Feedback Control of Dynamic Bipedal Robot Locomotion Eric R. Westervelt, Jessy W. Grizzle, Christine Chevallereau, Jun Ho Choi, and Benjamin Morris

## **Errata**

Known errors and correction as of July 17, 2010.

• Page 58 (Submitted by Kaveh Akbari Hamed): Equation (3.31) should be the following.

$$\mathcal{S} := \{ (q_{s}, \dot{q}_{s}) \in T\mathcal{Q}_{s} \mid p_{2}^{v}(q_{s}) = 0, \ p_{2}^{h}(q_{s}) > 0 \}.$$

• Page 63 (Submitted by Kaveh Akbari Hamed): Equation (3.57) should be the following.

$$\tilde{\Sigma}: \left\{ \begin{array}{ll} \dot{\tilde{x}} = \tilde{f}_{\mathrm{s}}(\tilde{x}) + \tilde{g}_{\mathrm{s}}(\tilde{x})v & \tilde{x}^{-} \notin \mathcal{S} \\ \tilde{x}^{+} = \tilde{\Delta}(\tilde{x}^{-}) & \tilde{x}^{-} \in \mathcal{S}, \end{array} \right.$$

• Page 67 (Submitted by Hae Won Park): Equation (3.67) should be the following.

$$(C_{s}(q,\dot{q}))_{1,2} = -\frac{1}{2}mr^{2}\sin(\theta_{1} - \theta_{2})\dot{\theta}_{2}$$

$$(C_{s}(q,\dot{q}))_{1,3} = M_{T}r\ell\sin(\theta_{1} - \theta_{3})\dot{\theta}_{3}$$

$$(C_{s}(q,\dot{q}))_{2,1} = \frac{1}{2}mr^{2}\sin(\theta_{1} - \theta_{2})\dot{\theta}_{1}$$

$$(C_{s}(q,\dot{q}))_{3,1} = -M_{T}r\ell\sin(\theta_{1} - \theta_{3})\dot{\theta}_{1}$$

- Page 93 (Submitted by Kaveh Akbari Hamed): In item (e), " $\varphi^+(t) := \lim_{\tau \nearrow t} \varphi(\tau)$ " should be " $\varphi^-(t) := \lim_{\tau \nearrow t} \varphi(\tau)$ ".
- Page 95 (Submitted by Kaveh Akbari Hamed): On the first line, " $\mathcal{X}_2$ " should be " $\mathcal{X}_1$ ".
- Page 107 (Submitted by Kaveh Akbari Hamed): The following hypothesis should be added to list of hypotheses for Proposition 4.3:
  - 5.  $\mathcal{Z}_{(\alpha \to \beta)}$  is forward invariant and continuously finite-time attractive under  $f_{(\alpha \to \beta)}$ .
- Page 147 (Submitted by Kaveh Akbari Hamed): In Table 6.1, "0.813" should be "0.662".
- Pages 153,154: NEC2, NEC4, and NEC5 should be NIC4, NIC5, and NIC6, respectively.
- Page 158 (Submitted by Thomas Schauss): Equation (6.67) should be the following.

$$\left[L_{\tilde{g}}L_{\tilde{f}}h(\tilde{q})\right]^{-1} = \mathbf{I}_{(N-1)\times(N-1)} - \frac{1}{\det(L_{\tilde{q}}L_{\tilde{f}}h)(\tilde{q})} \frac{\partial h_d(\theta)}{\partial \theta} \, \tilde{J}^{\mathrm{norm}}(q_{\mathrm{b}}).$$

• Page 158 (Submitted by Thomas Schauss): Equation (6.68) should be the following.

$$\begin{split} \left[L_{\tilde{g}}L_{\tilde{f}}h(\tilde{q})\right]^{-1} &= \mathbf{I}_{(N-1)\times(N-1)} \\ &- \left(\frac{1}{\tilde{d}_{N,N}(q_{\mathbf{b}}) + \left[\tilde{d}_{N,1}(q_{\mathbf{b}}), \cdots, \tilde{d}_{N,(N-1)}(q_{\mathbf{b}})\right] \frac{\partial h_d(\theta)}{\partial \theta}}\right) \\ &- \left(\frac{\partial h_d(\theta)}{\partial \theta} \left[\tilde{d}_{N,1}(q_{\mathbf{b}}), \cdots, \tilde{d}_{N,(N-1)}(q_{\mathbf{b}})\right]\right). \end{split}$$

