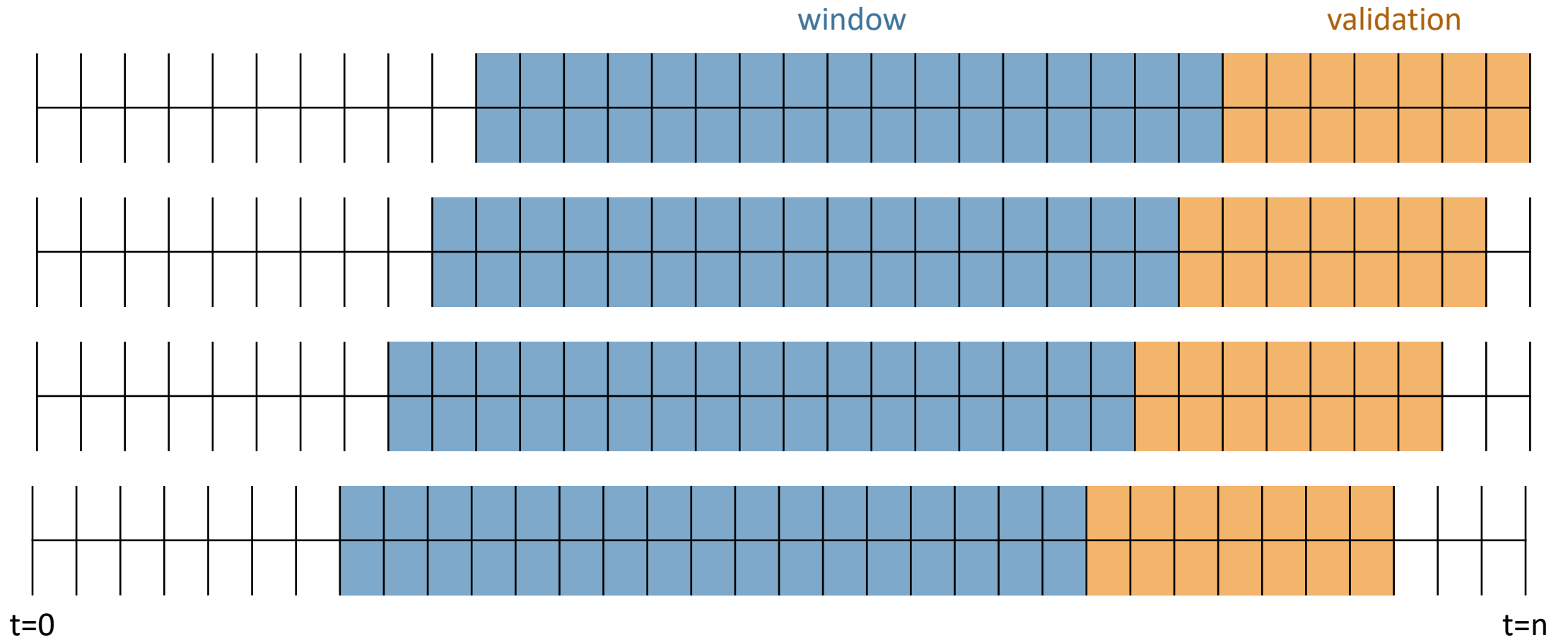
RMSLE over RMSE

- ❑ Robust to outliers
- ❑ Ignores scale of error
- ❑ Penalizes underestimation

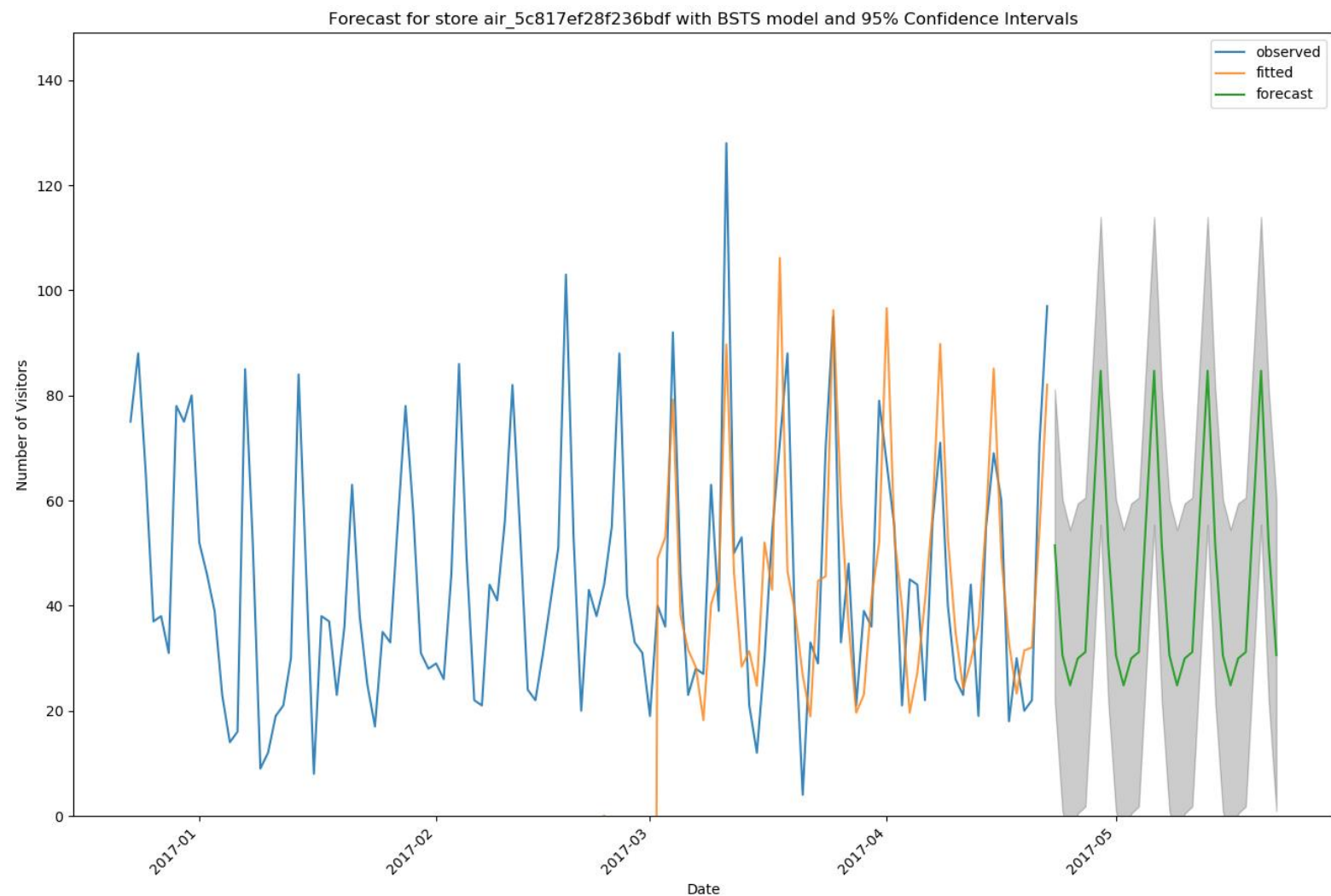
$$\sqrt{\frac{1}{n} \sum_{i=1}^n (\ln(p_i + 1) - \ln(a_i + 1))^2}$$

- ❑ n = total number of observations
- ❑ p_i = prediction for number of visitors
- ❑ a_i = actual number of visitors

