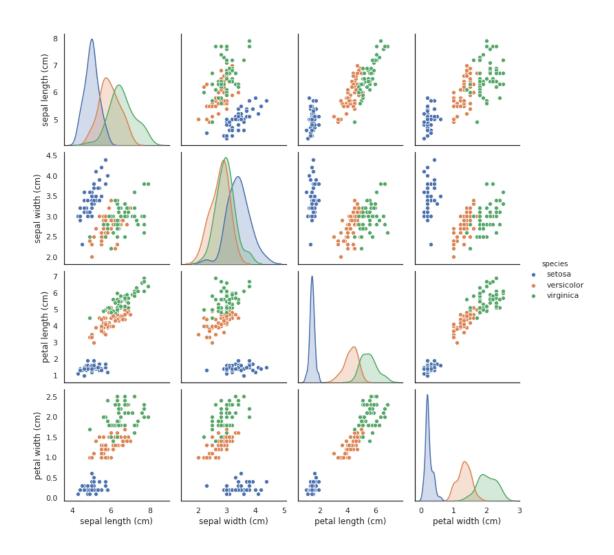
Untitled

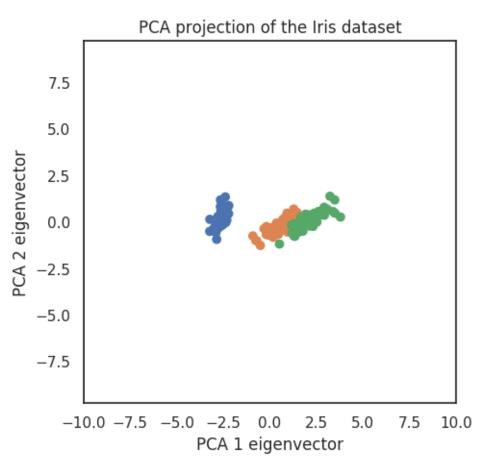
February 10, 2020

1 1. PCA Example of dimension reduction

/usr/bin/python Python 3.6.9



```
plt.xlabel('PCA 1 eigenvector')
plt.ylabel('PCA 2 eigenvector')
plt.gca().set_aspect('equal', 'datalim')
plt.title('PCA projection of the Iris dataset',fontsize = 12)
axes = plt.gca()
axes.set_xlim([-10,10])
axes.set_ylim([-10,10])
plt.show()
```



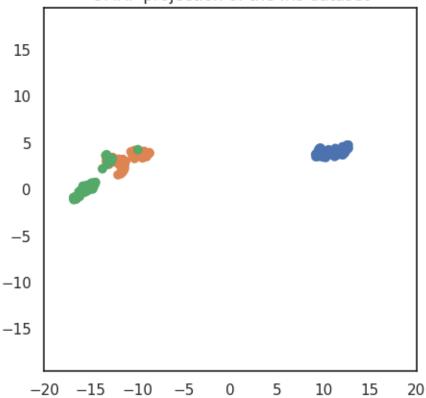
2 2. UMAP Example of dimension reduction

```
[4]: import umap
reducer = umap.UMAP()
embedding = reducer.fit_transform(iris.data)
embedding.shape
```

/home/henry/.local/lib/python3.6/site-packages/umap/spectral.py:229: UserWarning: Embedding a total of 2 separate connected components using metaembedding (experimental)

