

SAMPLE SPACES

the **sample space** (Ω) of an experiment consists of all **sample points** (ω), each representing a different outcome.

example: a sequence of 3 coin flips

$$\Omega = \begin{array}{cccc} \text{HHH} & \text{HTH} & \text{TTH} & \text{TTT} \\ \text{HHT} & \text{HTT} & \text{THT} & \text{TTT} \end{array} \rightarrow \omega$$

(Note: In the original image, the entire set of outcomes is enclosed in a large green oval labeled Ω , and the outcome TTT is enclosed in a smaller green oval labeled ω .)

an **event** is a subset of the sample space

$$E_1 = \{ \text{HHH}, \text{TTT} \}$$

$$E_2 = \{ \text{HHT}, \text{HTH}, \text{TTH} \} \quad (\text{from } \Omega \text{ above})$$

PROBABILITY SPACES

a probability space consists of a sample space (Ω) and a probability for each sample point ($P(\omega)$)

the probabilities must satisfy

① $0 \leq P(\omega) \leq 1$ for all $\omega \in \Omega$

② $\sum_{\omega \in \Omega} P(\omega) = 1$

if every sample point has equal probability, the probability space is uniform

$$P(\omega) = \frac{1}{|\Omega|} \quad \forall \omega \in \Omega$$

PROBABILITIES OF EVENTS

to calculate the probability of an event E :

$$P(E) = \sum_{\omega \in E} P(\omega)$$

if the probability space is uniform, this is equivalent to

$$P(E) = \frac{|E|}{|\Omega|}$$

we can use counting techniques to find the size of these sets!

sometimes it's helpful to calculate $P(E)$ by finding $P(E) = 1 - P(\bar{E})$ where \bar{E} is the complement of E ($\bar{E} = \Omega \setminus E$)