Rolling Window Analysis

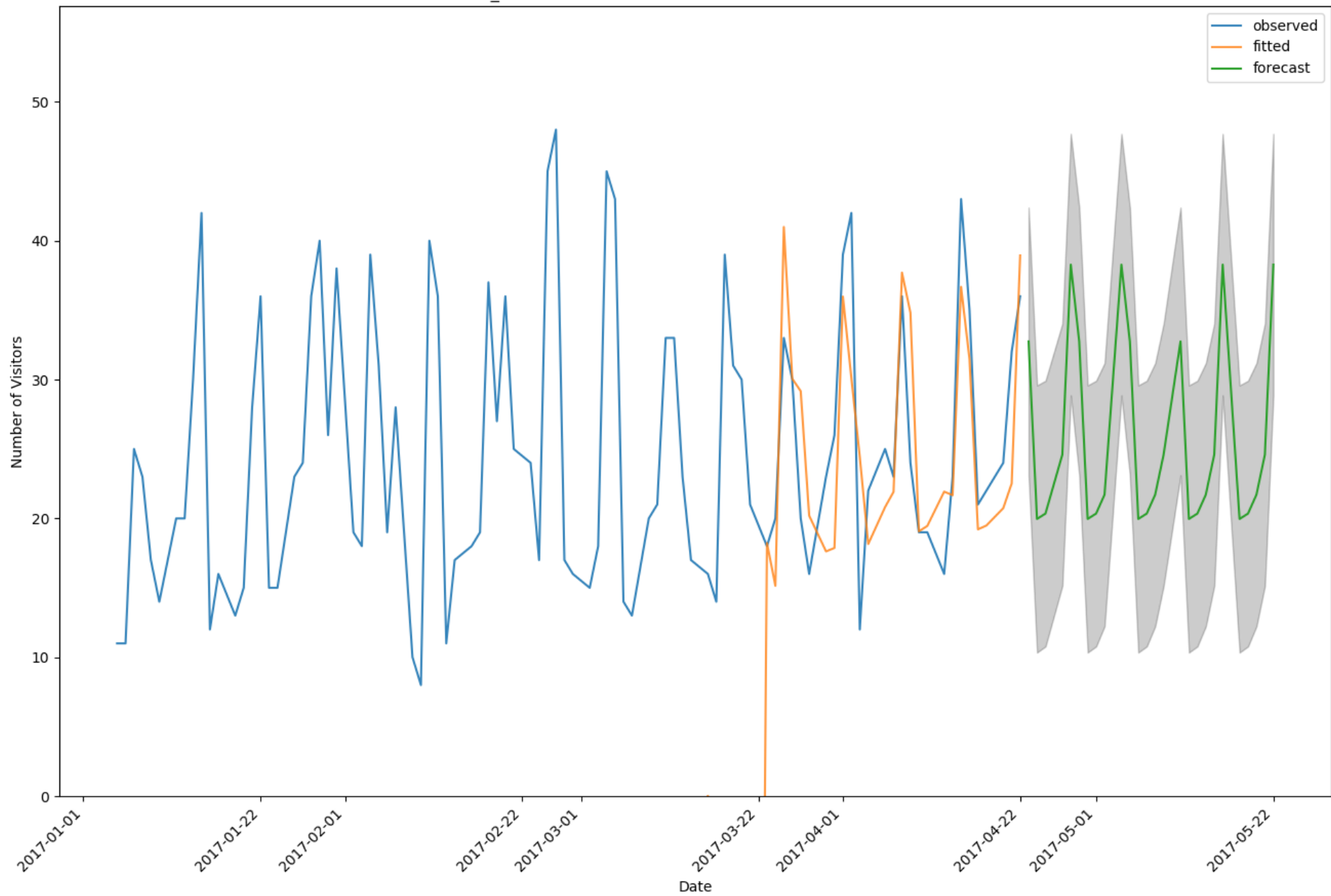


Forecasts

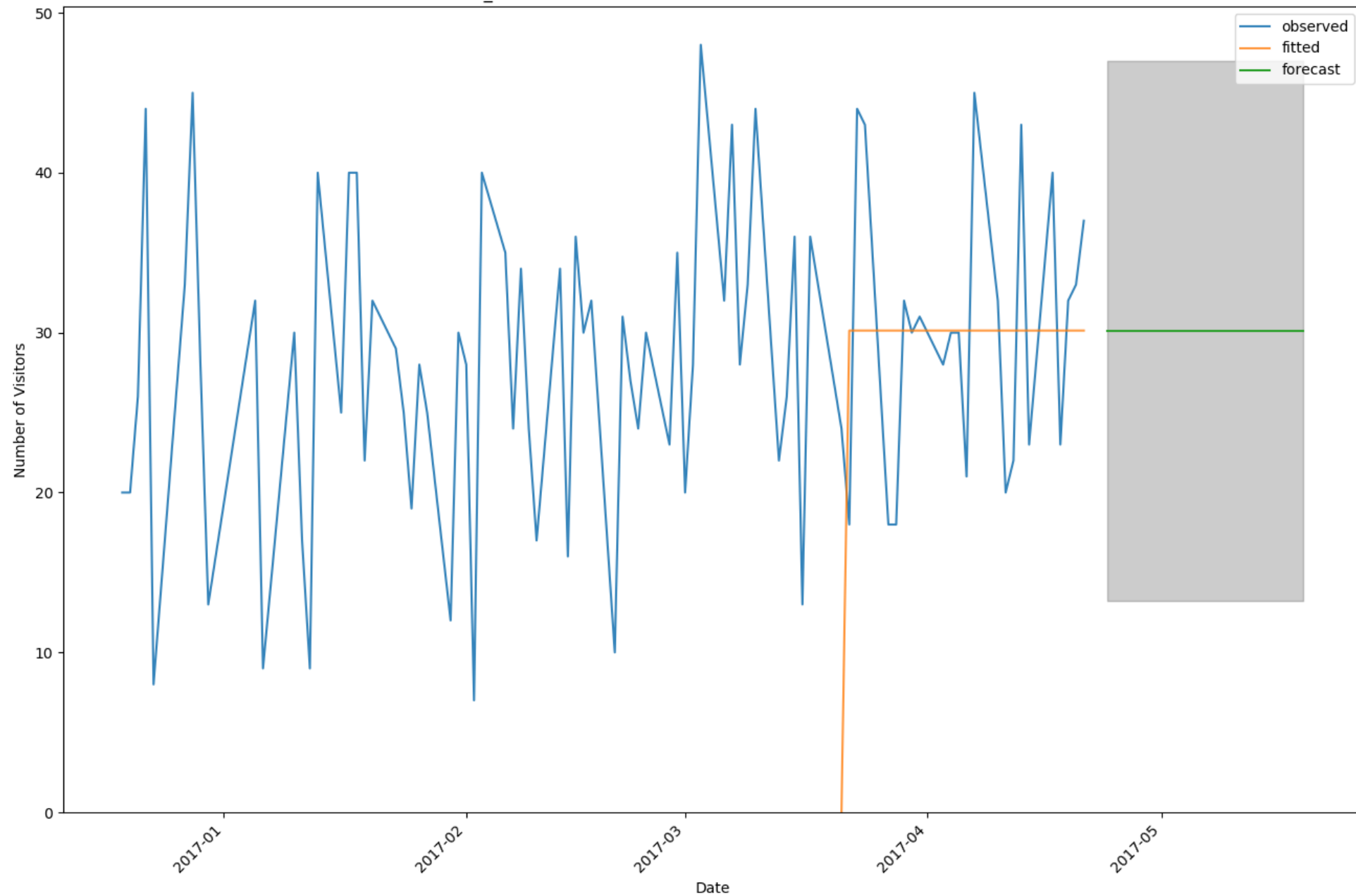