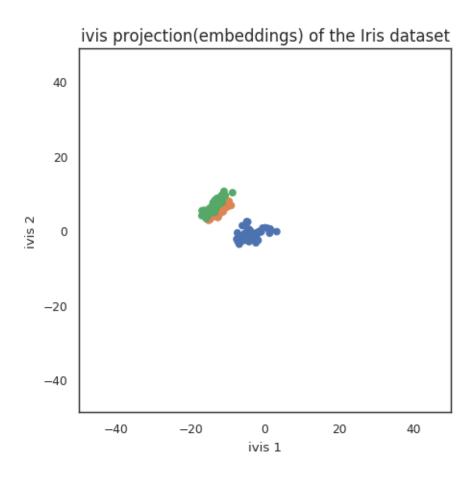
n_components





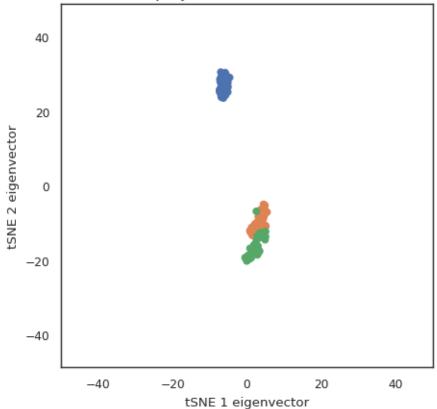
3 3. IVIS Example of dimension reduction

```
[5]: import seaborn as sns
     import matplotlib.pyplot as plt
     from sklearn.datasets import load_iris
     from sklearn.preprocessing import MinMaxScaler
     from ivis import Ivis
     sns.set(context='paper', style='white')
     X = load_iris().data
     X = MinMaxScaler().fit_transform(X)
     ivis = Ivis(k=5, model='maaten', verbose=0)
     ivis.fit(X)
     embeddings = ivis.transform(X)
     plt.figure(figsize=(5,5), dpi=100)
     plt.scatter(embeddings[:, 0],
                 embeddings[:, 1],
                 c=[sns.color_palette()[x] for x in iris.target])
                 #c=load_iris().target, s=20)
     plt.xlabel('ivis 1')
     plt.ylabel('ivis 2')
     plt.gca().set_aspect('equal', 'datalim')
     plt.title('ivis projection(embeddings) of the Iris dataset',fontsize = 12)
     axes = plt.gca()
     axes.set_xlim([-50,50])
     axes.set_ylim([-50,50])
     plt.show()
```



4 4. tSNE Example of dimension reduction

tSNE projection of the Iris dataset



5 5. Circular coordinates Example of dimension reduction

```
[8]: type(iris)
     iris_pd = pd.DataFrame(
         iris.data,
         columns=features)
     iris_pd[target] = iris.target
     iris_pd.head()
     iris_ar=iris_pd.to_numpy()
     type(iris_ar)
     iris_ar=iris_ar[:,0:3]
     print(iris_ar)
    [[5.1 3.5 1.4]
     [4.9 \ 3. \ 1.4]
     [4.7 3.2 1.3]
     [4.6 3.1 1.5]
     [5. 3.6 1.4]
     [5.4 3.9 1.7]
     [4.6 3.4 1.4]
     [5. 3.4 1.5]
     [4.4 2.9 1.4]
     [4.9 3.1 1.5]
     [5.4 3.7 1.5]
     [4.8 3.4 1.6]
     [4.8 3. 1.4]
     [4.3 3. 1.1]
     [5.8 4. 1.2]
     [5.7 4.4 1.5]
     [5.4 3.9 1.3]
     [5.1 3.5 1.4]
     [5.7 3.8 1.7]
     [5.1 3.8 1.5]
     [5.4 3.4 1.7]
     [5.1 3.7 1.5]
     [4.6 3.6 1.]
     [5.1 3.3 1.7]
     [4.8 3.4 1.9]
     [5. 3. 1.6]
     [5. 3.4 1.6]
     [5.2 3.5 1.5]
     [5.2 3.4 1.4]
     [4.7 \ 3.2 \ 1.6]
     [4.8 3.1 1.6]
     [5.4 3.4 1.5]
     [5.2 4.1 1.5]
     [5.5 4.2 1.4]
```