• Page 195 (Submitted by Amine Kamel): Equation (7.9) should be the following.

$$\left[\begin{array}{c} \alpha_0 \\ \theta_{\alpha}^+ \end{array}\right] = HRH^{-1} \left[\begin{array}{c} \alpha_M \\ \theta_{\alpha}^- \end{array}\right]$$

- Page 242: "10.1 W" should be "40.4 W"
- Page 245: "8.9 W" should be "35.6 W"
- Page 398 (Submitted by Kaveh Akbari Hamed): Equation (B.83) should be the following.

$$ilde{f}^*(\eta,z) = \left[ egin{array}{c} ilde{f}_1^*(\eta_1) \ dots \ ilde{f}_m^*(\eta_m) \ ilde{f}_{r+1}(\eta,z) \ dots \ ilde{f}_n(\eta,z) \end{array} 
ight]$$

• Page 398 (Submitted by Kaveh Akbari Hamed): Equation (B.85) should be the following.

$$\tilde{f}^*\Big|_{\mathcal{Z}}(z) = \begin{bmatrix} \tilde{f}_{r+1}(0,z) \\ \vdots \\ \tilde{f}_n(0,z) \end{bmatrix}$$

• Page 431 (Submitted by Hae Won Park): Equation (B.204) should be the following.

$$\bar{D}(\bar{q}) = \left. \left( \frac{\partial F(q)'}{\partial q}' \right)^{-1} D(q) \left( \frac{\partial F(q)}{\partial q} \right)^{-1} \right|_{q = F^{-1}(\bar{q})}$$

• Page 432 (Submitted by Noah Cowan): Equation (B.211) should be the following.

$$\Gamma = \begin{bmatrix} -\left(\frac{\partial \lambda(q_1)}{\partial q_1}\right)' \\ \mathbf{I} \end{bmatrix} u^*(q, \dot{q}),$$

• Page 432 (Submitted by Noah Cowan): Equation (B.212) should be the following.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} x_2 \\ D^{-1}(x_1) \left( -C(x_1, x_2)x_2 - G(x_1) + \begin{bmatrix} -\left(\frac{\partial \lambda(q_1)}{\partial q_1}\right)' \\ I \end{bmatrix} u^*(x_1, x_2) \right) \end{bmatrix}.$$

• Page 432 (Submitted by Kaveh Akbari Hamed): Equation (B.214) should be the following.

$$D(q_1, q_2) = \begin{bmatrix} D_{11}(q_1, q_2) & D_{12}(q_1, q_2) \\ D'_{12}(q_1, q_2) & D_{22}(q_1, q_2) \end{bmatrix}$$

• Page 432 (Submitted by Noah Cowan): Equation (B.216) should be the following.

$$\Gamma \cdot \dot{q} = \left( \left[ -\left( \frac{\partial \lambda(q_1)}{\partial q_1} \right)' \right] u^* \right)' \dot{q} = (u^*)' \frac{d}{dt} \left( q_2 - \lambda(q_1) \right),$$

• Page 438 (Submitted by Oscar E. Ramos Ponce): Equation (B.234b) should be the following.

$$(G_{\rm s}(q_1, q_2))_2 = \left(m_1 g_0 L_2 + m_2 g_0 \ell_{\rm cm, 2}^{\rm h}\right) \cos(q_2) + m_1 g_0 \ell_{\rm cm, 1}^{\rm h} \cos(q_1 + q_2),$$

- Page 441 (Submitted by Kaveh Akbari Hamed): On the second line of Section C.1.4, " $T_I(x) < \infty$ " should be " $T_I(\Delta(x)) < \infty$ ".
- Page 445 (Submitted by Kaveh Akbari Hamed): Equation (C.25) should be the following.

$$\mathcal{D}T_{I}^{\epsilon}(\hat{\Delta}(z_{2:k}^{*},\eta^{*})) = -(L_{f^{\epsilon}}H(x^{*}))^{-1}\frac{\partial H}{\partial x}(x^{*})\Phi^{\epsilon}(t^{*},\hat{\Delta}(z_{2:k}^{*},\eta^{*})).$$