	visit_date	forecast	95_lower	95_upper
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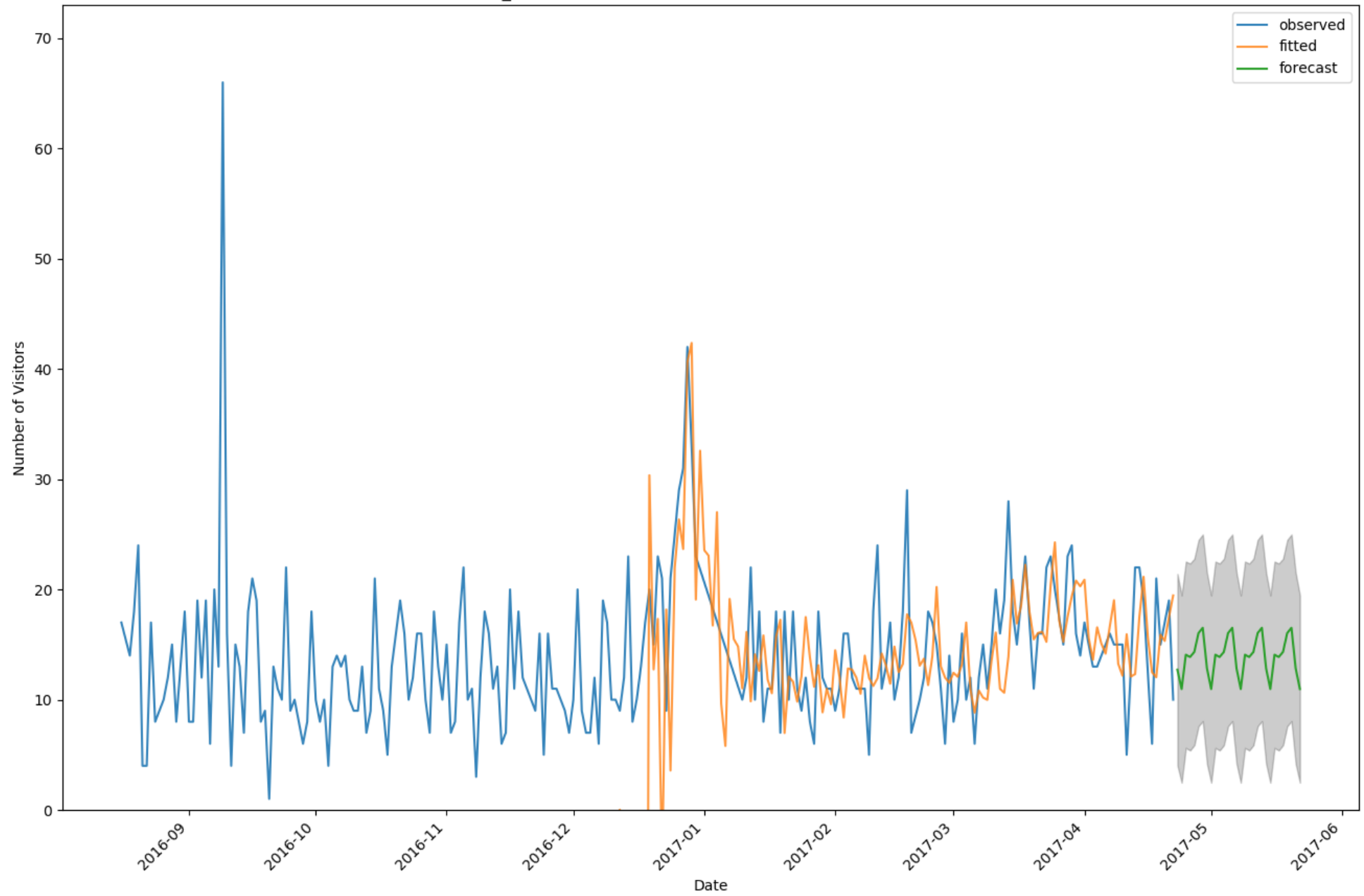
Forecast for store air_ebd31e812960f517 with BSTS model and 95% Confidence Intervals