- [4.9 3.1 1.5]
- [5. 3.2 1.2]
- [5.5 3.5 1.3]
- [4.9 3.6 1.4]
- [4.4 3. 1.3]
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- [5. 3.5 1.3]
- [4.5 2.3 1.3]
- [4.4 3.2 1.3]
- [5. 3.5 1.6]
- [5.1 3.8 1.9]
- [4.8 3. 1.4]
- [5.1 3.8 1.6]
- [4.6 3.2 1.4]
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- [5. 3.3 1.4]
- [7. 3.2 4.7]
- [6.4 3.2 4.5]
- [6.9 3.1 4.9]
- [5.5 2.3 4.]
- [6.5 2.8 4.6]
- [5.7 2.8 4.5]
- [6.3 3.3 4.7]
- [4.9 2.4 3.3]
- [6.6 2.9 4.6]
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- [5.2 2.7 3.9] [5. 2. 3.5]
- [5.9 3. 4.2]
- [6. 2.2 4.]
- [6.1 2.9 4.7]
- [5.6 2.9 3.6]
- [6.7 3.1 4.4]
- [5.6 3. 4.5]
- [5.8 2.7 4.1]
- [6.2 2.2 4.5]
- [5.6 2.5 3.9]
- [5.9 3.2 4.8]
- [6.1 2.8 4.]
- [6.3 2.5 4.9]
- [6.1 2.8 4.7]
- [6.4 2.9 4.3]
- [6.6 3. 4.4]
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- [6.7 3. 5.]
- [6. 2.9 4.5]
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- [5.8 2.7 3.9]
- [6. 2.7 5.1]
- [5.4 3. 4.5]
- [6. 3.4 4.5]
- [6.7 3.1 4.7]
- $[6.3 \ 2.3 \ 4.4]$
- [5.6 3. 4.1]
- [5.5 2.5 4.]
- [5.5 2.6 4.4]
- [6.1 3. 4.6]
- [5.8 2.6 4.] [5. 2.3 3.3]
- [5.6 2.7 4.2]
- [5.7 3. 4.2]
- [5.7 2.9 4.2]
- [6.2 2.9 4.3]
- [5.1 2.5 3.]
- [5.7 2.8 4.1]
- [6.3 3.3 6.]
- [5.8 2.7 5.1]
- [7.1 3. 5.9]
- [6.3 2.9 5.6]
- $[6.5 \ 3. \ 5.8]$
- [7.6 3. 6.6]
- $[4.9 \ 2.5 \ 4.5]$
- [7.3 2.9 6.3]
- $[6.7 \ 2.5 \ 5.8]$
- [7.2 3.6 6.1]
- [6.5 3.2 5.1]
- [6.4 2.7 5.3]
- $[6.8 \ 3. \ 5.5]$
- [5.7 2.5 5.]
- [5.8 2.8 5.1]
- $[6.4 \ 3.2 \ 5.3]$
- $[6.5 \ 3. \ 5.5]$
- [7.7 3.8 6.7]
- [7.7 2.6 6.9]
- [6. 2.2 5.]
- $[6.9 \ 3.2 \ 5.7]$
- [5.6 2.8 4.9]
- [7.7 2.8 6.7]
- [6.3 2.7 4.9]
- [6.7 3.3 5.7]
- [7.2 3.2 6.]
- [6.2 2.8 4.8]
- [6.1 3. 4.9]
- $[6.4 \ 2.8 \ 5.6]$
- [7.2 3. 5.8]

```
[7.4 2.8 6.1]
     [7.9 3.8 6.4]
     [6.4 \ 2.8 \ 5.6]
     [6.3 2.8 5.1]
     [6.1 2.6 5.6]
     [7.7 3. 6.1]
     [6.3 3.4 5.6]
     [6.4 3.1 5.5]
     [6. 3. 4.8]
     [6.9 \ 3.1 \ 5.4]
     [6.7 3.1 5.6]
     [6.9 3.1 5.1]
     [5.8 2.7 5.1]
     [6.8 \ 3.2 \ 5.9]
     [6.7 \ 3.3 \ 5.7]
     [6.7 \ 3. \ 5.2]
     [6.3 2.5 5.]
     [6.5 \ 3. \ 5.2]
     [6.2 \ 3.4 \ 5.4]
     [5.9 3. 5.1]]
[9]: import dionysus as dionysus
     prime = 23
     vr = dionysus.fill_rips(iris_ar, 2, 10.) #Vietoris-Rips complex
     cp = dionysus.cohomology_persistence(vr, prime, True) #Create the persistent

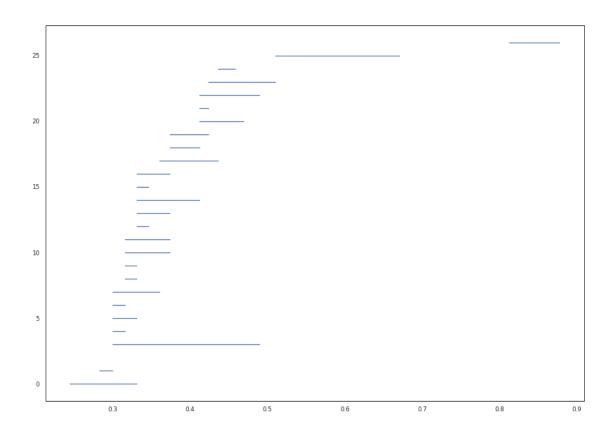
⊔
     ⇔cohomology based on the chosen parameters.
     dgms = dionysus.init_diagrams(cp, vr) #Calculate the persistent diagram using_
     → the designated coefficient field and complex.
     dionysus.plot.plot_bars(dgms[1], show=True)
     threshold = 0.1
```

bars = [bar for bar in dgms[1] if bar.death-bar.birth > threshold] #choosing_

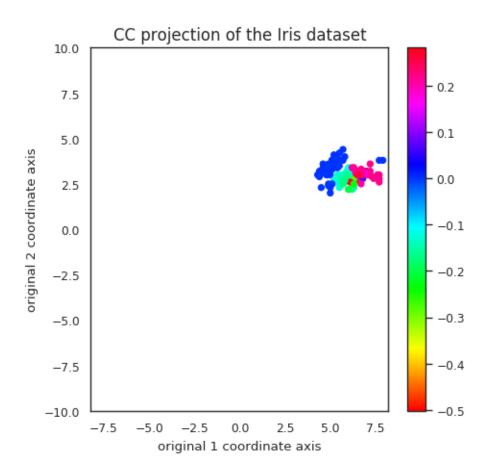
⇒cocycle that persist at least threshold=1.

cocycles = [cp.cocycle(bar.data) for bar in bars]

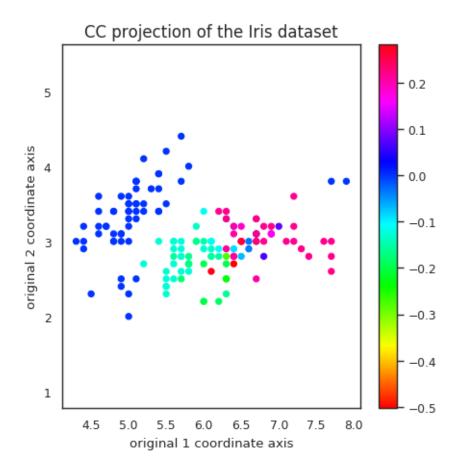
#print(coords)



```
[10]: chosen_cocycle= cocycles[0]
      chosen_bar= bars[0]
      vr_8 = dionysus.Filtration([s for s in vr if s.data <= max([bar.birth for bar__
      →in bars])])
      coords = dionysus.smooth(vr_8, chosen_cocycle, prime)
      plt.figure(figsize=(5,5), dpi=100)
      plt.scatter(iris_ar[:,0],iris_ar[:,1],s=20, c=coords, cmap="hsv")
      #scatter(*annulus.T, c= color, cmap="hsv")
      plt.colorbar()
      plt.xlabel('original 1 coordinate axis')
      plt.ylabel('original 2 coordinate axis')
      plt.gca().set_aspect('equal', 'datalim')
      plt.title('CC projection of the Iris dataset',fontsize = 12)
      axes = plt.gca()
      axes.set_xlim([-10,10])
      axes.set_ylim([-10,10])
      plt.show()
```



```
[11]: plt.figure(figsize=(5,5), dpi=100)
    plt.scatter(iris_ar[:,0],iris_ar[:,1],s=20, c=coords, cmap="hsv")
    #scatter(*annulus.T, c= color, cmap="hsv")
    plt.colorbar()
    plt.xlabel('original 1 coordinate axis')
    plt.ylabel('original 2 coordinate axis')
    plt.gca().set_aspect('equal', 'datalim')
    plt.title('CC projection of the Iris dataset',fontsize = 12)
    #axes = plt.gca()
    #axes.set_xlim([-10,10])
    #axes.set_ylim([-10,10])
    plt.show()
```



6 Reference