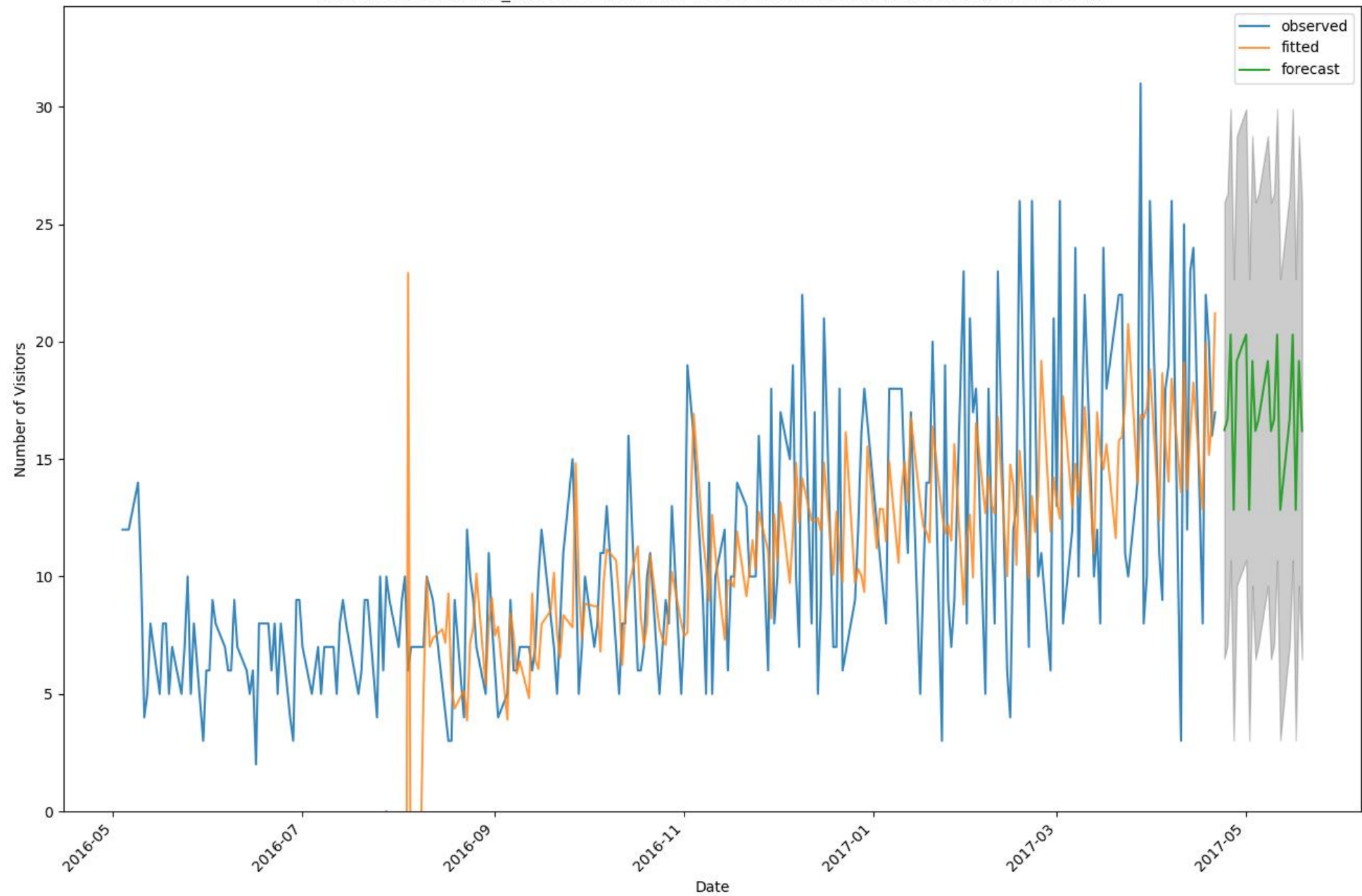
Forecast for store air_96929a799b12a43e with SARIMAX model and 95% Confidence Intervals



Forecast for store air_af24e3e817dea1e5 with BSTS model and 95% Confidence Intervals



Forecast for store air_e0118664da63a2d0 with BSTS model and 95% Confidence Intervals



Future Work

Possible Enhancements

- ☐ Add user interface
- ☐ Read data from database
- ☐ Parallelize with pySpark
- ☐ Add multivariate models

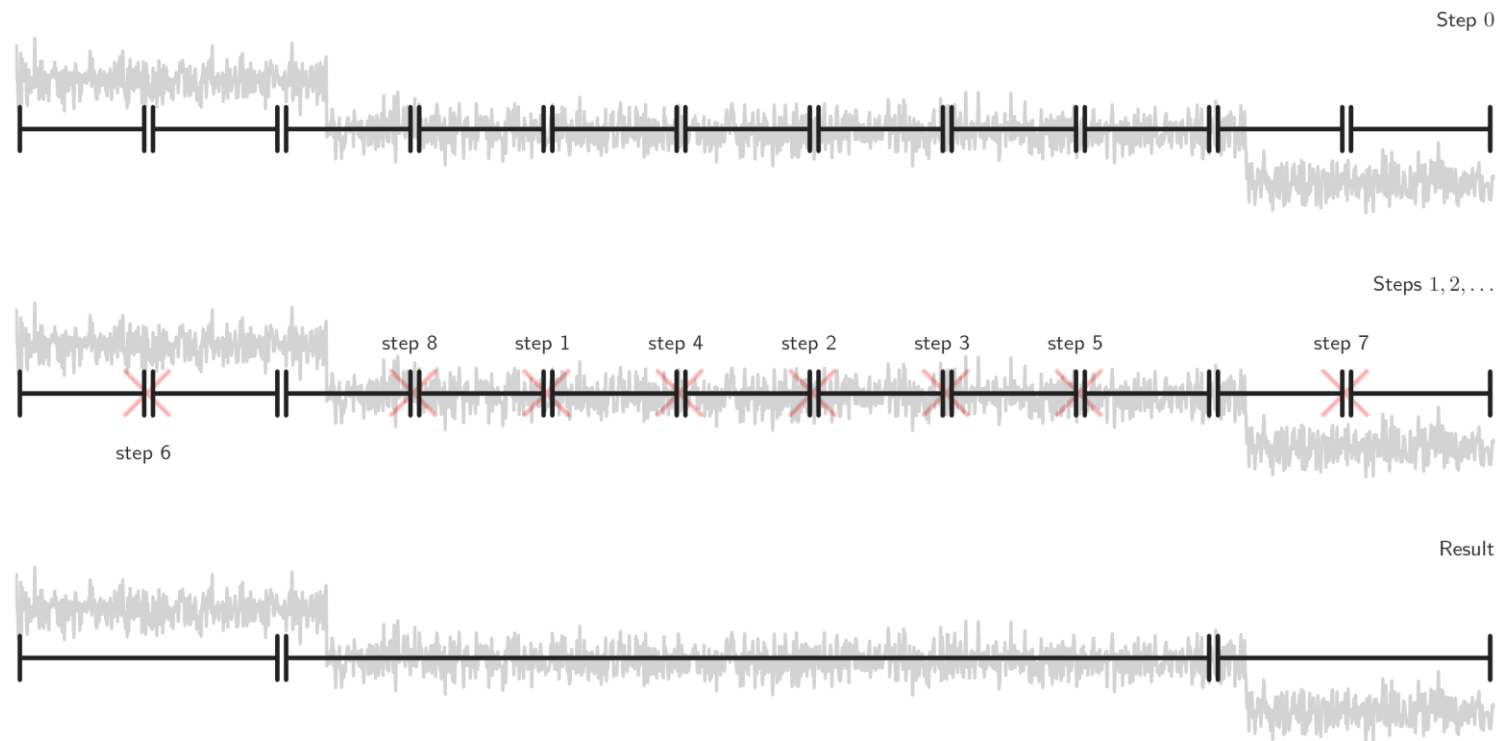
References

- ❑ Amin, H. (2018, October 2). Restaurant Food Waste is Killing Your Profit Margin—Here's How to Fix It. Retrieved from ChefHero | The Online Marketplace for Restaurant Supplies: <https://www.chefhero.com/blog/restaurant-food-waste-profit-margin>
- ❑ Hall, M. (2018, September 5). How to Efficiently Manage Labor Costs for Your Restaurant. Retrieved from Restaurant Insider: <https://upserve.com/restaurant-insider/labor-cost-guidelines-restaurant/>
- ❑ Jong, C. d. (2017, November 30). 3 Reasons Your Restaurant Employee Schedule is Costing You Money. Retrieved from Toast POS: <https://pos.toasttab.com/blog/restaurant-employee-schedule-cost>
- ❑ Lachapelle, J. (2018, October 4). The Restaurant Turnover Rate is Astronomical. Here's Why (And How to Fix It). Retrieved from ChefHero | The Online Marketplace for Restaurant Supplies: <https://www.chefhero.com/blog/restaurant-turnover-rate>
- ❑ Nau, R. (n.d.). Identifying the numbers of AR or MA terms in an ARIMA model. Retrieved from Statistical forecasting: notes on regression and time series analysis: <https://people.duke.edu/~rnau/411arim3.htm>
- ❑ Nau, R. (n.d.). Identifying the order of differencing in an ARIMA model. Retrieved from Statistical forecasting: notes on regression and time series analysis: <https://people.duke.edu/~rnau/411arim2.htm>
- ❑ Seth, Y. (2018, January 19). Understanding Time Series Modelling and Forecasting – Part 1. Retrieved from Let the Machines Learn: <https://yashueth.blog/2018/01/19/time-series-analysis-forecasting-modelling-arima/>
- ❑ Smith, T. G. (n.d.). pmdarima: ARIMA estimators for Python. Retrieved from pmdarima 1.2.1 documentation: <https://www.alkaline-ml.com/pmdarima/index.html>

Appendix

Bottom-up Segmentation

Complexity: $O(n \log n)$



Source: <http://ctruong.perso.math.cnrs.fr/ruptures-docs/build/html/detection/bottomup.html>

Bias-corrected Akaike information criterion (AICc)

- ❑ Estimates information lost
- ❑ Lower is better
- ❑ Balances complexity and goodness of fit
- ❑ Corrects for preference of AIC to select model with n parameters

Additional resources:

- ❑ <http://pages.stern.nyu.edu/~churvich/Forecasting/Handouts/AICC.pdf>